

# Combining Aggregate and Plant-Level Data to Estimate a Discrete-Choice Demand Model\*

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## Abstract

This paper builds on the methodology developed by Katayama, Lu and Tybout (2003), who use a nested logit demand model to estimate demand parameters from plant-level data that usually report only revenue and cost figures. I demonstrate how to extend their framework by including the extra information provided by commonly available data on aggregate physical output. Using data from the Colombian beer industry from 1977 to 1990, the model, estimated through Bayesian Monte Carlo Methods, shows a sizeable precision gain in the parameter estimates once the aggregate variable is included.

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*JEL Codes:* L10, L11, C11, C15.

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## 1. Introduction

The objective of this paper is to extend the existing literature on the estimation of demand parameters using plant-level data sets, which typically report only revenue and cost figures. A common approach to estimate these parameters is given from a regression of output values on input values<sup>1</sup> following Hall's (1990) approach. There, he demonstrates that, under imperfect competition, a demand parameter shows up in the regression equation. Klette (1999), employing Norwegian plant-level data, used Hall's approach to make inference about demand parameters and to evaluate firms' market power. However, like most plant-level studies<sup>2</sup> plant-level quantities are obtained by simply deflating the revenue series by a commonly available price index. This procedure is appropriate when goods are perfect substitutes, however it can be seriously misleading when the degree of product differentiation is not negligible.

Only recently, through the works of Klette and Griliches (1996), Melitz (2000) and DeSouza (2004), researchers gave a closer look into this issue. They all assume monopolistic competition and a CES demand for differentiated products. DeSouza's result is closer to the object developed in this paper – the other two papers are rather concerned with the estimation of technology parameters. Indeed, DeSouza estimates the CES demand parameter under the assumption that firms are monopolistically competitive, and concludes that studies that neglect price differentiation, and therefore price heterogeneity, tend to find misleading evidence of highly elastic demands.

However, the assumption of monopolistic competition may not be a reasonable model for many industries. It assumes that firms are not big enough to influence the aggregate market variables and therefore a price change by one firm has an irrelevant effect on the demand of any other firm. This assumption states that each product has no neighbor in the product space, which strongly restricts cross-effects and strategic interaction between products (Tirole, 1988).

The discrete-choice based demand function with oligopolistic competition avoids some of the undesirable results of the monopolistic setup. Consumers choose among  $N$  products given the product's prices and characteristics. Producers, in turn, set optimal prices in a Bertrand fashion. This allows for a richer model of cross-effect patterns and interactions among firms. Berry (1994) and Berry et al. (1995), henceforth referred to as BLP, develop an econometric methodology to estimate such model using market-level data on prices and quantities.

Along the same lines, Katayama et al. (2003) – KLT from now on – use a nested logit demand model and a price setting game to derive consumer and producer surplus and to measure firms' efficiency. Their work, however, differs from Berry's

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<sup>1</sup>If the econometrician can observe product-level prices and quantities or consumer-level choices, demand and supply parameters can be estimated directly using Berry's (1994) or Goldberg's (1995) frameworks.

<sup>2</sup>Another example is Botasso and Sembenelli (2001).

since the data set used there is not as informative. They develop a methodology to uncover demand parameters from plant-level data that report only revenue and cost figures. Using data from the Colombian beer industry, originally containing only plant-level information on revenue and total costs from 1977 to 1990, I shall demonstrate how to extend the KLT framework by including the extra information provided by aggregate data. Although it may be difficult to obtain detailed data on quantities at the plant level, the same is not true for aggregate variables in many cases. For instance, in the beverage sector, the amount of beer, in liters, consumed in a given year is widely available for many countries. The United Nations common database reports the total production of many goods for a long list of countries. Thus, the methodology proposed here qualifies as an extension to the KLT framework as it applies not only to the Colombian beer industry, but also to the data sets of many industries currently available to economists.

Aggregate quantities also carry information on demand parameters and therefore may help in the estimation process. Integrating different data sets to improve the quality of inference is not new in the economic field. Examples include Petrin (2002) and Berry et al. (2004). The first paper combines market-level data on car purchases to data on the averaged characteristics of consumers that purchase different types of car (e.g. minivans, station wagons and SUVs). The second paper develops a methodology to deal with consumer-level data on car purchases augmented by information on consumers' second choices if their first choices were not available. Another important contribution is provided by Imbens and Lancaster (1994), who suggest bringing macro data to microeconomic models. A common conclusion found in these papers is the precision gain (measured by the  $t$ -values) in the parameter estimates. The same conclusion is reached in this paper.

This paper is organized as follows. Section 2 describes the traditional approaches to estimating discrete-choice based demands. The next section provides details of the data set to be analyzed. The subsequent section shows how to incorporate the aggregate information into the model. And finally, the last section discusses the results.

## 2. Traditional Approaches to Estimating Discrete-Choice Demand Parameters

In this section, I shall describe the discrete-choice model commonly used in the literature and the different econometric strategies to estimate its parameters.

Consumers rank products according to their characteristics and prices. There are  $N + 1$  choices in the market,  $N$  inside goods and one outside good. Consumer  $i$  chooses a good  $j$ , given price  $p_j$ , observed and unobserved characteristics<sup>3</sup> ( $x_j$  and  $\xi_j$  respectively), and unobserved idiosyncratic preferences  $\epsilon_{ij}$ , according to the following equation:

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<sup>3</sup>For notational convenience I include only one observed characteristic, but more generally, there could be more.

$$u_{ij} = x_j \beta_1(h_i; \theta_1) - p_j \beta_2(h_i; \theta_2) + \xi_j + \epsilon_{ij} \quad (1)$$

where  $\beta_1(h_i; \theta_1)$  is a function of a vector of demographic variables  $h_i$ , such as income, age, and marital status and  $\theta_1$  is a vector of parameters defining that function. The coefficient for price,  $\beta_2(h_i; \theta_2)$ , is defined similarly.

Assuming that  $\epsilon_{ij}$  has a Type I Extreme Value distribution, the probability of individual  $i$  choosing good  $j$  takes the familiar logit form

$$prob(j/h_i) = \frac{\exp(x_j \beta_1(h_i; \theta_1) - p_j \beta_2(h_i; \theta_2) + \xi_j)}{\sum_k \exp(x_k \beta_1(h_i; \theta_1) - p_k \beta_2(h_i; \theta_2) + \xi_k)} \quad (2)$$

If the econometrician observes prices, individuals' choices and their characteristics, the vector of parameters can be estimated by setting up the maximum likelihood profile of all the observed consumer choices. Goldberg (1995) and Trajtenberg (1990) are two examples of this approach. The former author observes the new car choices of a random sample of consumers in the U.S. from the Consumer Expenditure Survey, whereas the latter author collected data on purchases of CT scanners.<sup>4</sup>

Suppose now that consumer-level data are not available, the econometrician observes only prices, market shares, and characteristics. Then, the estimation procedure has to be modified, since it is no longer possible to construct the maximum likelihood profile. Instead, some aggregation argument has to be invoked.

Indeed, taking the expected value with respect to consumer attributes  $h$  yields the market share implied by the model  $s_j = E[prob(j/h)]$ , which in extensive form is simply

$$s_j(x, p, \theta, \xi) = \int \frac{\exp(x_j \beta_1(h_i; \theta_1) - p_j \beta_2(h_i; \theta_2) + \xi_j)}{\sum_k \exp(x_k \beta_1(h_i; \theta_1) - p_k \beta_2(h_i; \theta_2) + \xi_k)} dF(h) \quad (3)$$

A regression equation can now be written by matching observed market share of product  $j$  ( $\bar{s}_j$ ) with the one implied by the model, which gives

$$\bar{s}_j = s_j(x, p, \theta, \xi) \quad (4)$$

Firms take into account the unobservables ( $\xi$ ) when setting their prices. Thus, the endogeneity of prices requires the use of instrumental variables. However, usual IV estimation techniques do not apply since the unobservables enter the regression equation nonlinearly. Some simulation method has to be applied. Shortly, it involves solving for the  $\xi_j$ 's given data and the parameters to construct moment restrictions conditional on available instruments (for further details, see Berry (1994), and BLP).

<sup>4</sup>Actually, these authors use a variation of the logit model known as the nested logit model, which I shall discuss later in this paper.

When setting prices, firms take into account demand and cost determinants. Therefore, the pricing decision also contains information on consumer preferences such that efficiency can be improved by incorporating this information into the estimation procedure.

First, assume that each firm  $f$  produces a subset  $F_f$  of the goods sold in this market and maximizes the sum of profits given by

$$\Pi_f = \sum_{j \in F_f} (p_j - mc_j) M s_j \quad (5)$$

where  $M$  is the total market size and  $mc_j$  is the marginal cost of producing brand  $j$ .

Then, it can be shown that the price  $p_j$  of any product  $j$  produced by firm  $f$  must satisfy the following equation.<sup>5</sup>

$$s_j + \sum_{r \in F_f} (p_r - mc_r) \frac{\partial s_r}{\partial p_j} = 0 \quad (6)$$

Note that (6) is flexible enough to accommodate different market structures. The first structure is the single-product firm, in which the firm can only control the price of its unique brand. The second is the multiproduct firm, in which the firm internalizes the price decision of all of its brands.

In turn, let marginal cost be modeled as

$$mc_j = w_j \gamma + \psi_j$$

where  $w_j$  is a vector of product characteristics and  $\psi_j$  is an unobserved cost component. Similarly to the demand-side unobservable, given  $(x, p, \theta, \xi, w, \gamma)$ , one can solve for the vector  $\psi$  from the quasi-supply relation (6) and set up the moment conditions based on appropriate instruments. All the parameters of the model can then be estimated through GMM using the demand and supply-side moments. KLT go a little further by devising a methodology to estimate the demand parameters without directly observed market-level data (prices and market shares).

### 3. Data

The data set consists of an unbalanced panel of plants in the beer industry, with more than 10 employees, covering the period from 1977 to 1990. Originally, these data were gathered by Colombia's National Department of Statistics (DANE) and have been cleaned by Roberts (1996), as described in further details in Appendix A. Table 1 displays the summary of a few descriptive statistics for the beer industry during the sample period. The revenue series are constructed as the total sale

<sup>5</sup>It is assumed that a Bertand-Nash equilibrium in pure strategies (prices) exists.

revenue divided by a general wholesale price deflator.<sup>6</sup> The total variable costs are defined as the sum of payments to labor, intermediate input purchases and energy purchases. Since some of the cost is incurred in the export activity, one has to scale it by the ratio of total domestic sales to total sales and deflate the result by the same wholesale price deflator mentioned before.

Labor costs only include payments to production workers. Intermediate input purchases include items such as accessories and replacement parts of less than one year of duration, fuels and lubricants consumed by the plant and raw materials. The remaining cost item is the energy consumed by the plant.

Table 1  
Summary statistics for the Colombian beer industry (1977-1990)

	Mean	SD	Min	Max
Sales revenue	445.44	471.03	6.39	2694.66
Total variable cost	184.47	195.74	4.64	1328.52
No. of employees	215.214	180.885	34	812
No. of active plants per year	21.35	1.88	20	23
Total no. of plants during the sample period	27			
No. of observations	299			

Note: Sales and costs are in million of 1975 Colombian pesos.

There are a total of 27 plants in the sample. But not all of them were active during the sampled years. The number of active plants per year did not vary so much, averaging 21.35 with a standard error of only 1.88. The same cannot be claimed regarding sales revenue, total cost and the number of employees whose variance/mean ratios are much larger.

From an additional source (UN common database) I obtained the quantity of beer (in hectoliters) produced in the country during the same sample period. Ideally, one would want to have data on the quantity of beer consumed in the country. However, the data in hand are not so restrictive since there is very little export activity in this sector.

I also use auxiliary data to uncover the price of the imported good ( $p_{0t}$ )<sup>7</sup> as well as its imported quantity in hectoliters ( $q_{0t}$ ). In a separate publication DANE also reports the net weight (in kilos) and the monetary value of imports (in pesos). Assuming that beer has the same density as water (1kg per liter), it is easy to convert the net weight in kilos to volume of imported beer in hectoliters ( $q_{0t}$ ). Then,  $p_{0t}$  follows from the ratio of the peso value of imports to  $q_{0t}$ .

<sup>6</sup>I used the wholesale price deflator because I only observe revenue series, which by definition, are based on prices before the incidence of taxes, freight and retail costs. If I could also observe retailers' revenue, a consumer price deflator would be more appropriate.

<sup>7</sup>This is a composite good that bundles together all the different imported varieties.

#### 4. Model

In this section I shall lay out the model used in this investigation. For expositional purposes I assume first that market-level data on prices and quantities are available. Then, I shall demonstrate how to estimate the model with limited data (only revenue and cost data) according to the methodology developed by KLT.

Assume now that products are divided into groups,  $g = 0, 1$ . The first group contains only the outside good (imported variety)<sup>8</sup> while the second collects all the inside goods (domestic varieties). For product  $j$  belonging to group  $g$  define utility<sup>9</sup> as

$$u_{ij} = \xi_j - \alpha p_j + \varsigma_{ig} + (1 - \sigma)\epsilon_{ij} \text{ for } j = 0, 1, \dots, N$$

The first random term on the RHS ( $\varsigma_{ig}$ ) is a common shock to all products in group  $g$  and its distribution depends on the parameter  $\sigma$  ( $0 \leq \sigma < 1$ ). As  $\sigma$  approaches zero the within correlation of utilities within each group decreases. The second random term  $\epsilon_{ij}$  is identically and independently distributed extreme value. Given these assumptions, McFadden (1981) shows that, if product  $j$  belongs to the group that contains the inside goods ( $g = 1$ ), the market share of product  $j$  as a fraction of the total group share is

$$sw_j = \frac{\exp[(\delta_j - \delta_0)/(1 - \sigma)]}{\sum_{k=1}^N \exp[(\delta_k - \delta_0)/(1 - \sigma)]}, j = 1, 2, \dots, N \quad (7)$$

Here,  $\delta_j = -\alpha p_j + \xi_j$ . The share of all domestic brands is given by  $s_d = D/(D + 1)$ , where  $D = [\sum_{k=1}^N \exp(\delta_k - \delta_0)/(1 - \sigma)]^{1-\sigma}$ .

Thus the market share for a domestic variety  $s_j$  is given by

$$s_j = \left( \frac{\exp[(\delta_j - \delta_0)/(1 - \sigma)]}{\sum_{k=1}^N \exp[(\delta_k - \delta_0)/(1 - \sigma)]} \right) \left[ \frac{D}{D + 1} \right]; j = 1, 2, \dots, N$$

<sup>8</sup>Usually the outside good is defined as a composite good that bundles together all goods other than beer. Not allowing for the consumption of other goods yields an undesirable result. If the price of all brands of beer goes up, including the imported variety, their market shares remain unchanged, as consumers cannot substitute other goods (e.g. wine) for beer. Dealing with this problem is not a simple task, though. To do so, one would have to define the potential market size. In the BLP application this number is defined as the number of families in the U.S., based on the reasonable assumption that each family buys at most one car per year. Nevo (2000) assumes that a person consumes at most one serving of ready-to-eat cereal per day to come up with a number for the potential market size. However, defining the total market for beer is not obvious since it is difficult to establish the potential consumption of beer (or alcohol) per capita.

<sup>9</sup>Plant-level data sets rarely report product characteristics. For this reason, as in KLT, they are excluded from the model.

which is simply the product of  $sw_j$  times  $s_d$ . Further, taking the log-difference between  $s_j$  and  $s_0$  the demand equation takes the simple linear relation

$$\ln s_j - \ln s_0 = -\alpha.(p_j - p_0) + \sigma \ln sw_j + \xi_j - \xi_0 \quad (8)$$

If prices and quantities were available, the model above could be estimated using the methodologies described in Section 2. Indeed, notice that, under some rearrangements, (8) is a closed form version of (4) that can be solved, conditional on the model parameters, for the unobservable term  $\xi_j - \xi_0$ . Also, the marginal cost unobservable can be uncovered from (6). Then, these unobservables can be combined with appropriate instruments to estimate the parameters through GMM.

Obviously, this strategy is unfeasible in the absence of market-level data (prices and quantities). However, KLT show that commonly available information on revenue and total costs along with some assumptions on the technology can be used to uncover relevant variables and estimate the model.

Note that firm  $j$ 's revenue ( $R_j$ ) and variable cost<sup>10</sup> ( $TC_j$ ) can be written as  $R_j = p_j q_j$ ,  $TC_j = mc_j q_j$ , where  $q_j$  represents firm  $j$ 's output. Thus, one can write the market share for firm  $j$  as  $s_j = q_j / (Q + Q_0)$ , where  $Q$  and  $Q_0$  represent the total output produced by domestic firms and total imported quantity, respectively. Then, it is simple to demonstrate that these two identities together with the F.O.C (6) can be solved for quantity as a function of data  $(\mathbf{R}, \mathbf{TC}, Q_0)$  and the demand parameters  $(\alpha, \sigma)$ , where  $\mathbf{R}$  collects the revenue of all plants in the sample and  $\mathbf{TC}$  collects the costs of all plants in the sample in a given year.

Similarly, from the same system of equations, one can retrieve  $mc_j = mc_j(\alpha, \sigma, \mathbf{R}, \mathbf{TC}, Q, Q_0)$ ,  $p_j = p_j(\alpha, \sigma, \mathbf{R}, \mathbf{TC}, Q, Q_0)$ . Thus, from  $\sum_N q_j(\alpha, \sigma, \mathbf{R}, \mathbf{TC}, Q, Q_0) = Q$ , one is able to solve for  $Q = Q(\alpha, \sigma, \mathbf{R}, \mathbf{TC}, Q_0)$ . Then, using prices and market shares, relative quality, defined as  $a_{jt} = \xi_{jt} - \xi_{0t}$ , can be determined from the demand system (8). To summarize, given  $(\alpha, \sigma, \mathbf{R}, \mathbf{TC}, Q_0)$ , the KLT algorithm<sup>11</sup> shows how to obtain firm level prices, marginal costs, relative quality and quantities as well as aggregate output ( $Q$ ).

Further, dynamics is introduced into the model through the assumption that relative quality and marginal cost follow an exogenous<sup>12</sup> VAR process given by

$$a_{jt} = b_{01} + \varphi a_{jt-1} + \varphi^c mc_{jt-1} + \beta t + \epsilon_{jt}^a \quad (9)$$

<sup>10</sup> $TC_j = mc_j q_j$  as long as marginal costs are flat.

<sup>11</sup>For more details, see Appendix B, which lays out a generalization of the original transformation algorithm found in KLT in order to accommodate multiplant firms.

<sup>12</sup>It is also assumed that firms observe their marginal costs and relative quality before they set prices. The exogeneity of the joint evolution of marginal costs and quality is an important assumption since it keeps the model consistent with the assumption that firms maximize static profits (5). Otherwise, if firms could influence marginal costs and quality of their products, one would have to set up a dynamic model of profit maximization following Pakes and McGuire (1994) framework.



$$mc_{jt} = b_{02} + \lambda mc_{jt-1} + \lambda^a a_{jt-1} + \phi t + \epsilon_{jt}^c \quad (10)$$

The VAR restricts the comovements of quality and costs. Since one does not observe product characteristics, this restriction is crucial for identification, as explained below.

### Estimation Strategy

From the demand system, the price setting game and the VAR, one is able to uncover demand and supply side “errors”, represented respectively by  $\epsilon_{jt}^c$  and  $\epsilon_{jt}^a$ . At this point the model seems very close to Berry’s (1994) methodology, where similar error terms are combined with exogenous product characteristics to form the identifying moment conditions. Here, however, these data are not available. Note that not even prices or quantities are observed; they are themselves functions of data and demand parameters to be estimated within the model. The model is therefore not identified such that traditional econometric techniques such as GMM and ML do not apply.

To identify it more structure has to be imposed on the parameters. This is achieved by assuming a prior knowledge of the parameter distribution and by using the data set and the structure imposed by the model to update this prior distribution according to Bayes’ rule

$$p(\theta; D) \propto L(D; \theta)p(\theta)$$

The LHS is the posterior probability distribution of the parameters  $\theta$  updated by the data  $D$ , and the RHS is the product of the likelihood function of the data times the prior distribution. However, only in special cases, the posterior distribution has a closed form from which one can make inference either by sampling from it or by consulting easily available tables. Fortunately, Monte Carlo techniques have been developed to deal with such problem. Shortly, it relies on ergodic theory to guarantee that a computable statistic converges to the true posterior distribution. Then, once convergence has been attained, one can sample from this statistic and make inference (see Appendix C for further details on the Bayesian Monte Carlo estimation process).<sup>13</sup>

This paper proposes appending the KLT methodology by bringing data on aggregate quantities to improve inference. Aggregate quantities also carry information on demand parameters and therefore may help in the estimation process, especially in small data sets. Assume now that the amount of beer consumed in a given year is observed up to a measurement error. Note that the model implies

<sup>13</sup>An alternative methodology, which basically follows from Panzar and Rosse (1987), consists in solving for prices and quantities, given demand and cost shifters up to the model parameters, to obtain a reduced-form equation for observable revenue.

an aggregate quantity given the demand parameters and data. One can then ask the model to match the observed quantity for every period  $t$  according to

$$Q_t(\alpha, \sigma, \mathbf{R}, \mathbf{TC}_t, Q_0) = Q_t^{obs} - w_t \quad (11)$$

where  $w_t$  is assumed to be a serially uncorrelated and normally distributed mean zero error term which is independent of the VAR error terms. To include this new “moment”<sup>14</sup> in the estimation it suffices to incorporate the likelihood of  $Q_{obs}^t$  in the likelihood function  $L(D_{jt}; \theta)$ . The next section presents the estimates and analyzes the effect of bringing more information into the model.

## 5. Market Idiosyncrasies and Results

While it is common for data sets to report plant-level revenue and cost data, they do not usually contain information on plant ownership. This is important for estimation since each ownership arrangement implies a different supply function and therefore, given  $(\alpha, \sigma, \mathbf{R}, \mathbf{TC}, \mathbf{Q}_0)$ , different values for the unobserved variables (price, quantities, marginal cost and qualities). In the Colombian beer sector, however, ownership identification does not pose a problem since one company (Bavaria S.A.) controls the whole non-imported beer market.

Indeed, after an aggressive horizontal merger strategy, Bavaria became a monopoly in the beer production by acquiring all of its rivals (Cerveceria Aguila, Cerveceria Union and Cerveceria Andina and other smaller producers) in the beer business by the early seventies. Its monopoly went unchallenged until 1995 when Cerveceria Leona entered the beer market as retaliation for the placeStateBavaria entry in the soft drink business, which was dominated by Leona’s parent company. Since the data sample period ranges from 1977 to 1990 all the estimations presented below assume that a single firm owns all plants.

Two different models are implemented. The first one uses the nested logit model without the aggregate quantity while the second one uses the same model, but includes the aggregate quantity. They are both estimated using Markov Chain Monte Carlo (MCMC) Bayesian techniques (for details on the estimation technique, see Appendix C). In both models, the demand parameters are significantly different from zero.

In addition, they yield high estimates for the within value  $\sigma$ , which means that the set of the inside goods (domestic goods) is highly differentiated from the outside good (imported variety). In other words, the degree of substitution between domestic varieties is higher than the degree of substitution between domestic and imported varieties.

Table 2 displays all parameter estimates. The demand parameter estimates are

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<sup>14</sup>Although this is a likelihood-based econometric model, I keep the GMM terminology due to its intuitive appeal.

sensitive to the inclusion of the aggregate moment.<sup>15</sup> There is a sizeable precision gain (higher  $t$ -values) for the demand parameters. The  $t$ -values for  $\sigma$  go from 64.0 to 94.1 once the aggregate information is brought to estimation. In turn,  $\alpha$  shows an even larger precision gain, going from 3.75 to 14.18. The same is not true for the VAR estimates, which do not show considerable changes ( $t$ -values are slightly higher). This should not come as a surprise as the new moment incorporated into the model bears more directly on the demand parameters and only obliquely on VAR parameters.

Table 2  
Parameter estimates

	With aggregate information	Without aggregate information
$\alpha$	2.738 (0.193) [14.186]	3.122 (0.828) [3.758]
$\sigma$	0.941 (0.010) [94.1]	0.960 (0.015) [64.0]
VAR quality equation (9)		
Const.	20.287 (4.495) [3.898]	19.232 (4.934)
Lagged Quality	0.026 (0.068) [0.382]	0.022 (0.069) [0.319]
Lagged Marg. cost	1.279 (0.289) [4.426]	1.292 (0.295) [4.379]
Trend	-0.204 (0.052) [3.923]	-0.191 (0.058) [3.293]
VAR cost equation (10)		
Const.	-0.542 (1.249) [0.434]	0.669 (1.265) [0.529]
Lagged Quality	-0.042 (0.018) [2.333]	-0.041 (0.018) [0.277]
Lagged Marg. Cost	0.752 (0.075) [10.026]	0.745 (0.075) [9.933]
Trend	0.005 (0.014) [0.357]	0.006 (0.014) [0.428]

\*Standard deviations are in parentheses and  $t$ -values in square brackets.

<sup>15</sup>Figures 1 and 2 show the Monte Carlo simulation for the demand parameters calculated with the aggregate moment.

## 6. Final Remarks

Using data from the Colombian beer industry from 1977 to 1990, I demonstrate how to extend the KLT framework by including the extra information provided by commonly available data on aggregate physical output. The idea behind the estimation procedure is to ask the structural model, parameterized by consumers' preferences, to reproduce observed data on aggregate physical quantities. The model is then estimated through Bayesian Markov Chain Monte Carlo Methods. The results show a precision gain in the parameter estimates once the additional information is included. This precision gain, measured by the  $t$ -values, is sizeable for the demand parameters  $\alpha$  and  $\sigma$ . In turn, the VAR parameters show little sensitivity to the inclusion of the aggregate variable. Although the closed form of the nested logit demand systems has some computational advantages, it comes at the cost of strong restrictions on own and cross-price effects (see Nevo (2000)). In this way, an interesting extension to this paper would consist in introducing consumer heterogeneity in a more sophisticated fashion along the same lines as BLP.

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## Appendix A

### Colombian Data Set

This appendix shows how Roberts (1996) constructed his data set from the survey collected by DANE.

Plant-specific identification numbers are not available on the original Colombia data set. Then, plants are matched across years by using reported values for inventories and capital stock and by comparing them in successive years. Inventories and capital stock are unlikely to change considerably in successive years. For this reason, they were selected as matching criteria.

The original data set has information on: SIC code (at the four digit level), the year in which the plant was established, the section of the country in which the plant is located (not available in 1977 – 79) and metropolitan area in which the plant is located. Values of inventories and capital stocks are broken down into their component parts as follows:

$$\begin{aligned} \text{Total inventories} &= \text{finished goods} + \text{raw materials} + \text{goods in progress} \\ \text{Total capital stock} &= \text{buildings and structures} + \text{machinery and equipment} \\ &+ \text{land} + \text{transportation equipment} + \text{office equipment} \end{aligned}$$

The matching algorithm goes as follows. First, observations are pre-matched on: SIC, year of establishment, section of the country and metropolitan area. Then, values for inventories and capital stocks are compared in the following order: finished goods inventories, raw materials, total inventories, buildings and structures, machinery and equipment, land, transportation equipment, office equipment and total capital stock.

When a candidate for a match is found following the sequence described above the matching observation is checked for quality. For instance, if a match is made on finished goods, it needs to match on at least one other continuous variable.



## Appendix B

### Uncovering Relevant Quantities from Revenue and Cost Data with Multiplant Ownership

This appendix shows how to uncover relevant plant-level quantities from revenue and cost data conditional on the parameters of the model. Equation (6) in the text can be rewritten as

$$1 + \left( \sum_{r \in F_f} (p_r - mc_r) \frac{\partial s_r}{\partial p_j} / s_j \right) = 0 \quad (\text{B.1})$$

Further, it is easy to show that the following equalities hold for the cross and own price derivatives

$$\begin{aligned} \frac{\partial s_r}{\partial p_j} / s_j &= -\frac{\alpha}{1 - \sigma} \frac{s_r}{s_j} [-(1 - \sigma)s_j - \sigma s_w] \\ \frac{\partial s_j}{\partial p_j} / s_j &= -\frac{\alpha}{1 - \sigma} [1 - (1 - \sigma)s_j - \sigma s_w] \end{aligned}$$

Note also that  $s_r/s_j = q_r/q_j$ ,  $R_j = p_j \cdot q_j$ ,  $TC_j = mc_j q_j$ , and  $s_j = q_j/(Q + Q_0)$  where  $R_j$ ,  $TC_j$ ,  $Q$  and  $Q_0$  are revenue, total variable cost, total output produced by domestic firms and total imported quantity, respectively. Hence, substituting these equations into the pricing rule (B.1) and solving for quantity of plant  $j$  belonging to firm  $f$  ( $j \in F_f$ ), one obtains

$$q_j = \left( \frac{1 - \sigma}{\alpha(R_j - TC_j)} + \left( \left( \frac{(1 - \sigma)}{Q + Q_0} + \frac{\sigma}{Q} \right) \sum_{r \in F_f} \frac{(R_r - TC_r)}{(R_j - TC_j)} \right) \right)^{-1} \quad (\text{B.2})$$

Aggregating over the  $q_j$ 's results in

$$Q = \sum_{f=1,2,\dots,NF} \sum_{j \in F_f} \left( \frac{1 - \sigma}{\alpha(R_j - TC_j)} + \left( \left( \frac{(1 - \sigma)}{Q + Q_0} + \frac{\sigma}{Q} \right) \sum_{r \in F_f} \frac{(R_r - TC_r)}{(R_j - TC_j)} \right) \right)^{-1}$$

where  $NF$  is the total number of firms. This nonlinear equation can be solved numerically for  $Q$  given  $(\alpha, \mathbf{R}, \mathbf{TC}, Q_0)$ , where  $\mathbf{R} = \{R_j; j = 1, \dots, NF\}$  and  $\mathbf{TC} = \{TC_j; j = 1, \dots, NF\}$ . Then, given the same parameters and data,  $q_j$  is determined from (A1.2), whereas  $p_j$ ,  $mc_j$  and  $s_j$  follow trivially from  $p_j = R_j/q_j$ ,  $mc_j = TC_j/q_j$  and  $s_j = q_j/(Q + Q_0)$  respectively.

Finally, the log-linearized version of the demand system (8) can be solved for relative quality  $a_j$

$$a_{jt} \equiv \xi_j - \xi_0 = \alpha(p_j - p_0) - \sigma \ln s_w + \ln s_j - \ln s_0$$

In sum, for a given set  $(\alpha, \mathbf{R}, \mathbf{TC}, Q_0, p_0)$ , this mapping shows how to obtain total quantity ( $Q$ ) and plant-level information on price, marginal cost, relative quality and quantity.

## Appendix C

### Gibbs Sampler<sup>16</sup>

Although one cannot make inference directly from  $L(D; \theta)p(\theta)$ , it is possible to sample from the full conditionals of the  $\theta$  components. In the NLB model, the parameter vector is divided into:  $\theta_1 = (\varphi, \lambda)$ ,  $\theta_2 = (\Sigma)$ ,  $\theta_3 = (\nu)$ ,  $\theta_4 = (\alpha, \sigma)$ . The parameters  $\varphi, \lambda, \alpha, \sigma$  are defined as before,  $\Sigma$  is the covariance matrix of the VAR error terms and  $\nu$  is the variance of error in the aggregate quantity equation (10). The Gibbs algorithm goes as follows.

Step 0: Draw initial values for the parameter vector

$$\theta^0 = (\theta_1^0, \theta_2^0, \theta_3^0, \theta_4^0) \text{ and set } i = 0$$

Step 1: Draw  $\theta^{i+1}$  from the conditionals below.

1.1) Draw  $\theta_1^{i+1} \sim \pi_1(\theta_1 | \theta_2^i, \theta_3^i, \theta_4^i, D)$

1.2) Draw  $\theta_2^{i+1} \sim \pi_2(\theta_2 | \theta_1^{i+1}, \theta_3^i, \theta_4^i, D)$

1.3) Draw  $\theta_3^{i+1} \sim \pi_3(\theta_3 | \theta_1^{i+1}, \theta_2^{i+1}, \theta_4^i, D)$

1.4) Draw  $\theta_4^{i+1} \sim \pi_4(\theta_4 | \theta_1^{i+1}, \theta_2^{i+1}, \theta_3^{i+1}, D)$

Step 2: Set  $i = i + 1$  and go back to step 1.

Here  $\pi_k(\theta_k | \theta_{-k}, D) = L(D; \theta) \cdot p_{\theta_k}(\theta_k)$ , where  $p_{\theta_k}(\theta_k)$  is the prior of the sub-vector  $\theta_k$ . Further, to describe the conditionals, define

$$\begin{aligned} Y_{jt} &= (a_{jt}, mc_{jt})', Z_{jt} = (1, a_{jt}, mc_{jt}, t)', U_{jt} = (\epsilon_{jt}^a, \epsilon_{jt}^c)', \text{ and } B' \\ &= \begin{pmatrix} b_{01} \varphi \varphi^c \beta \\ b_{02} \lambda \lambda^c \phi \end{pmatrix} \end{aligned}$$

In addition, let

$$\begin{aligned} Y &= [Y_{12} \dots Y_{1T} \dots Y_{N2} \dots Y'_{NT}] \\ Z &= [Z_{12} \dots Z_{1T} \dots Z_{N2} \dots Z'_{NT}] \end{aligned}$$

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<sup>16</sup>This appendix is heavily based on KLT (2003) and is included in this work for the sake of clarity.

$$U = [U_{12} \dots U_{1T} \dots U_{N2} \dots U'_{NT}]$$

The VAR system can then be written as  $Y=XB+U$ . Given  $\theta_4$ ,  $Y$  and  $Z$  are given and 1.1) to 1.3) have known probability distributions. On the other hand,  $\pi_4(\theta_4 | \theta_1, \theta_2, \theta_3, D)$  does not have a closed form solution, which requires the use of a Metropolis-Hastings (M-H) algorithm.

More specifically, defining  $K$  as one plus the number of variables appearing on the RHS of the VAR and assuming that the prior of  $\theta_1$  is  $N(0_{2k}, 100 \times I_{2k})$ , one can show that  $\pi_1(\theta_1 | \theta_2, \theta_3, \theta_4, D)$  is also a normal with mean  $u_n = [(Z' \otimes \Sigma)Vec(Y')]$  and variance  $V_n = [((Z'Z) \otimes \Sigma^{-1}) + (1/100)I_{2k}]^{-1}$ .

For 1.2 it is assumed that  $\Sigma$  has Inverse Wishart prior with parameters 6 and  $100xI_2$ . Then  $\pi_2(\theta_2 | \theta_1, \theta_3, \theta_4, D)$  has a distribution  $InvWish(m_n, G_n^{-1})$ , where  $m_n = 6 +$  number of observations,<sup>17</sup> and

$$G_n^{-1} = (100 \times I_2) + (Y - ZB)'(Y - ZB)$$

Similarly,  $\nu$  has the prior distribution defined as the scalar version of the inverse Wishart ( $InvWish(6, 100)$ ). Hence, the conditional  $\pi_3(\theta_3 | \theta_1, \theta_2, \theta_4, D)$  is also an  $InvWish(m_n, G_n^{-1})$ ,  $m_n = 6 + (np - 1)$ , and  $G_n^{-1} = 100 + w'w$ , where  $w$  is a vector that collects all the  $w_t$ 's.

The prior for  $\alpha$  is uniform with support  $[0, 10]$ , while  $\sigma$  has the same prior, but its support is a little narrower  $[0, 1]$ . Since one cannot identify the shape of  $\pi_4(\theta_4 | \theta_1, \theta_2, \theta_3, D)$ ,  $\theta_4$  has to be sampled using a random walk Metropolis-Hastings acceptance criterion with a normal proposal density. The probability of acceptance of  $\theta'_4$  is  $\min \left\{ 1, \frac{\pi_4(\theta'_4 | \theta_1^{i+1}, \theta_2^{i+1}, \theta_3^{i+1}, D)}{\pi_4(\theta_4^i | \theta_1^{i+1}, \theta_2^{i+1}, \theta_3^{i+1}, D)} \right\}$ , where  $\theta'_4$  is drawn from a normal density with mean  $\theta_4^i$  and variance  $\Lambda$ . In principle, any  $\Lambda$  can be used in the algorithm, however, for a well behaved convergence to the invariant probability distribution, it is recommended to calibrate this variance such that it is not too "big" (all the proposed  $\theta'_4$  will be accepted, but the chain will move slowly) nor too "small" (nearly all proposed moves will be rejected and the chain may not move for several iterations).

Once convergence of the Markov chain has been attained (suppose at the  $L^{th}$  simulation), it suffices to sample from the invariant distribution using the draws  $\theta^i$ , where  $i > L$ . To obtain the statistics reported in Table 1, I run 20,000 iterations of the Markov chain and set  $L$  to be 2,000. Figures 1 and 2 show the graphs of the MCMC simulations for the demand parameters for the nested logit model with the aggregate quantity. Clearly, after 2,000 iterations the Markov chain moves within a certain range and inference can be made from then on.

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<sup>17</sup>Adjusted for the lags.

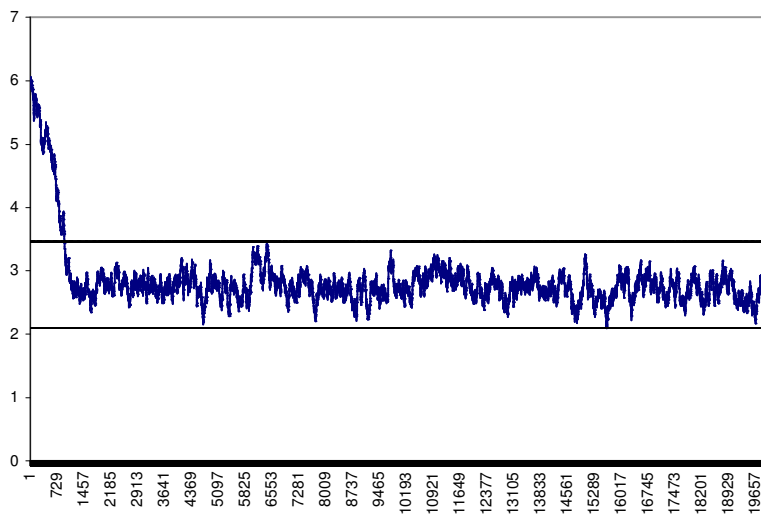


Figure 1  
MCMC simulation for  $\alpha$

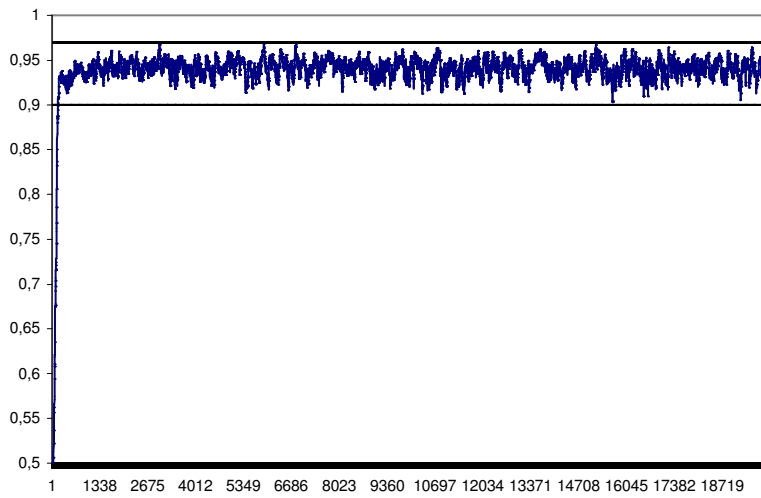


Figure 2  
MCMC simulation for  $\sigma$