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ADDRESSING 5G ENHANCED MOBILE BROADBAND AND LEAN SIGNALING BASED ON DUAL-CONNECTIVITY AND CHANNEL HARDENING OCCURRENCE

FORTALEZA 2018

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Tese apresentada ao Curso de Doutorado em Engenharia de Teleinformática da Universidade Federal do Ceará, como parte dos requisitos para obtenção do Título de Doutor em Engenharia de Teleinformática. Área de concentração: Sinais e Sistemas

Orientador: Prof. Dr. Francisco Rodrigo Porto Cavalcanti

Coorientador: Dr. Igor Moaco Guerreiro

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RESUMO

Sistemas 5G serão baseados na implantação de largos conjuntos de antenas operando no espectro de ondas milimétricas para suportar o aumento significativo no tráfego de dados. Com mais antenas e maior largura de banda, a estimação da qualidade do canal e o envio dessas medidas do usuário para a estação rádio base serão processos computacionalmente mais complexos que os atuais e envolverão maior sinalização. Neste contexto, a presente tese analisa duas estratégias para tratar ambos os problemas: aumento de tráfego de dados e de sinalização. A primeira estratégia consiste em explorar a redução das flutuações do canal devido ao uso de feixes estreitos com largos conjuntos de antenas (o canal "endurece"). Quando este fenômeno ocorre, funções de camadas superiores baseadas em medições podem ser otimizadas. A segunda estratégia é relacionada à integração entre sistemas 5G e LTE. Mais precisamente, os usuários têm a capacidade de se conectarem simultaneamente a sistemas de ambas as tecnologias. Isto é chamado conexão dual. Antes de abordar essas duas estratégias, apresentamos uma visão geral das principais características do 5G usadas nessa tese e padronizadas pelas especificações do 3GPP versão 15. Depois disso, apresentamos análises gerais relacionadas à conexão dual e ao endurecimento do canal. Finalmente, investigamos esses dois conceitos da perspectiva da alocação de recursos de rádio. Mais especificamente, propomos soluções baseadas no endurecimento do canal e relacionadas à medição da qualidade do canal e ao envio destes dados. Além disso, também apresentamos soluções para seleção de estação rádio base e alocação de recursos em sistemas com múltiplas tecnologias e múltiplas conexões. Análises numéricas considerando parâmetros 5G são apresentadas para validar os métodos propostos.

Palavras-chave: conexão dual, endurecimento do canal, medição e envio da qualidade do canal, alocação de recursos.

ABSTRACT

[Fifth Generation \(5G\)](#page-10-0) systems are expected to deploy massive [Multiple Input Multiple Output](#page-10-1) [\(MIMO\)](#page-10-1) antennas and operate with millimeter waves in order to support a significantly increasing data traffic. With more antennas and wider bandwidth, [Channel Quality Indicator \(CQI\)](#page-10-2) estimation and reporting will be computationally demanding, increasing signaling between [Base](#page-10-3) [Stations \(BSs\)](#page-10-3) and [User Equipments \(UEs\).](#page-12-0) In this context, the present thesis analyzes two strategies to address both problems: increasing data traffic and signaling. The first strategy is to exploit the reduction of channel fluctuations due to the use of narrow beams with large antenna arrays, i.e., the channel "hardens". When this phenomenon happens, upper layer functions related to measurements can be optimized and signaling reduced. The second strategy concerns the adoption of a tight integration between 5G NR and LTE. More precisely, the [UEs](#page-12-0) would be allowed to be simultaneously connected to both [Radio Access Technologies \(RATs\),](#page-11-0) the so-called [Dual](#page-10-4) [Connectivity \(DC\).](#page-10-4) Before addressing these two strategies, we present an overview of the main 5G features used in this thesis and standardized in [3rd Generation Partnership Project \(3GPP\)](#page-10-5) specification release 15. After that, we present general analyses related to [DC](#page-10-4) and [Channel](#page-10-6) [Hardening \(CH\)](#page-10-6) occurrence. Finally, we investigate these concepts from the perspective of [Radio](#page-11-1) [Resource Allocation \(RRA\).](#page-11-1) More specifically, frameworks related to [CQI](#page-10-2) measurement and reporting based on [CH](#page-10-6) occurrence are proposed. Besides, we also propose procedures for base station selection and resource assignment in a multi[-RAT](#page-11-0) multi-connectivity system. Numerical analyses considering 5G system parameters are presented validating the proposed methods and showing that they improve system performance.

Keywords: dual connectivity, channel hardening, CQI measurement and reporting, radio resource allocation.

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SUMMARY

1 INTRODUCTION

In the last few years, academia and industry were together in international consortia, e.g. the [Mobile and Wireless Communications Enablers for the Twenty-twenty Information](#page-10-15) Society 5G [\(METIS\)](#page-10-15) project, discussing scenarios and requirements related to the next generation of wireless cellular networks, the [Fifth Generation \(5G\).](#page-10-0) Based on the agreements of these discussions, the [International Telecommunication Union \(ITU\)](#page-10-16) categorized the envisioned use cases into 3 groups [\[1\]](#page-90-0):

- [Enhanced Mobile Broadband \(eMBB\)](#page-10-17) This is an evolution of today's humancentric cases for access to multimedia content, but with significantly increased data traffic and transmission rates;
- [Ultra-Reliable and Low-Latency Communications \(URLLC\)](#page-12-1) This category includes services with strict requirements of latency, reliability and availability, such as self-driving cars and remote medical surgery;
- [Massive Machine-Type Communications \(mMTC\)](#page-11-9) This scenario addresses a very large number of connected devices, each transmitting a low volume of data and with constraints on their prices and battery life. Sensors and actuators in a smart city are examples of these devices.

For each of these use cases, [ITU](#page-10-16) set the key requirements that must be achieved in [5G](#page-10-0) networks. They are listed in [\[2\]](#page-90-1). For example: the network must provide for [eMBB](#page-10-17) [User](#page-12-0) [Equipments \(UEs\)](#page-12-0) a downlink data rate of at least 100 Mbps when accessing multimedia content in dense urban areas; [URLLC](#page-12-1) [UEs](#page-12-0) must experience a maximum latency of 1 ms; and [mMTC](#page-11-9) scenarios must support a minimum of one million connected devices per square kilometer.

Aiming at supporting this wide range of services, the [3rd Generation Partnership](#page-10-5) [Project \(3GPP\)](#page-10-5) has already released the first sets of [5G](#page-10-0) standards, known as [3GPP](#page-10-5) specification 38 series release 15 [\[3\]](#page-90-2). They were delivered in December 2017 and June 2018 [\[4\]](#page-90-3), and they are called as non-standalone and standalone [5G](#page-10-0) radio specifications, respectively. On one hand, in the non-standalone, the control plane connection to the core network is done through [Long Term](#page-10-11) [Evolution \(LTE\),](#page-10-11) while data capacity is boosted through [5G](#page-10-0) [New Radio \(NR\).](#page-11-2) On the other hand, in the standalone, [5G](#page-10-0) [NR](#page-11-2) has full control plane support and does not need to rely on [LTE](#page-10-11) for control plane communications.

To achieve the performance requirements set by [ITU](#page-10-16) in [\[2\]](#page-90-1), the [5G](#page-10-0) specifications not only improve features already present in [LTE,](#page-10-11) but also consider new ones. Some of the key [NR](#page-11-2) features are [\[5,](#page-90-4) [6\]](#page-90-5): adoption of a flexible and scalable physical layer numerology, support to low and high frequency bands, deployment of massive [Multiple Input Multiple](#page-10-1) [Output \(MIMO\)](#page-10-1) antenna arrays and multi-beam operation. Regarding the scalable numerology, a frequency dependent frame structure will enable service-specific adaptations, improving energy and spectral efficiency. Concerning the wide spectrum, low frequency bands, e.g., below 6 GHz, will be useful for [mMTC](#page-11-9) cases where coverage is important, while high frequency bands, e.g., 60 GHz, will be useful for [eMBB](#page-10-17) cases where higher throughput can be achieved.

In [Millimeter Wave \(mmWave\)](#page-11-10) frequencies, there is still a huge amount of underutilized spectrum resources [\[7\]](#page-90-6). However, in this part of the spectrum, the propagation conditions are challenging [\[7\]](#page-90-6): lower diffraction, higher path loss, and so on. This means that signals have less ability to propagate around corners and penetrate walls. In addition, atmospheric/rain attenuation and higher blockage attenuation could also contribute to making the coverage of the new [5G](#page-10-0) air interface spotty.

In order to overcome these issues, beamforming with the use of large antenna arrays is one of the considered solutions [\[8\]](#page-90-7). Beamforming is an array signal processing technique where multiple antenna elements are adaptively phased to form a concentrated and directed beam pattern. The narrower the beam, the higher the directivity gain is, which helps mitigate propagation losses. In order to deploy narrow beams, one needs large antenna arrays, which is not a problem in [mmWaves,](#page-11-10) since their small wavelengths enable placing a large number of antenna elements into a small area.

At least two major problems arise with this solution. The system's reliability might decrease [\[9\]](#page-90-8) while its complexity might increase [\[10\]](#page-90-9).

Concerning the system's reliability, although beamforming overcomes the problem of high propagation losses in [mmWave](#page-11-10) frequencies, a [UE](#page-12-0) can be out-of-coverage if it is not well aligned with a beam. Thus, there will be a tight interworking between the [5G](#page-10-0) [Radio Access](#page-11-0) [Technology \(RAT\),](#page-11-0) called [NR,](#page-11-2) and legacy standards, such as [LTE.](#page-10-11) [3GPP](#page-10-5) has even standardized a [Dual Connectivity \(DC\),](#page-10-4) where [UEs](#page-12-0) are simultaneously served by [LTE](#page-10-11) and [NR.](#page-11-2) This tight interworking is expected to enable an early deployment of [5G](#page-10-0) [NR,](#page-11-2) besides improving the throughput and ensuring connectivity when [5G](#page-10-0) [NR](#page-11-2) link fails. In this thesis, we exploit solutions related to [DC](#page-10-4) in order to improve [Quality of Service \(QoS\)](#page-11-11) metrics of the system.

Regarding the system's complexity, the amount of [UE](#page-12-0) measurements and reports will drastically increase [\[10\]](#page-90-9). This is due to the fact that [5G](#page-10-0) [BS](#page-10-3) deployed in [mmWaves](#page-11-10) are expected to support dozens of beams and [5G](#page-10-0) measurement model is based on beam measurements [\[11\]](#page-90-10), instead of cell measurements as in [LTE](#page-10-11) [\[12\]](#page-91-0). Besides, upper layer functions as [Radio Resource](#page-11-1) [Allocation \(RRA\)](#page-11-1) and [UE](#page-12-0) mobility management rely on accurate channel quality estimation, thus the complexity of these functions will also increase. In order to overcome this issue, we investigate solutions that take advantage of the [Channel Hardening \(CH\)](#page-10-6) effect [\[13\]](#page-91-1). As it will be explained in more details later, narrow beams may spatially filter out angular-separated taps of the channel response. This reduces the effective channel delay spread, and, as a consequence, channel variations due to fast fading also decrease (the channel "hardens"). If the channel fluctuations might decrease, one can take advantage of it and optimize functions based on measurements.

Next section presents the state-of-the-art of both concepts: [DC](#page-10-4) and [CH.](#page-10-6)

1.1 State-of-the-Art

1.1.1 Dual-Connectivity

From the earliest days of wireless communications, networks based on different [RATs](#page-11-0) have co-existed, each of them with its own characteristics. According to their coverage range, the networks are usually classified as: [Wireless Personal Area Networks \(WPAN\),](#page-12-2) [Wireless](#page-12-3) [Local Area Network \(WLAN\),](#page-12-3) [Wireless Metropolitan Area Networks \(WMAN\)](#page-12-4) and [Wireless](#page-12-5) [Wide Area Networks \(WWAN\).](#page-12-5) Examples of these networks are: Bluetooth, [Wireless Fidelity](#page-12-6) [\(Wi-Fi\),](#page-12-6) [Worldwide Interoperability for Microwave Access \(WiMAX\)](#page-12-7) and [LTE,](#page-10-11) respectively. Despite their different coverage ranges, they are usually deployed in overlapping areas, hence forming a [Heterogeneous Network \(HetNet\).](#page-10-14)

Currently, an unprecedented escalation of network densification and heterogeneity is taking placing due to the growing consumer demand for higher throughput. Besides, [UEs,](#page-12-0) e.g., smartphones, are being equipped with multiple [RAT](#page-11-0) interfaces, e.g., [Wi-Fi](#page-12-6) and [LTE](#page-10-11) interfaces, in order to be able to access the most suitable network in a giving instant of time. In [\[14\]](#page-91-2), the author highlights seven aspects that should be taken into account in this process:

- traditional methods of *interference management* like frequency reuse or [Base Station](#page-10-3) [\(BS\)](#page-10-3) coordination may not be adequate for [HetNets;](#page-10-14)
- different networks might have different *backhaul constraints* and they should be taken into account;
- one must consider *metrics* that are valid for all the networks being compared;
- since the distance to desired and interfering [BSs](#page-10-3) is important in determining performance, a reasonable *topology model* is required;
- [HetNets](#page-10-14) might introduce asymmetries between *uplink and downlink*, so they should be considered as two different systems;
- another topic of high importance is related to *network selection* policies as the system load fluctuates:
- moreover, it is interesting to support *mobility* between the different networks, mainly focused on how and when the users are handed off.

Regarding the aspect of [RAT](#page-11-0) selection, [\[15\]](#page-91-3) presents an overview of the most important mathematical theories for modeling the network selection in [HetNets.](#page-10-14) Some of these theories are: combinatorial optimization, utility theory, Fuzzy logic, game theory and Markov chain.

An example of inter[-RAT](#page-11-0) handover decision mechanism can be found in [\[16\]](#page-91-4). It considers the co-existence of [Wi-Fi](#page-12-6) [Access Points \(APs\),](#page-10-18) representing small cells, and [LTE](#page-10-11)

[BSs,](#page-10-3) representing macro cells. In order to avoid the ping-pong effect, the authors prioritize [UEs](#page-12-0) with high mobility to be connected to a [LTE](#page-10-11) [BS,](#page-10-3) which has a broader coverage, while [UEs](#page-12-0) with low mobility tend to be connected to a [Wi-Fi](#page-12-6) [AP.](#page-10-18) The main reason for this is that [UEs](#page-12-0) with low mobility are expected to keep a more stable connection to a [Wi-Fi](#page-12-6) [AP](#page-10-18) than a [UE](#page-12-0) with high mobility.

Unfortunately, in the method presented in [\[16\]](#page-91-4), moving [UEs](#page-12-0) do not benefit from the advantages of both [RATs.](#page-11-0) In order to address this problem, [3GPP](#page-10-5) specification 36 series release 12 [\[17\]](#page-91-5) standardized the concept of [DC](#page-10-4) for [LTE.](#page-10-11) This mechanism allows the [UEs](#page-12-0) to consume radio resources provided by two different network points at the same time. For this, it was proposed the split of user and control planes, where the control plane manages system information and the user plane transmits user data.

Many works have already investigated the concept of [DC](#page-10-4) proposed in [\[17\]](#page-91-5). Usually, a centralized entity, called *cloud*, is considered in order to centralize system information and take better decisions regarding resource management [\[18\]](#page-91-6). For example, [\[19\]](#page-91-7) considered a [Time](#page-11-12) [Division Duplex \(TDD\)](#page-11-12) based system and proposed a framework based on the channel quality of uplink rather than downlink signal quality, as in traditional [LTE](#page-10-11) systems. The use of uplink signals eliminates the need for the [UE](#page-12-0) to send measurement reports back to the network and thereby removes a point of failure in the control signaling path. The framework proposed in [\[19\]](#page-91-7) is split into 3 stages. In the first one, the [UEs](#page-12-0) broadcast uplink reference signals, which are measured by the [BSs.](#page-10-3) After that, these measurements are sent to a centralized controller, which will finally make handover and scheduling decisions based on these measurements.

Centralized processing has practical issues related to backhaul constraints, e.g., limited capacity and delay on the interfaces, which can reduce the spectrum efficiency gain achieved by the cloud [\[20\]](#page-91-8). Besides, a centralized solution is computationally intensive and also incurs in signaling overhead due to the need of global information.

One possible solution for overcoming the centralized processing drawbacks is presented in [\[21\]](#page-91-9). The authors studied the problem of traffic offloading via dual connectivity in the uplink. Since data flows from the [UEs](#page-12-0) to the [BSs,](#page-10-3) each [UE](#page-12-0) independently selects its percentage of data to transmit to each [BS.](#page-10-3)

As one can see, different approaches can be adopted when implementing [DC.](#page-10-4) Thus, [3GPP](#page-10-5) specification release 15 standardized in [\[22\]](#page-91-10) the options that will be accepted for [DC](#page-10-4) between [5G](#page-10-0) [NR](#page-11-2) and [LTE.](#page-10-11) The technical details will be presented in Chapter [2.](#page-30-1)

Before being standardized, [DC](#page-10-4) between [5G](#page-10-0) [NR](#page-11-2) and [LTE](#page-10-11) was discussed by academia and industry in international consortia, e.g., the [METIS](#page-10-15) project. Report [\[23\]](#page-92-0) was one of the first works to propose a tight interwork between [5G](#page-10-0) air interface and legacy standards such as [LTE.](#page-10-11) Until then, the majority of works covering heterogeneous systems either considered [Wi-Fi](#page-12-6) associated with [LTE,](#page-10-11) as in [\[16\]](#page-91-4), or considered only [LTE](#page-10-11) [BSs](#page-10-3) with different coverage ranges, as in [\[24\]](#page-92-1).

The authors of [\[25\]](#page-92-2) performed initial analyses related to mobility robustness and

reliability in a dense urban scenario using [DC](#page-10-4) between [LTE](#page-10-11) macro [BSs](#page-10-3) and [5G](#page-10-0) small [BSs.](#page-10-3) They concluded that the reliability is still below the target expected for [5G.](#page-10-0) To achieve the desired target, other features should also be considered as make-before-break, packet duplication and handover prediction.

A make-before-break scheme based on [DC](#page-10-4) is proposed in [\[26\]](#page-92-3). The main objective is to get 0 ms interruption during a handover procedure. In this approach, [DC](#page-10-4) allows a target [BS](#page-10-3) to be added as a secondary [BS](#page-10-3) while the [UE](#page-12-0) is still connected to the serving one. Thus, the [UE](#page-12-0) will keep its connection with the source [BS](#page-10-3) until it is able to receive packets from the target [BS.](#page-10-3) At this time, target and source [BSs](#page-10-3) can switch the roles of primary and secondary, and, finally, the old [BS](#page-10-3) can be released.

In the previous strategy, it is quite challenging to know the right timing when a [UE](#page-12-0) should stop receiving from the source [BS](#page-10-3) and start receiving from target one without interruption or loss of packets. Thus, packet duplication on both links could be used in [URLLC,](#page-12-1) as done in [\[27\]](#page-92-4). The authors of [\[27\]](#page-92-4) adopted this strategy to improve the connection robustness for [Vehicle-to-Everything \(V2X\)](#page-12-8) use cases while ensuring that packets are reliably transmitted with low interruption time. They admit that this approach increases resource usage. Thus, to achieve a balanced trade-off between reliability and resource usage they suggest to dynamically control the activation of packet duplication to certain scenarios when channel conditions are typically unfavorable.

Regarding handover prediction, an example can be found in [\[28\]](#page-92-5). The authors propose a scheme operated at the [UE](#page-12-0) that predicts the expected handover time in addition to the target [BS.](#page-10-3) The [UE](#page-12-0) speed and direction are utilized to narrow down the candidate [BSs](#page-10-3) and minimize processing. [DC](#page-10-4) is used together with this scheme to allow the [UEs](#page-12-0) to perform advanced handover signaling via a second link.

A final remark concerning [DC](#page-10-4) is that it is not always better than a single connection. One can think that a [UE](#page-12-0) will always benefit from a larger transmission bandwidth. However, from the network's perspective, when the load is high and the [UEs](#page-12-0) are trying to connect to more than one [BS](#page-10-3) at the same time, the network becomes interference-limited and the system's performance decreases very fast. In this case, a single connection might be preferable. This conclusion is analytically demonstrated in [\[29\]](#page-92-6).

1.1.2 Channel Hardening

The idea that the channel fluctuations might decrease due to the deployment of large antenna arrays and the use of narrow beams is not new. In 1966, W. C. Y. Lee confirmed this experimentally and reported his results in [\[30\]](#page-92-7). He noticed that the number of times the fading signal crossed an arbitrarily chosen level below the average signal strength increased significantly with the beamwidth. Furthermore, in 1968, R. H. Clarke concluded in [\[31\]](#page-92-8) that narrow beams reduces not only the rate of fading but also the fading depth.

Although this is not a new concept, the term [CH](#page-10-6) is quite new. One of the first works

to use it was [\[32\]](#page-92-9). The authors analyzed this effect from the perspective of information theory. They considered a [MIMO](#page-10-1) channel matrix with independent zero-mean complex-Gaussian entries to demonstrate that, as the number of antennas increases, the variance of channel mutual information decreases rapidly relative to its mean. Hence, the distribution of the mutual information approaches a Gaussian [\[32\]](#page-92-9). In other words, the channel fluctuations relative to its mean decreases (the channel "hardens") and the channel gains become nearly deterministic. This definition can be formulated as [\[33\]](#page-92-10):

$$
\frac{\|\mathbf{h}_k\|^2}{\mathrm{E}\left\{\|\mathbf{h}_k\|^2\right\}} \to 1, \text{ as } M \to \infty, \ k = 1, \dots, K,
$$
\n(1.1)

where \mathbf{h}_k is the $M \times 1$ channel vector between [UE](#page-12-0) k and a [BS](#page-10-3) with M antennas, $\|\cdot\|$ is the Euclidian norm and $E\{\cdot\}$ is the expectation operator.

In the following, a simple example is presented to illustrate this concept. The left hand side of Fig. [1.1](#page-22-0) presents a transmitter with M antennas, while the right hand side presents the evolution in time of the h_i links. Suppose that all the h_i links are independent and that the probability of one of them is facing a deep fading is P , then the probability of all of them is fluctuating is P^M . Thus, when the number of antennas grows (i.e., $M \to \infty$), this probability becomes too small. The red dashed line in the right hand side of Fig. [1.1](#page-22-0) presents the envelope link. Notice that in this example there is always at least one link in good conditions, so the envelope fluctuates much less than the links themselves.

Figure 1.1 – [CH](#page-10-6) due to the deployment of large antenna array.

Source: Created by the author.

[CH](#page-10-6) depends on the characteristics of the channel. Some works, as [\[33\]](#page-92-10) and [\[34\]](#page-93-0), assume the uncorrelated Rayleigh channel model to demonstrate that [\(1.1\)](#page-22-1) can be achieved. For this model, the channel becomes flat in both time and frequency domains when $M \to \infty$. This is due to the law of large numbers. Many random channel realizations are combined, which reduces the total channel variation. However, this assumption may not be verified in real [5G](#page-10-0) systems. Firstly, the number of antennas cannot tend to infinity. Secondly, spatially correlated fading has been observed in practical measurements [\[35\]](#page-93-1).

Figure 1.2 – [CH](#page-10-6) due to the use of narrow beams.

Source: Created by the author.

The authors of [\[36\]](#page-93-2) analyzed how close to the asymptotic [CH](#page-10-6) one can be with a practical number of antennas. They concluded that, under uncorrelated fading, $M = 100$ is typically sufficient to benefit from almost perfect [CH.](#page-10-6) They also concluded that under spatially correlated fading, it is still possible to achieve [CH,](#page-10-6) however the number of required antennas increases compared to the previous case. Moreover, they demonstrated that in the extreme case when the spatial correlation matrix has rank one, [CH](#page-10-6) does not occur. Complementary to this work, the authors of [\[37\]](#page-93-3) also analyzed the [CH](#page-10-6) in a scenario not limited to classically assumed Rayleigh fading. They used a physically motivated ray-based channel model to derive an expression of [CH](#page-10-6) measure.

From another perspective, one can also obtain the [CH](#page-10-6) as a consequence of the use of narrow beams, allowed by the deployment of large antenna arrays. As illustrated in Fig. [1.2,](#page-23-0) transmitter and receiver are surrounded by objects which reflect and scatter the transmitter energy, causing several waves to arrive at the receiver via different routes [\[38\]](#page-93-4). These multipath components usually have different phase and amplitude leading to frequency selective fading and time dispersion [\[39\]](#page-93-5). In the frequency domain, the coherence bandwidth of a channel is a metric used to measure the range of frequencies over which all spectral components have approximately equal gain and linear phase, i.e., the range of frequencies over which the channel can be considered "flat". In the time domain, the RMS delay spread is used as an indicator of dispersion. It takes into account the relative power of the different taps as well as their delays. Important to highlight that the coherence bandwidth and the RMS delay spread are inversely proportional. When deploying narrow beams, as in Fig. [1.2b,](#page-23-0) they might act as a spatial filter (with narrow spatial bandwidth) on different delay taps of the channel response. Since part of the scatters are no longer illuminated, the channel delay spread might be reduced and the overall channel response might look flat. In general, the narrower the beam the flatter the channel response is. This effect was predicted in [\[40\]](#page-93-6).

Based on measurement campaigns, the authors of [\[41\]](#page-93-7) used massive [MIMO](#page-10-1) antennas with beamforming and verified the existence of [CH](#page-10-6) in a real environment. The results were compared with an [Independent and Identically Distributed \(IID\)](#page-10-19) Gaussian random channel with the same average power. Even if the measured hardening was not as strong as in the Gaussian

Figure 1.3 – [CH](#page-10-6) in an indoor environment. (a) Scenario. (b) Result.

Source: [\[43\]](#page-93-8).

channel, it was observed.

Works [\[42,](#page-93-9) [43,](#page-93-8) [44\]](#page-93-10) also identified the existence of [CH](#page-10-6) in real environments based on measurements. On one hand [\[42,](#page-93-9) [43\]](#page-93-8) conducted measurements in indoor environments, more specifically, a subway station and an auditorium, respectively. On the other hand, [\[44\]](#page-93-10) considered moving [UEs](#page-12-0) in an outdoor environment.

Regarding [\[43\]](#page-93-8), the authors considered an indoor crowded auditorium at Lund University with one [BS](#page-10-3) and nine closely-spaced [UEs](#page-12-0) placed as depicted in Fig. [1.3a.](#page-24-0) [Line of](#page-10-20) [Sight \(LOS\)](#page-10-20) propagation conditions predominated, with occasional blocking due to other [UEs](#page-12-0) or room furniture. The [BS](#page-10-3) acted as a receive unit and it was equipped with 64 dual-polarized patch antennas, i.e., 128 antenna elements. [UEs](#page-12-0) and [BS](#page-10-3) were communicating at center frequency of 2.60 GHz and bandwidth of 40 MHz, resulting in 129 measured points in frequency and 300 snapshots taken over 17 s. Fig. [1.3b](#page-24-0) presents the normalized channel gains of [UE](#page-12-0) 1 when using one antenna (green lower layer) versus the case of combining the channel of all 128 antenna elements (yellow upper layer). Notice that the channel of just one antenna element presents many severe dips and varies much more than the case with 128 antenna elements. In other words, the channel hardened when considering more antenna elements.

Concerning [\[44\]](#page-93-10), the authors considered the uplink communication between single antenna [UEs](#page-12-0) and a [BS](#page-10-3) with 100 antenna elements deployed at 3.70 GHz and bandwidth of 20 MHz. Fig. [1.4a](#page-25-0) presents one of the analyzed scenarios as viewed from the [BS.](#page-10-3) The considered [UE](#page-12-0) was moving at a speed of 29 km/h. Its trajectory is indicated by the yellow arrow in Fig. [1.4a.](#page-25-0) Fig. [1.4b](#page-25-0) presents the relative channel magnitude measured by a single antenna and the composite channel of the 100 antenna elements. The authors concluded that the composite channel tends to follow the average of the single antenna case, smoothing out the fast fading. In the analyzed scenario, larger variations started to occur over the course of seconds rather than milliseconds. They also noticed improvements in robustness and latency due to the mitigation of fast-fading error bursts. Another verified benefit of [CH](#page-10-6) was the possibility to relax the update rate of power

Figure 1.4 – [CH](#page-10-6) in an outdoor environment.

Source: [\[44\]](#page-93-10).

control when increasing the number of antennas. In [\[45\]](#page-93-11), some of the authors of [\[44\]](#page-93-10) investigated the practicality of relying on the [CH](#page-10-6) in their design and proposed a power control algorithm exploiting [CH](#page-10-6) properties.

In the literature, it is possible to find works assuming the existence of [CH](#page-10-6) to simplify the adopted models. In [\[46\]](#page-94-0), the power allocation matrix is based only on the large-scale fading characteristics and the same power control is applied over the whole spectrum. In [\[47\]](#page-94-1), the authors assumed that the [UEs](#page-12-0) detect downlink data coherently by assuming that the channel gain is equal to its expected value due to [CH.](#page-10-6) In [\[48\]](#page-94-2), a receiver is presented based on message passing. This receiver exploits the [CH](#page-10-6) for the purposes of detection and channel estimation. In [\[49\]](#page-94-3), [CH](#page-10-6) and spatial resolution properties of massive [MIMO](#page-10-1) are used to derive a new protocol enabling distributed collision detection and resolution at the [UEs.](#page-12-0)

As already mentioned, [CH](#page-10-6) is not always sufficiently pronounced, so one needs to be careful when making these assumptions. Works [\[50\]](#page-94-4) and [\[51\]](#page-94-5) considered a different deployment of massive [MIMO](#page-10-1) called cell free or distributed. In this scenario, multiple antennas of a [BS](#page-10-3) are clustered in geographically separated [APs](#page-10-18) which jointly serve the [UEs.](#page-12-0) These works showed that more antennas are needed in this kind of system to achieve the same level of [CH](#page-10-6) as in co-located massive [MIMO](#page-10-1) antennas, since it is very likely that each [UE](#page-12-0) is most effectively served by only part of the [APs.](#page-10-18)

It is also important to remark that, although the majority of the works exploits the [CH](#page-10-6) in the time domain, [CH](#page-10-6) is also present in the frequency domain, as demonstrated in [\[52\]](#page-94-6). That work showed that the asymptotic [Mean Squared Error \(MSE\)](#page-11-13) of the estimated transmitted symbols may converge to a deterministic quantity not depending on the subcarrier index, i.e., the channel becomes flat across the frequency band. They presented this result for three types of linear receivers, namely, [Zero-Forcing \(ZF\),](#page-12-9) [Matched Filter \(MF\)](#page-10-21) and [Minimum Mean Square](#page-11-14) [Error \(MMSE\).](#page-11-14)

Furthermore, the authors of [\[53\]](#page-94-7) introduced a general definition for the hardening phenomena that includes, but is not limited to, [CH.](#page-10-6) They verified that other metrics in [MIMO](#page-10-1) systems, after being normalized by their mean, as the channel is in Equation [\(1.1\)](#page-22-1), converge to 1 as the number of antennas increases. They provide a simple example considering the distance between arbitrary received code words.

1.2 Objectives and Thesis Structure

Considering what has been presented in the previous section, the main objective of this thesis is to address, in the downlink, the [eMBB](#page-10-17) requirements and the expected lean signaling in [5G](#page-10-0) based on [DC](#page-10-4) and [CH](#page-10-6) occurrence.

The thesis structure is presented in Fig. [1.5](#page-27-0) and is described in the following. On one hand, general analyses related to [DC](#page-10-4) and [CH](#page-10-6) occurrence are presented in Chapter [3](#page-45-0) and Chapter [4,](#page-52-1) respectively. On the other hand, these concepts are addressed from the perspective of [Radio Resource Management \(RRM\)](#page-11-8) in Chapter [5](#page-59-0) and Chapter [6.](#page-79-0)

More specifically, Chapter [3](#page-45-0) aims at exploiting multi-connectivity solutions to improve [QoS](#page-11-11) metrics of the system by means of efficient [RAT](#page-11-0) scheduling. This chapter presents analyses concerning the metrics that should be used as [RAT](#page-11-0) scheduling criterion and how frequently switching evaluations should be done. Besides, the performance of [DC](#page-10-4) and [Fast-RAT](#page-10-7) [Scheduling \(FS\)](#page-10-7) solutions are compared, highlighting the scenarios in which each one of them performs better than the other.

Chapter [4](#page-52-1) proposes a framework for [CH](#page-10-6) detection and L1 measurement optimization, where the [CH](#page-10-6) is detected based on the standard deviation of [Reference Signal Received Power](#page-11-15) [\(RSRP\)](#page-11-15) measurements in a sliding window and the measurement periodicity is dynamically adjusted according to the level of [CH.](#page-10-6)

Chapter [5](#page-59-0) formulates an optimization problem in order to manage resources in a multi[-RAT](#page-11-0) scenario. Its objective is to maximize the minimum user throughput in the system subject to the constraint that, for each [UE,](#page-12-0) its throughput must be higher than its requirement. The referred problem is non-linear and hard to solve. However, we get to transform it into a simpler form, a [Mixed Integer Linear Programming \(MILP\),](#page-10-22) that can be optimally solved using

standard optimization methods. This solution is categorized as a centralized solution. Thus, a distributed framework is also proposed to overcome the drawbacks of centralized processing. This framework is divided into two parts: a [BS](#page-10-3) selection procedure (performed by the [UEs\)](#page-12-0) and a resource assignment algorithm (performed by the [BSs\)](#page-10-3). Besides, a performance evaluation is conducted, considering [LTE](#page-10-11) and [5G](#page-10-0) [NR](#page-11-2) parameters.

Finally, Chapter [6](#page-79-0) focuses on [RRA](#page-11-1) in order to illustrate how the proposed solutions can improve the reliability and decrease the complexity of a [5G](#page-10-0) system. Three different schedulers are considered and three different [Key Performance Indicators \(KPIs\)](#page-10-13) are used to analyze the impact of using either [FS](#page-10-7) or [DC](#page-10-4) strategies and reducing [Channel Quality Indicator \(CQI\)](#page-10-2) reporting due to [CH](#page-10-6) occurrence.

Besides the already described chapters, Chapter [2](#page-30-1) presents an overview of the main [5G](#page-10-0) features used in this thesis and specified in [3GPP](#page-10-5) specification release 15. Moreover, Chapter [7](#page-88-0) summarizes the main conclusions of this thesis.

Figure 1.5 – Thesis structure.

Source: Created by the author.

1.3 Scientific Contributions

Currently, the content of this thesis has been partially published with the following bibliographic information:

Journal Papers

• MONTEIRO, V. F.; ERICSON, M.; CAVALCANTI, F. R. P. Fast-RAT Scheduling in a 5G Multi-RAT Scenario. IEEE Communications Magazine, v. 55, n. 6, p. 79– 85, June 2017. DOI: [10.1109/MCOM.2017.1601094](https://doi.org/10.1109/MCOM.2017.1601094)

- This paper is listed as a publication of METIS II project in [https://metis-ii.](https://metis-ii.5g-ppp.eu/documents/publications/) [5g-ppp.eu/documents/publications/](https://metis-ii.5g-ppp.eu/documents/publications/)

• MONTEIRO, V. F.; SOUSA, D. A.; MACIEL, T. F.; CAVALCANTI, F. R. P.; SILVA, C. F. M.; RODRIGUES, E. B. Distributed RRM for 5G Multi-RAT Multi-Connectivity Networks. IEEE Systems Journal, p. 1–13, 2018. ISSN 1932-8184. DOI: [10.1109/JSYST.2018.2838335](https://doi.org/10.1109/JSYST.2018.2838335)

Patents

- MONTEIRO, V. F.; GUERREIRO, I. M.; FRESIA, M. A Method, a Base Station and a User Equipment for Selecting a Set of Beams to be Monitored by Said UE. Aug. 2017. PCT/EP2017/069410. Patent Application
- MONTEIRO, V. F.; ERICSON, M.; CHRISTOFFERSSON, J.; WANG, M. Methods and Apparatus for Measurement Reporting in a Wireless Network. Apr. 2018. WO/2018/063073. Patent Application. Available from: <[https://patent](https://patentscope.wipo.int/search/en/detail.jsf?docId=WO2018063073) [scope.wipo.int/search/en/detail.jsf?docId=WO2018063073](https://patentscope.wipo.int/search/en/detail.jsf?docId=WO2018063073)>. Visited on: 24 Sept. 2018
- MONTEIRO, V. F.; GUERREIRO, I. M.; DA SILVA, I. L. J. Methods and Apparatus Relating to a Wireless Communication Network that Utilises Beamforming. July 2018. PCT/EP2018/068453. Patent Application
- MONTEIRO, V. F.; RAMACHANDRA, P.; DA SILVA, I. L. Measurement Adaptation Based on Channel Hardening Detection. Nov. 2018. Provisional Patent Application

It is worth mentioning that this thesis was developed under the context of Ericsson/UFC technical cooperation projects:

- UFC.40 *Quality of Service Provision and Control for 5th Generation Wireless Systems*, October/2014 - September/2016;
- UFC.43 *5G Radio Access Network (5GRAN)*, November/2016 October/2018,

in which a number of eight technical reports, four in each project, have been delivered. Besides, due to this partnership, two Ph.D. internships took place during this Ph.D.:

- Feb/2016-Jun/2016: Ph.D. internship at Ericsson Research in Luleå-Sweden;
- Sep/2017-Aug/2018: Ph.D. internship at Ericsson Research in Stockholm/Kista Sweden.

Also in the context of these projects, the author collaborated in the following scientific publication:

Journal Papers

• SOUSA, D. A.; MONTEIRO, V. F.; MACIEL, T. F.; LIMA, F. R. M.; CAVAL-CANTI, F. R. P. Resource Management for Rate Maximization with QoE Provisioning in Wireless Networks. Journal of Communication and Information Systems (JCIS), v. 31, n. 1, p. 290–303, 2016. DOI: [10.14209/jcis.2016.25](https://doi.org/10.14209/jcis.2016.25)

2 IMPORTANT ASPECTS OF [3GPP](#page-10-5) [5G](#page-10-0) TECHNICAL SPECIFICATIONS

The system architecture adopted in this thesis is based on [3GPP](#page-10-5) specification release 15. Thus, for the sake of completeness, this chapter provides technical insights into some [5G](#page-10-0) [NR](#page-11-2) features relevant to the remaining of this thesis. However, before addressing them, next section presents a brief overview of how the [3GPP](#page-10-5) standards are conceived.

2.1 [3GPP](#page-10-5) Working Process

Nowadays, [3GPP](#page-10-5) is the largest standards body in charge of the development of [5G](#page-10-0) standards. It is a collaborative effort among hundreds of different entities, such as manufacturers, mobile service providers and research institutions.

[5G](#page-10-0) standards must achieve the main requirements set by [ITU,](#page-10-16) an agency under the United Nations. Fig. [2.1](#page-30-0) presents a high-level view of [3GPP](#page-10-5) working process [\[54\]](#page-94-8) in order to deliver new technical specifications. In step 1, [3GPP](#page-10-5) members submit technical documents, called *Contributions*, to propose new solutions. These *Contributions* are discussed in regular *[3GPP](#page-10-5) Meetings* and, if approved by the other [3GPP](#page-10-5) members, it becomes a *Study Item*. The *Study Items* are responsible for conducting feasibility studies on multiple solutions based on the proposed *Contributions*. Besides, the *Study Items* must deliver *[Technical Reports \(TRs\)](#page-11-16)* detailing the agreed concepts. Based on these *[TRs](#page-11-16)*, *Working Items* investigate implementation details related to the proposed concepts. Their conclusions are released in the form of *[Technical](#page-11-17) [Specifications \(TSs\)](#page-11-17)*. The *[TSs](#page-11-17)* are used by industry and academia to produce standard compliant products.

Figure 2.2 – Simplistic overview of the [DC](#page-10-4) architecture specified in [3GPP](#page-10-5) specification release 15, where eNB and ng-eNB provide E-UTRA protocol terminations towards the UE via EPC and 5GC, respectively, while en-gNB and gNB provide [NR](#page-11-2) protocol terminations towards the UE via EPC and 5GC, respectively. The colored lines (black, brown and blue) represent the possible ways for control plane flow.

Source: Created by the author.

2.2 [LTE/](#page-10-11)[NR](#page-11-2) Dual Connectivity

One of the most important [TS](#page-11-17) for this thesis is [\[22\]](#page-91-10). This [TS](#page-11-17) provides the details regarding [LTE](#page-10-11) and [NR](#page-11-2) [DC](#page-10-4) operation. It specifies that, when operating in [DC](#page-10-4) mode, a [UE](#page-12-0) is connected to a [Master Node \(MN\)](#page-11-18) and a [Secondary Node \(SN\)](#page-11-19) belonging to different [RATs.](#page-11-0) These nodes are connected via non-ideal backhaul, in terms of capacity and latency, which can restrict the ability to perform inter-node coordination. The standardized architectures are presented in Fig. [2.2](#page-31-0) according to the [Core Network \(CN\)](#page-10-25) being used.

In Fig. [2.2a,](#page-31-0) the [UE](#page-12-0) is connected to the [LTE](#page-10-11) [CN,](#page-10-25) i.e., the [Evolved Packet Core \(EPC\).](#page-10-23) In this case, a [LTE](#page-10-11) [BS,](#page-10-3) i.e., a eNB, always acts as [MN,](#page-11-18) while a [5G](#page-10-0) [BS,](#page-10-3) i.e., a en-gNB, always acts as [SN.](#page-11-19) This will allow an early introduction of [5G](#page-10-0) [NR,](#page-11-2) since eNB and [EPC](#page-10-23) are already deployed. The [LTE](#page-10-11) network will handle control functionalities like connection set-up and paging, while [5G](#page-10-0) [NR](#page-11-2) will be responsible for primarily providing data-rate and capacity boostering.

In Fig. [2.2b,](#page-31-0) the [UE](#page-12-0) is connected to [5G Core Network \(5GC\).](#page-10-24) In this option, either the ng-eNB or the gNB can act as [MN,](#page-11-18) while the other acts as the [SN.](#page-11-19) As the eNB, the ng-eNB provides E-UTRA (the [LTE](#page-10-11) air interface) protocol terminations towards the [UE.](#page-12-0) The difference between them is the [CN](#page-10-25) to which each one is connected to, i.e., ng-eNB connects to [5GC,](#page-10-24) while eNB is only able to connect to [EPC.](#page-10-23) In a similar way, en-gNB and gNB provide [NR](#page-11-2) protocol terminations towards the [UE,](#page-12-0) but through different [CNs.](#page-10-25)

Concerning the user plane, three bearer types exist: master, secondary and split. As

Source: Created by the author.

illustrated in Fig. [2.3,](#page-32-0) on one hand, the master and the secondary bearers are sent through the protocol stack (PDCP, RLC, MAC and PHY) related to the [MN](#page-11-18) and [SN,](#page-11-19) respectively. On the other hand, the split bearer is sent through the lower layers (RLC, MAC and PHY) of both nodes. In order to support this interworking, a common [Packet Data Convergence Protocol \(PDCP\)](#page-11-20) layer is expected to be deployed across both master and secondary nodes. This common layer must be able to process [Protocol Data Units \(PDUs\)](#page-11-21) coming from both air interfaces, i.e., [NR](#page-11-2) and [LTE.](#page-10-11) Thus, enhancements were made in [LTE](#page-10-11) release 14 to support [NR](#page-11-2) [PDCP](#page-11-20) at [LTE](#page-10-11) nodes and, in [\[22\]](#page-91-10), it was standardized that the [NR](#page-11-2) [PDCP](#page-11-20) will be used as aggregation layer for the split bearer.

Besides the [DC,](#page-10-4) this thesis also considered a [FS](#page-10-7) architecture, proposed in [\[55\]](#page-94-9) and illustrated in Fig. [2.4.](#page-33-0) The main difference between [DC](#page-10-4) and [FS](#page-10-7) is that, while, in [DC,](#page-10-4) the [UE](#page-12-0) user plane is allowed to stay simultaneously connected to both [LTE](#page-10-11) and [NR](#page-11-2) [BSs,](#page-10-3) in [FS,](#page-10-7) it is allowed to be connected to only one of them at a time. Concerning the [UE](#page-12-0) control plane, it might stay always connected to the RRC layer of both master and secondary nodes. These RRC connections would be responsible for allowing the [UE](#page-12-0) user plane in the [FS](#page-10-7) mode to switch very fast between the [RATs,](#page-11-0) since no signaling exchanging between the core and the master would be required.

2.3 Flexible Physical Layer

Besides the co-existence of [NR](#page-11-2) and [LTE,](#page-10-11) [3GPP](#page-10-5) also standardized a scalable physical layer design for [NR.](#page-11-2) As in [LTE,](#page-10-11) [Orthogonal Frequency Division Multiplexing \(OFDM\)](#page-11-22) was adopted as waveform of [5G](#page-10-0) [NR.](#page-11-2) However, different of [LTE,](#page-10-11) [5G](#page-10-0) [NR](#page-11-2) is expected to support more than one value of subcarrier spacing as specified in [\[56\]](#page-94-10) and presented in Table [2.1.](#page-33-1)

A larger subcarrier spacing is beneficial from a frequency-error perspective as it reduces the impact of frequency errors and phase noise. However, for a certain cyclic prefix length, the relative overhead increases the larger the subcarrier spacing and from this perspective

Figure 2.4 – Comparison of [DC](#page-10-4) and [FS](#page-10-7) architectures. In [DC,](#page-10-4) control and user planes from master and secondary can be simultaneously connected to the UE, while in [FS,](#page-10-7) the user plane must switch between master and secondary.

Source: Created by the author.

μ	Subcarrier Spacing $2^{\mu} \cdot 15$ [kHz]	Cyclic Prefix $[\mu s]$	Slot Duration [ms]	Nslot 'symbol	N subframe 'slot	N frame 'slot
	15	4.7		14		10
	30	2.3	0.5	14	2	20
	60	1.2	0.25	14	4	40
	120	0.59	0.125	14	8	80
4	240	0.29	0.0625	14	16	160

Table 2.1 – Supported transmission numerologies.

Source: Created by the author.

a smaller cyclic prefix would be preferable [\[57\]](#page-94-11). The selection of the subcarrier spacing therefore needs to carefully balance overhead from the cyclic prefix against sensitivity to Doppler spread and phase noise.

In [NR,](#page-11-2) having a single subcarrier spacing would not be possible, since it is designed to support a wide range of deployment scenarios, from large cells deployed in sub-6 GHz carrier frequency up to small cells deployed in [mmWave](#page-11-10) band with very wide spectrum allocations.

For sub-6 GHz deployments, the cell size can be relatively large and a cyclic prefix capable of handling the delay spread (in the order of a couple of microsseconds) is necessary. Consequently, a subcarrier spacing equal to the one of [LTE](#page-10-11) (15 kHz) or somewhat higher is needed.

In [mmWave](#page-11-10) bands, phase noise becomes more critical, calling for higher subcarrier

spacing. At the same time, due to the challeging propagation conditions in these frequencies, the expected cell size is smaller, which helps to reduce the delay spread. Thus, for these frequencies, a higher subcarrier spacing and a shorter cyclic prefix is suitable.

Regarding the time domain structure, illustrated in Fig. [2.5,](#page-35-0) regardless of the adopted numerology, [NR](#page-11-2) transmissions are divided into *frames* of length equal to 10 ms, each of which is divided into 10 equally sized *subframes* of length equal to 1 ms. A *subframe* is in turn divided into *slots* consisting of 14 [OFDM](#page-11-22) symbols each. Since, when doubling the subcarrier spacing the [OFDM](#page-11-22) symbol duration halves due to the nature of [OFDM,](#page-11-22) there is a different number of *slots* within one *subframe* for each numerology, as presented in Table [2.1](#page-33-1) and in Fig. [2.5.](#page-35-0) Remark that the number of [OFDM](#page-11-22) symbols in one *subframe* changes according to the value of subcarrier spacing.

It is important to highlight that some definitions in [LTE](#page-10-11) and [NR](#page-11-2) are the same, as the duration of a *frame* and of a *subframe*. However, other definitions changed. In [LTE,](#page-10-11) a *slot* consists of 7 [OFDM](#page-11-22) symbols, instead of 14 as in [NR,](#page-11-2) and a [LTE](#page-10-11) *subframe* always consists of 2 *slots* [\[58\]](#page-94-12). Due to these different definitions, in [LTE,](#page-10-11) a *subframe* is the minimum scheduling unit, while in [NR](#page-11-2) a *slot* is the typical scheduling unit.

Another difference between [LTE](#page-10-11) and [NR](#page-11-2) definitions is seen in the frequency domain structure. While the term *resource element* is used by both technologies to refer to one subcarrier during one [OFDM](#page-11-22) symbol, the term *resource block* is used in different ways. On one hand, in [NR,](#page-11-2) a *resource block* is an one-dimensional measure spanning only the frequency domain, more specifically, it corresponds to 12 consecutive subcarriers. On the other hand, in [LTE,](#page-10-11) a *resource block* is a two-dimensional set consisting of 12 subcarriers in the frequency domain and one *slot* in the time domain. One reason for defining, in [NR,](#page-11-2) a *resource block* only in the frequency domain is the flexibility in time duration for different transmissions.

2.4 [CSI-RS](#page-10-8) and [SSB](#page-11-3)

As presented in Chapter [1,](#page-17-0) procedures as [RRA](#page-11-1) and [UE](#page-12-0) mobility management rely on accurate channel quality estimation. For this, [BSs](#page-10-3) and [UEs](#page-12-0) are periodically transmitting and receiving synchronization and reference signals. Thus, in this section, we address two of them: [Channel State Information Reference Signal \(CSI-RS\)](#page-10-8) and [Synchronization Signal Block \(SSB\).](#page-11-3)

CSI-RS

As in [LTE,](#page-10-11) in [NR,](#page-11-2) the [CSI-RSs](#page-10-8) are used for [Channel State Information \(CSI\)](#page-10-26) acquisition, which is important for scheduling and link adaptation. Besides, in [NR,](#page-11-2) their use has been broadened and they are also used for [RSRP](#page-11-15) measurements, which are taken into account for example for mobility management.

Regarding the [RSRP](#page-11-15) measurement procedure, the [SSBs](#page-11-3) are also used to this purpose. In this case, the main difference between [SSBs](#page-11-3) and [CSI-RSs](#page-10-8) is the way how the [UE](#page-12-0) can measure

Source: Created by the author.

Figure 2.6 – [SSB](#page-11-0) and [CSI-RS](#page-10-2) beams.

them. The [SSBs](#page-11-0) are blindly decoded, which means that even in idle mode the [UEs](#page-12-0) can detect and decode them. However, in order to decode the [CSI-RSs,](#page-10-2) the [UEs](#page-12-0) must be already connected, since they need to be configured in advance by the [BSs.](#page-10-3) Among other configurations, the [BSs](#page-10-3) need to inform the [UEs](#page-12-0) in which bandwidth part they should perform the measurements and which [CSI-RSs](#page-10-2) they should monitor [\[59\]](#page-95-1).

Another difference between [SSB](#page-11-0) and [CSI-RS](#page-10-2) is that the second one can be [UE](#page-12-0) specifically configured. This way, one possible deployment is to associate [SSBs](#page-11-0) with wider beams and [CSI-RS](#page-10-2) with narrower beams [\[60\]](#page-95-0), as illustrated in Fig. [2.6.](#page-36-0) On one hand, wider [SSBs](#page-11-0) make the system more robust to blockage, since wider beams can propagate signals in more directions [\[61\]](#page-95-2). On the other hand, narrower [CSI-RSs](#page-10-2) provide better [Signal to Noise Ratio](#page-11-1) [\(SNR\)](#page-11-1) due to the directivity gain. The negative side of using different beamwidth for [SSB](#page-11-0) and [CSI-RS](#page-10-2) is that the range at which a [UE](#page-12-0) could send and receive data, which is based on [CSI-RS](#page-10-2) measurements, will be longer than the range where a cell can be detected [\[62\]](#page-95-3), which is based on [SSB](#page-11-0) measurements.

Concerning the [CSI](#page-10-4) reporting, it may consist of [CQI,](#page-10-5) [Precoding Matrix Indicator](#page-11-2) [\(PMI\),](#page-11-2) [CSI-RS resource indicator \(CRI\),](#page-10-6) [Layer Indication \(LI\),](#page-10-7) [Rank Indicator \(RI\)](#page-11-3) and L1- RSRP [\[63\]](#page-95-4). The [CQI](#page-10-5) informs the [BS](#page-10-3) how good/bad the channel quality is. This information can be used by the [BS](#page-10-3) as an input in order to select the [Modulation and Coding Scheme \(MCS\)](#page-10-8) that will be used in future transmissions.

The [UE](#page-12-0) estimates a [CQI](#page-10-5) for each defined subband, in addition to a wideband [CQI,](#page-10-5) where a subband is a contiguous set of [Resource Blocks \(RBs\)](#page-11-4) [\[63\]](#page-95-4). A [UE](#page-12-0) is configured via higher layer signaling with one out of two possible subband sizes depending on the total number of [RBs](#page-11-4) in the considered carrier bandwidth part according to Table [2.2.](#page-37-0)

Furthermore, for each defined subband the [UE](#page-12-0) calculates the difference between its estimated [CQI](#page-10-5) and the wideband one. Then, it maps this difference into a 2-bit subband differential [CQI](#page-10-5) defined in [\[63\]](#page-95-4). Finally, according to the selected reporting mode (periodic, semi-persistent or aperiodic), the [UE](#page-12-0) reports the wideband [CQI](#page-10-5) with or without some of the 2-bit subband differential [CQIs.](#page-10-5)

Bandwidth part size (# of RBs)	Subband size (# of RBs)	
~< 24	N/A	
24 - 72	4,8	
72 - 144	8, 16	
$145 - 275$	16, 32	

Table 2.2 – Configurable subband size.

Figure 2.7 – Time-frequency structure of a [SSB.](#page-11-0)

Source: Created by the author.

SSB

Regarding the [SSB,](#page-11-0) as illustrated in the top part of Fig. [2.7,](#page-37-1) it is a group of 4 [OFDM](#page-11-5) symbols along 240 subcarriers [\[56\]](#page-94-0). It consists of [Primary Synchronization Signal \(PSS\),](#page-11-6) [Secondary Synchronization Signal \(SSS\)](#page-11-7) and [Physical Broadcast Channel \(PBCH\).](#page-11-8)

As in [LTE,](#page-10-9) in [NR](#page-11-9) there are 3 possible values for [PSS.](#page-11-6) The [UE](#page-12-0) applies a time domain matched filter to search for one of them. After finding it, the [UE](#page-12-0) knows the timing of the [SSB](#page-11-0)

and can also find the [SSS.](#page-11-7) The [SSS](#page-11-7) can assume 336 different values, twice more options than in [LTE.](#page-10-9) Together, [PSS](#page-11-6) and [SSS](#page-11-7) indicate the physical cell ID, which can then assume $3 \times 336 = 1008$ different values [\[56\]](#page-94-0). After decoding the [PSS](#page-11-6) and [SSS,](#page-11-7) the [UE](#page-12-0) can also decode the [PBCH](#page-11-8) and have access to the [Master Information Block \(MIB\)](#page-10-10) [\[59\]](#page-95-1). Since the amount of information in the [MIB](#page-10-10) is quite limited, one of the most important information that it carries is the searching spacing for the [Remaining Minimum System Information \(RMSI\)](#page-11-10) scheduling, which contains the necessary information for getting initial access to the system.

When operating with beams, the [BSs](#page-10-3) will transmit [SSBs](#page-11-0) in bursts. Beams from the same cell have the same [PSS](#page-11-6) and [SSS.](#page-11-7) The main difference between them is the content of [PBCH,](#page-11-8) which tells the beam index and is usually associated with a given transmission direction, as illustrated in the bottom part of Fig. [2.7.](#page-37-1) The number of [SSBs](#page-11-0) that can be broadcast in a burst depends on the frequency range. Frequency ranges up to 3 GHz may have a maximum of 4 [SSBs](#page-11-0) in a burst, while for 3 GHz-6 GHz the maximum is 8 and for [mmWaves](#page-11-11) is 64 [\[64\]](#page-95-5). Furthermore, the time duration of the burst must be lower than or equal to 5 ms.

When accessing the network for the first time, the [UEs](#page-12-0) should assume a [SSB](#page-11-0) periodicity of 20 ms. Other values for the [SSB](#page-11-0) burst periodicity are standardized in [\[59\]](#page-95-1), which are: 5 ms, 10 ms, 40 ms, 80 ms and 160 ms. Compared to [LTE](#page-10-9) [Cell specific Reference Signal \(CRS\),](#page-10-11) the [NR](#page-11-9) [SSB](#page-11-0) design is leaner, since the [NR](#page-11-9) [SSBs](#page-11-0) are transmitted less frequent than the [LTE](#page-10-9) [CRSs,](#page-10-11) which are transmitted at every millisecond and over all the spectrum. This minimizes "always on" broadcasting of system information, allowing power saving and minimizing interference.

2.5 Physical Layer Measurements

As in [LTE,](#page-10-9) the most important metrics on power measurements are [RSRP,](#page-11-12) [Reference](#page-11-13) [Signal Received Quality \(RSRQ\),](#page-11-13) [Received Signal Strength Indicator \(RSSI\)](#page-11-14) and [Signal to](#page-11-15) [Interference-plus-Noise Ratio \(SINR\).](#page-11-15) However, while in [LTE](#page-10-9) these metrics are based on [CRSs](#page-10-11) measurements, in [NR](#page-11-9) they can be based on measurement of either [SSBs](#page-11-0) or [CSI-RSs,](#page-10-2) as standardized in [\[65\]](#page-95-6). Below, you can find a summarized description of them:

- **[RSRP:](#page-11-12)** it is the linear average over the power contributions (in watts) of the resource elements carrying either [SSBs](#page-11-0) or [CSI-RSs](#page-10-2) within the considered measurement frequency bandwidth.
- [RSSI:](#page-11-14) it is the total received power over the entire bandwidth, including signals from co-channel serving and non-serving cells.
- [RSRQ:](#page-11-13) while [RSRP](#page-11-12) is the absolute strength of the reference radio signals, the [RSRQ](#page-11-13) is the ratio:

(number of resource blocks in which the [RSSI](#page-11-14) was measured) \times [RSRP](#page-11-12)

(2.1)

• [SINR:](#page-11-15) it is the linear average over the power contributions (in watts) of the resource elements carrying either [SSBs](#page-11-0) or [CSI-RSs](#page-10-2) divided by the linear average of the noise and interference power contribution (in watts) over the resources carrying either [SSBs](#page-11-0) or [CSI-RSs](#page-10-2) within the considered measurement frequency bandwidth.

In order to demonstrate these concepts, consider Fig. [2.8,](#page-40-0) which illustrates the structure of a two-port [CSI-RS](#page-10-2) [\[57\]](#page-94-1) consisting of two resource elements within an [RB/](#page-11-4)slot block. The blue squares represent resource elements with reference signals and the other squares represent resources carrying other data channels. We assume that the power of all of them is the same, i.e., 0.021 watt. It is important to highlight that [RSRP](#page-11-12) and [RSSI](#page-11-14) are measured only in [OFDM](#page-11-5) symbols containing reference signals. Thus, in Fig. [2.8,](#page-40-0) we have illustrated the power of resource elements in only one [OFDM](#page-11-5) symbol.

As previously stated, [RSRP](#page-11-12) is the linear average of downlink reference signals for a given channel bandwidth, therefore in the example of Fig. [2.8:](#page-40-0)

$$
RSRP = \frac{0.021 + 0.021}{2} = 0.021W = 13.2dBm.
$$
 (2.2)

[RSSI](#page-11-14) is the total received power, thus:

$$
RSSI = 12 \times 0.021 = 0.252W = 24dBm.
$$
 (2.3)

Finally, [RSRQ](#page-11-13) is the ratio between [RSRP](#page-11-12) and [RSSI:](#page-11-14)

$$
RSRQ = 10 \times \log \left(\frac{0.021}{0.252} \right) = -10.79 \, \text{dB}. \tag{2.4}
$$

Comparing [RSRP](#page-11-12) and [RSRQ,](#page-11-13) it is possible to determine if coverage or interference problems occur in a specific location. If [RSRP](#page-11-12) remains stable or becomes even better, while [RSRQ](#page-11-13) is declining, this is a symptom of rising interference. If, on the other hand, both [RSRP](#page-11-12) and [RSRQ](#page-11-13) decline at the same time, this clearly indicates an area with weak coverage.

The most important difference between [RSRQ](#page-11-13) and [SINR,](#page-11-15) is that the first one considers self-interference, since if the [UE](#page-12-0) is receiving data from the serving cell this power will be included in the value of [RSSI.](#page-11-14) For example, in Fig[.2.8,](#page-40-0) the data being received by a [UE](#page-12-0) is accounted in a blue square, which is not considered by the [SINR,](#page-11-15) but it is by the [RSSI,](#page-11-14) and therefore, by the [RSRQ.](#page-11-13)

2.6 Measurement Model

As already mentioned, [SSBs](#page-11-0) and [CSI-RSs](#page-10-2) are used for beam and cell measurements. The measurement model adopted in [5G](#page-10-1) is specified in [\[11\]](#page-90-0) and presented in Fig. [2.9.](#page-40-1) According to this model, in connected mode, the [UEs](#page-12-0) measure multiple beams of a cell and the measurement results are averaged to derive the cell quality. In order to derive beam and cell qualities, filtering takes place at two different levels: at the physical layer (L1) and at upper layers (L3).

Figure 2.8 – Structure of a two-port [CSI-RS](#page-10-2) consisting of two resource elements within an [RB/](#page-11-4)slot block.

Source: Created by the author.

Source: [\[11\]](#page-90-0).

On one hand, the L1 filtering is not constrained by the standard. Each vendor can implement its own filtering method. On the other hand, the beam consolidation and the L3 filtering are standardized.

Regarding the beam consolidation procedure, it averages the Y best beams above a given threshold. The values of Y and of the threshold are provided by [Radio Resource Control](#page-11-16)

Figure 2.10 – Measurement report triggering events.

[\(RRC\)](#page-11-16) signaling. Concerning the L3 filtering, the [UEs](#page-12-0) should use the following formula [\[59\]](#page-95-1):

$$
F_n = (1 - a) \cdot F_{n-1} + a \cdot M_n,\tag{2.5}
$$

where M_n is the latest received measurement from the physical layer; F_n is the updated filtered measurement result; F_{n-1} is the previous filtered measurement result; and $a = 1/2^{k/4}$, where k is the filter coefficient. F_0 is set to M_1 when the first measurement is received.

It is important to highlight that the measurement periodicities at points A^1 , B, C and E are equal.

2.7 Measurement Report Triggering Events

Previous sections have already presented the [3GPP](#page-10-0) specifications related to [5G](#page-10-1) physical layer, the reference and synchronization signals used to derive power measurements, the power measurements themselves and the measurement model. Finally, regarding measurements related to mobility management, e.g., [RSRP](#page-11-12) and [RSRQ,](#page-11-13) this section addresses the events that trigger measurement reporting from the [UEs](#page-12-0) to the [BSs.](#page-10-3) Besides, regarding measurements related to [RRA,](#page-11-17) e.g., [CQI,](#page-10-5) next section addresses how the [BSs](#page-10-3) must perform link adaptation based on the reported [CQI.](#page-10-5)

In order to keep connected to the most suitable [BS,](#page-10-3) the [UEs](#page-12-0) are constantly "hearing" their surroundings. If the signal of either the serving or some neighboring cell reaches predefined conditions, the [UEs](#page-12-0) report this to its serving [BS,](#page-10-3) which will then evaluate the need of taking actions like initiating a handover procedure. These predefined conditions are known as measurement report triggering events and are standardized in [3GPP](#page-10-0) technical specification [\[59\]](#page-95-1). Some of these events are illustrated in Fig. [2.10](#page-41-0) and listed in Table [2.3.](#page-42-0)

Event A3 is one of the most important events for this thesis. It is illustrated in Fig. [2.11.](#page-42-1) Its main idea is to report a measurement when a neighbor [BS](#page-10-3) becomes better than the serving one. The red and blue solid lines represent the serving and neighbor [BS](#page-10-3) [RSRP](#page-11-12) after L3 filtering, respectively. In order to avoid unnecessarily frequent measurement reporting caused by small range of fluctuations, [3GPP](#page-10-0) defines the following parameters: hysteresis, offset and

Figure 2.11 – Measurement report triggering event A3.

Source: Created by the author.

[Time-To-Trigger \(TTT\).](#page-11-18) On one hand, the role of hysteresis and offset is to make the neighbor [BS](#page-10-3) looks worse than serving [BS](#page-10-3) to ensure it is really stronger before the [UE](#page-12-0) decides to send a measurement report. On the other hand, the role of [TTT](#page-11-18) is to ensure that entering condition was reached for real, instead of just for a few instants of time.

Notice in Fig. [2.11](#page-42-1) that the entering conditions is only reached when:

$$
RSRPserving + offsetserving + hysteresis < RSRPneighbor + offsetneighbor.
$$
 (2.6)

After this inequality is satisfied, it must be valid at least for time equal to [TTT](#page-11-18) before the [UE](#page-12-0) starts sending the measurement reports to its serving [BS.](#page-10-3) Then, the [UE](#page-12-0) will periodically send a new measurement to the [BS](#page-10-3) until either it receives a RRC message from its [BS](#page-10-3) or the leaving condition is reached, i.e.,

$$
RSRPserving + offsetserving - hysteresis > RSRPneighbor + offsetneighbor.
$$
 (2.7)

2.8 Link Adaptation

Link adaptation consists of dynamically adjusting the transmission parameters, such as [MCSs,](#page-10-8) to match the conditions of the [UEs'](#page-12-0) radio links. During good propagation conditions, a high order modulation scheme with low coding redundancy is used in order to increase the transmission data rate, while during a signal fade, the system selects a more robust modulation scheme and a higher coding rate to maintain both connection quality and link stability without increasing the signal power [\[66\]](#page-95-7).

Table [2.4](#page-43-0) presents the mapping of [CQI](#page-10-5) into [MCS](#page-10-8) in [NR](#page-11-9) standardized in [\[63\]](#page-95-4). Note that larger [CQI](#page-10-5) indexes, i.e., better channel conditions, allow to transmit more bits on each [OFDM](#page-11-5) symbol and to use the channel more efficiently.

Differences in [MCS](#page-10-8) imply different [BLock Error Rate \(BLER\)](#page-10-12) performances, which can be seen in Fig. [2.12.](#page-44-0) This data is available in [\[67\]](#page-95-8) and it represents the relationship between [SNR,](#page-11-1) [BLER](#page-10-12) and [MCS.](#page-10-8) Note that for the same [SNR,](#page-11-1) higher [MCS](#page-10-8) index represents higher [BLER,](#page-10-12) which means that a given [MCS](#page-10-8) requires a certain [SNR](#page-11-1) to operate with an acceptably low [BLER.](#page-10-12)

			\mathbf{r} ັ				
$\overline{\text{CQI}}$ index	Modulation	Code rate (x 1024)	Rate (bits/symbol)	CQI index	Modulation	Code rate (x1024)	Rate (bits/symbol)
$\overline{0}$		Out of range		8	16OAM	490	1.9141
	OPSK	78	0.152	9	16OAM	616	2.4063
2	OPSK	120	0.234	10	64OAM	466	2.7305
3	OPSK	193	0.377	11	64OAM	567	3.3223
4	OPSK	308	0.602	12	64OAM	666	3.9023
	OPSK	449	0.877	13	64OAM	772	4.5234
6	OPSK	602	1.176	14	64OAM	873	5.1152
	160AM	378	1.477	15	64OAM	948	5.5547

Table $2.4 - COI$ and [MCS](#page-10-8) mapping standardized in [\[63\]](#page-95-4).

Source: Created by the author.

Source: Created by the author.

3 [RAT](#page-11-19) SCHEDULING IN [5G](#page-10-1) MULTI[-RAT](#page-11-19) SCENARIO

This chapter presents general insights related to [5G](#page-10-1) Multi[-RAT](#page-11-19) networks that will support the studies presented in the next chapters related to multi[-RAT.](#page-11-19) It aims at investigating which measurement configuration is more efficient in a multi[-RAT](#page-11-19) scenario. More specifically, we present an analysis concerning the metrics that should be used as [RAT](#page-11-19) scheduling criterion and how frequent these switching evaluations should be done. Finally, we also compare the performance of [DC](#page-10-13) and [FS](#page-10-14) solutions, highlighting the scenarios in which each one of them performs better than the other.

3.1 [HetNet](#page-10-15) Challenges

Section [1.1.1](#page-19-0) presented seven aspects that should be taken into account in [HetNets.](#page-10-15) By optimizing the measurement configuration, we address 4 of these aspects as follows:

- 1. Guarantee a reasonable system performance despite of the *user mobility*: It is addressed by means of adjusting the time between consecutive [RAT](#page-11-19) scheduling evaluations, here called selection of multi[-RAT](#page-11-19) scheduling frequency.
- 2. Reduce the signaling overhead in the *[CN](#page-10-16)* due to frequent handover: It is ensured by the adoption of the [FS](#page-10-14) solution proposed in [\[55\]](#page-94-2).
- 3. Use the *radio resources* across different technologies: It is addressed by the comparison between [FS](#page-10-14) and [DC](#page-10-13) performances.
- 4. Choose a *measurement configuration* to monitor the channel propagation conditions of multiple [RATs](#page-11-19): It is addressed by selecting a metric defined by the [3GPP](#page-10-0) that gives better results when considered as a [RAT](#page-11-19) scheduling criterion.

Before addressing these challenges, the considered [LTE](#page-10-9)[-NR](#page-11-9) scenario will be presented in the next section.

3.2 Simulation Assumptions

The deployment scenario considered in this chapter corresponds to 3 hexagonal cells, within which there are co-sited [LTE](#page-10-9) and [NR](#page-11-9) [BSs,](#page-10-3) with inter-site distance equal to 500 m. The [BSs](#page-10-3) are three-sectored. The system parameters are aligned with the [3GPP](#page-10-0) case 1 typical urban channel model. They are based on Table A-6 of [\[68\]](#page-95-9). We consider that [LTE](#page-10-9) operates at 2 GHz with a subframe duration of 1 ms, while [NR](#page-11-9) operates at 15 GHz with a slot duration of 0.20 ms. It is also assumed that both [RATs](#page-11-19) have the same bandwidth of 20 MHz and the same transmit

Figure 3.1 – Average number of [UEs](#page-12-0) in the system.

power of 40 W. Since [LTE](#page-10-9) operates at a lower frequency than [NR,](#page-11-9) we assume that the coverage of a [NR](#page-11-9) cell is smaller than the coverage of a [LTE](#page-10-9) cell. The main parameters are summarized in Table [3.1.](#page-46-0)

We consider that the [BSs](#page-10-3) are connected to a central entity, which is aware of the value of the main reference signals measured by the [UEs.](#page-12-0)

When not explicitly defined, the [UEs](#page-12-0) were moving at 0.83 m/s (i.e., 3 km/h). For all of them, it is considered a video traffic using UDP with constant packet sizes. The [UEs'](#page-12-0) inter-arrival time follows an exponential distribution, which average number of arrivals per second is a predefined value called intensity. The [UE](#page-12-0) life time is also a predefined value. Fig. [3.1](#page-46-1) illustrates the evolution of the average system load in time. For the analyses we only consider [UEs](#page-12-0) which appear in the system after time equal to ["UE](#page-12-0) life time". Before this, the system is not yet stable, since the number of [UEs](#page-12-0) is still increasing. It is interesting to highlight that between time equal to ["UE](#page-12-0) life time" and " $2 \times$ [\(UE](#page-12-0) life time)" there are still [UEs](#page-12-0) which appeared in the system before time equal to ["UE](#page-12-0) life time", i.e., before the stationary state, thus only the results after " $2 \times$ [\(UE](#page-12-0) life time)" are considered. In this chapter, we consider ["UE](#page-12-0) life time" equal to 15 s and different values for intensity.

In the next sections, we consider the presented scenario to analyze the challenges concerning [RAT](#page-11-19) scheduling, such as, the selection of the multi[-RAT](#page-11-19) scheduling criterion and the

Parameter	LTE	NR
Carrier frequency	2 GHz	15 GHz
System bandwidth	20 MHz	20 MHz
Subframe $(LTE) \setminus$ Slot (NR) duration	1 ms	0.20 ms
Resource blocks per 20 MHz	100	20
Inter-site distance	$500 \,\mathrm{m}$	
BS transmit power	40 W	40 W
Fast fading	Typical urban	Typical urban
Log-normal shadowing std. dev.	8 dB	8 dB

Table 3.1 – Simulation parameters.

Source: Created by the author.

selection of the scheduling frequency. We compare the performance of [FS](#page-10-14) and [DC.](#page-10-13)

3.3 Selection of Multi[-RAT](#page-11-19) Scheduling Criteria

[NR](#page-11-9) is aiming to operate in a wide range of frequencies, and most of the available spectrum is in very high frequency bands. Thus, the [NR](#page-11-9) signal may in many cases be weaker compared to the [LTE](#page-10-9) signal. However, if a huge amount of data is being transmitted over a [LTE](#page-10-9) [BS,](#page-10-3) the interference will degrade the quality of the signal, even if the [LTE](#page-10-9) coverage is good. Thus, when scheduling [RATs,](#page-11-19) it could be interesting to consider not only the signal strength but also its quality. Hence, the first challenge considered here is the scheduling criterion. We investigate whether [RSRQ](#page-11-13) and [SINR](#page-11-15) are appropriated options to replace [RSRP](#page-11-12) as [RAT](#page-11-19) scheduling criterion in order to increase [FS](#page-10-14) performance.

Fig. [3.2](#page-47-0) presents the cell throughput versus the [UE](#page-12-0) throughput for 3 different [RAT](#page-11-19) scheduling criteria, i.e., [RSRQ,](#page-11-13) [SINR](#page-11-15) and [RSRP.](#page-11-12) For each curve, each point with a marker is related to a different number of [UEs](#page-12-0) arriving in the system, i.e., different values of intensity. From the left to right, the values of intensity are: 2, 6, 10, 14, 18, 22, 26, 30, 34 and 38. This figure shows the cases in which the packet loss is lower than 16%. This threshold was achieved by the [RSRP](#page-11-12) curve for intensity equal to 22, i.e., the sixth point, while for the other curves, it was only achieved for intensity higher than 38. That's why there are only 6 points in the [RSRP](#page-11-12) curve, but 10 in the others. We also highlight that the [RSRP](#page-11-12) curve at its sixth point, i.e., for intensity equal to 22, achieves a cell throughput of 13 Mbps/cell and a [UE](#page-12-0) throughput of 1.50 Mbps, while [RSRQ](#page-11-13) and [SINR](#page-11-15) achieve a cell throughput of approximately 15.60 Mbps/cell

and a [UE](#page-12-0) throughput of 2.70 Mbps.

We can see that [RSRP](#page-11-12) presents the worst performance between the considered metrics. This is explained by the fact that [RSRP](#page-11-12) only considers the signal strength. Thus, for high loads, [UEs](#page-12-0) with strong signal for a given [RAT,](#page-11-19) but suffering from high interference, will still connect to this [RAT](#page-11-19) but their transmissions will probably fail. [RSRQ](#page-11-13) is slightly better than [SINR.](#page-11-15)

The presented results suggest that, for the considered scenario, [RSRQ](#page-11-13) and [SINR](#page-11-15) are better [RAT](#page-11-19) scheduling criteria than [RSRP](#page-11-12) in order to improve the [UE](#page-12-0) throughput. Thus, in the next section, [RSRQ](#page-11-13) will be considered as the [RAT](#page-11-19) scheduling criterion. It will be analyzed the impact of reducing the time between consecutive [RSRQ](#page-11-13) evaluations.

3.4 Selection of Multi[-RAT](#page-11-19) Scheduling Frequency

In order to improve the system performance, [FS](#page-10-14) should take advantage of different fading variations in different [RATs,](#page-11-19) switching as fast as possible to the one that fits better. So, it is important to identify the factors that may produce such variations, e.g., the [UE](#page-12-0) mobility. Thus, in this section, we will analyze the impact of reducing the interval between consecutive [RAT](#page-11-19) scheduling evaluations for two different [UE](#page-12-0) speeds: 0.10 m/s (a stationary [UE\)](#page-12-0) and 10 m/s.

Fig. [3.3](#page-48-0) presents the [LTE](#page-10-9) and [NR](#page-11-9) [SINR](#page-11-15) values in time for a specific [UE](#page-12-0) moving at 2 different speeds, i.e., 0.10 m/s and 10 m/s. For each [RAT](#page-11-19) we have two different curves, each one corresponding to a different time of consecutive [RAT](#page-11-19) scheduling evaluations: 10 ms and 100 ms.

In Fig. [3.3a](#page-48-0) [\(UE](#page-12-0) speed equal to 0.10 m/s), we can see that [LTE](#page-10-9) has slower [SINR](#page-11-15) variations than [NR.](#page-11-9) This was already expected, since [LTE](#page-10-9) operates in a lower frequency. From

Figure 3.3 – [SINR](#page-11-15) of a specific [UE](#page-12-0) for two different [UE](#page-12-0) speeds.

Source: Created by the author.

this figure, we can also conclude that, when the [UE](#page-12-0) moves slowly, the [SINR](#page-11-15) does not change too fast. Thus, to consider the time between consecutive [RAT](#page-11-19) scheduling evaluations equal to 10 ms can be seen as unnecessary oversampling, since sampling the [LTE](#page-10-9) link at 10 ms and 100 ms produces similar curves of [SINR](#page-11-15) (in Fig. [3.3a,](#page-48-0) they are overlapped).

Fig. [3.3b](#page-48-0) presents the results related to [UE](#page-12-0) speed equal to 10 m/s. The markers indicate the instant when there is a [RAT](#page-11-19) switching. They are related to the 10 ms and 100 ms curves, respectively. From 15.44 s until 16.64 s, the [LTE](#page-10-9) [SINR](#page-11-15) decreases and the [NR](#page-11-9) [SINR](#page-11-15) increases. After that, they change their trend, the [LTE](#page-10-9) [SINR](#page-11-15) increases and the [NR](#page-11-9) [SINR](#page-11-15) decreases. Remark that both [RAT](#page-11-19) switching procedures, i.e., 10 ms and 100 ms, identify at the same time the moment in which the [NR](#page-11-9) [SINR](#page-11-15) becomes 3 dB higher than [LTE](#page-10-9) [SINR.](#page-11-15) However, 100 ms takes 1.4 s - 0.910 s = 0.490 s more to switch back to [LTE](#page-10-9) than 10 ms. It means that 100 ms stayed longer time using the bad link, which highlights the importance of reducing the time between consecutive evaluations.

Comparing Fig. [3.3a](#page-48-0) and Fig. [3.3b,](#page-48-0) we can see that the [SINR](#page-11-15) varies faster when the [UE](#page-12-0) speed increases. Thus, when the [UE](#page-12-0) moves faster, the time between consecutive evaluations should be reduced in order to capture the channel variations. Different of Fig. [3.3a,](#page-48-0) in Fig. [3.3b,](#page-48-0) the curves concerning 10 ms and 100 ms present different shapes.

When analyzing the cell throughput versus the [UE](#page-12-0) throughput for these 2 different [UE](#page-12-0) speed values, 0.10 m/s and 10 m/s, similar results were obtained. For low speed, the different intervals between consecutive [RAT](#page-11-19) evaluations presented similar results. However, when the [UE](#page-12-0) speed increased, we could see that the system performance degraded more for higher intervals of time between consecutive evaluations. This is a consequence of what was explained in Fig. [3.3.](#page-48-0) For higher [UE](#page-12-0) speeds, higher intervals between consecutive [RAT](#page-11-19) evaluations implies longer time using the bad link.

It is important to highlight that, for instance, in [LTE,](#page-10-9) the inter-frequency handover measurement period is 480 ms [\[69\]](#page-95-10). In that way, we conclude that, for [5G,](#page-10-1) it should be considered a faster measurement period which can vary according to the system conditions, e.g., the [UE](#page-12-0) speed.

3.5 Fast[-RAT](#page-11-19) Scheduling versus Dual Connectivity

The present study compares [DC](#page-10-13) and [FS](#page-10-14) performances considering the improvements suggested in the previous sections, such as the use of [RSRQ](#page-11-13) as [RAT](#page-11-19) scheduling criterion and the reduction of time between consecutive [RAT](#page-11-19) scheduling evaluations to 50 ms.

Fig. [3.4](#page-50-0) presents the [UE](#page-12-0) throughput with [DC](#page-10-13) and [FS.](#page-10-14) This result proves that, for high loads and in the presence of tight integration between [LTE](#page-10-9) and [NR,](#page-11-9) [FS](#page-10-14) can achieve higher [UE](#page-12-0) throughput gains than [DC.](#page-10-13)

[DC](#page-10-13) increases the available bandwidth and the link diversity is improved for higher reliability. For low loads, this results in a throughput performance increase and [DC](#page-10-13) performs better than [FS.](#page-10-14) However, when the load increases in [DC,](#page-10-13) there are more [UEs](#page-12-0) competing for the

Figure 3.4 – [UE](#page-12-0) throughput concerning [FS](#page-10-14) versus [DC.](#page-10-13)

same resources, since the [UEs](#page-12-0) can be connected to both [RATs](#page-11-19) at the same time. Therefore, the system performance may decrease due to higher interference. On the other hand, in [FS,](#page-10-14) the [UEs](#page-12-0) are connected to either [LTE](#page-10-9) or [NR,](#page-11-9) thus they will not compete for the same resources, resulting in higher throughput than [DC](#page-10-13) in high loads.

It is important to highlight that, for low loads, the double of bandwidth in [DC](#page-10-13) does not mean the double of the throughput, since the instantaneous traffic load from a low number of [UEs](#page-12-0) may not be enough to exploit all the system capacity.

Other interesting metric to consider when comparing [DC](#page-10-13) and [FS](#page-10-14) is the [SINR](#page-11-15) per [RAT,](#page-11-19) as presented in Fig. [3.5.](#page-51-0) Usually, [FS](#page-10-14) [UEs](#page-12-0) close to the [BSs](#page-10-3) tend to be connected to [NR,](#page-11-9) while the [FS](#page-10-14) [UEs](#page-12-0) far from [NR](#page-11-9) [BSs](#page-10-3) will connect to [LTE](#page-10-9) [BSs.](#page-10-3) On the other hand, the [DC](#page-10-13) [UEs](#page-12-0) transmitting in [NR](#page-11-9) are not only the ones close to the [NR](#page-11-9) [BSs.](#page-10-3) That is why the [SINR](#page-11-15) of [DC](#page-10-13) [UEs](#page-12-0) transmitting in [NR](#page-11-9) (dashed line with square markers in Fig. [3.5\)](#page-51-0) is worse than the [SINR](#page-11-15) of [FS](#page-10-14) [UEs](#page-12-0) transmitting in [NR](#page-11-9) (solid line with square markers in Fig. [3.5\)](#page-51-0). Similarly, for low loads, the [SINR](#page-11-15) of [DC](#page-10-13) [UEs](#page-12-0) transmitting in [LTE](#page-10-9) (dashed line with triangle markers) is better than the [SINR](#page-11-15) of [FS](#page-10-14) [UEs](#page-12-0) transmitting in [LTE](#page-10-9) (solid line with triangle markers), since [DC](#page-10-13) [UEs](#page-12-0) transmitting in [LTE](#page-10-9) are not only the ones far from the [BSs.](#page-10-3) However, as already said, when the load increases the interference in [LTE](#page-10-9) for [DC](#page-10-13) becomes very important and its [SINR](#page-11-15) decreases very fast.

Considering this, we can conclude that there is not a solution that fits better in all the cases. Thus, it could be interesting to merge [DC](#page-10-13) and [FS](#page-10-14) into a framework that could select the one that fits better in each case, for example, use [DC](#page-10-13) in low loads and [FS](#page-10-14) in high loads.

3.6 Chapter Summary

The analyses presented in this chapter helped in a better understanding of multi[-RAT](#page-11-19) scheduling using either [FS](#page-10-14) or [DC.](#page-10-13) Concerning the measurement configuration, we figured out that metrics related to signal quality, e.g. [RSRQ,](#page-11-13) should be prioritized instead of metrics only related to the signal strength, e.g., [RSRP.](#page-11-12) In a multi[-RAT](#page-11-19) scenario, decision criteria only related to the signal strength tend to overload the [RAT](#page-11-19) with better propagation conditions.

In order to take advantage of channel variations, it was concluded that, in [5G,](#page-10-1) it should be considered shorter time between consecutive [RAT](#page-11-19) scheduling evaluations, which can vary according to the system conditions, e.g., the [UE](#page-12-0) speed.

Finally, the performance of [DC](#page-10-13) and [FS](#page-10-14) were compared, considering the improvements suggested in the previous sections. It was concluded that there is not a solution that fits better in all the cases. While [DC](#page-10-13) performs better than [FS](#page-10-14) for low loads, [FS](#page-10-14) can present higher gains than [DC](#page-10-13) for high loads. Thus, it could be interesting to merge [DC](#page-10-13) and [FS](#page-10-14) into a framework that could select the one that fits better in each case, for example, use [DC](#page-10-13) in low loads and [FS](#page-10-14) in high loads.

4 [5G](#page-10-1) MEASUREMENT ADAPTATION BASED ON CHANNEL HARDENING OC-**CURRENCE**

Now that we have already investigated general aspects related to multi[-RAT](#page-11-19) scenario, we will focus on general aspects of [CH.](#page-10-17) More precisely, this chapter proposes a framework for [CH](#page-10-17) detection and L1 measurement optimization, where the [CH](#page-10-17) is detected based on the standard deviation of [RSRP](#page-11-12) measurements in a sliding window and the measurement periodicity is dynamically adjusted according to the level of [CH,](#page-10-17) where the less the channel fluctuates the higher the level of [CH](#page-10-17) is.

4.1 Introduction

As presented in Section [1.1.2,](#page-21-0) under specific conditions, the channel fluctuations of a link between a [BS](#page-10-3) and a [UE](#page-12-0) may decrease and, in the extreme case, the channel may become flat. Fig. [4.1](#page-52-0) presents the [RSRP](#page-11-12) measured by a random [UE](#page-12-0) in the scenario presented in Table [4.1.](#page-53-0) The [UE](#page-12-0) speed was 0.10 m/s, and the carrier frequency, 28 GHz. Two [BS](#page-10-3) configurations were considered: one with 4 wide [SSBs](#page-11-0) and 4 cross-polarized antennas; and other with 64 narrow [SSBs](#page-11-0) and 64 cross-polarized antennas. Each cross-polarized antenna represents two antenna elements orthogonally deployed.

First, notice that, as expected, considering narrower [SSBs](#page-11-0) (which, in this chapter, is equivalent to increasing the number of [SSBs\)](#page-11-0), the [RSRP](#page-11-12) increases. This is due to the gain of directivity. Besides, remark that in the second case, i.e. 64 [SSBs,](#page-11-0) the [RSRP](#page-11-12) fluctuates less than in the first case, i.e., 4 [SSBs.](#page-11-0) The narrow beams work as spatial filters, hardening the channel. Considering that between 12 s and 16 s the [UE](#page-12-0) is in NLOS state and after 16 s it is in a [LOS](#page-10-18) state, notice that the [RSRP](#page-11-12) gap between these two states is higher in the second case, i.e., 64 [SSBs.](#page-11-0)

Figure 4.1 – Simulation example of UE RSRP measurements.

Source: Created by the author.

Also, in the [Non-Line of Sight \(NLOS\)](#page-11-21) state, the flucuations are higher than in the [LOS](#page-10-18) state.

In the presence of [CH,](#page-10-17) a couple of actions can be done in order to reduce battery consumption, decrease signaling in the control plane, etc. Next section presents a method to identify when [CH](#page-10-17) is happening.

4.2 Channel Hardening Identification

Since [CH](#page-10-17) is characterized by the decrease in channel fluctuations, in order to detect whether it is happening or not in the time domain, we propose that the [UEs](#page-12-0) use a sliding window to log the last X channel quality measurements and calculate their standard deviation. It is expected a low standard deviation when [CH](#page-10-17) happens.

Based on the calculated value, the [UE](#page-12-0) can estimate the "degree" of [CH](#page-10-17) and execute a couple of actions. A simple example is shown in Table [4.2.](#page-54-0) In this case, the L1 measurement period value is being set according to the calculated standard deviation. Fig. [4.2](#page-54-1) presents an illustrative drawing in order to clarify how our proposal would work in practice. The green curves are signal strengths in two situations: with and without [CH.](#page-10-17) The red curves represent the standard deviation related to these signals. The blue lines show the time instants in which the [UE](#page-12-0) would do a new measurement. In this example, if the standard deviation is lower than a given threshold (black dashed line) for at least a few instants of time (equivalent to the [TTT](#page-11-18) in a handover procedure), thus the [UE](#page-12-0) is allowed to change the measurement frequency from very often to seldom.

The standard deviation may depend on the value of X , i.e., the window size. If we have a larger window, a new sample may not have a huge impact on the standard deviation. In this case, a high measurement period could hinder reacting fast to sudden drops in the signal quality, since it would take longer time until we have enough measurements to produce an important change in the standard deviation. To overcome this possible problem, we could also decrease the window size, i.e., the number of samples X , when increasing the measurement period. A shorter

Group	Standard deviation value	Action
01	< 0.30 dBm	Set L1 measurement period equal to 160 ms
02	0.30 dBm to 0.80 dBm	Set L1 measurement period equal to 80 ms
03	\geq 0.80 dBm	Set L1 measurement period equal to 20 ms

Table 4.2 – Example of actions based on the standard deviation.

Figure 4.2 – In the presence of [CH,](#page-10-17) the channel (green curves) presents less fluctuations, i.e., the standard deviation (red curves) decreases, thus it is not necessary to

window size would counterbalance the higher measurement period and fewer samples would be necessary to detect when the signal fluctuations increase, allowing the [UE](#page-12-0) to react faster to this change.

According to [3GPP](#page-10-0) standards, the network sends a measurement reporting configuration to each [UE.](#page-12-0) This configuration typically indicates if the reporting shall be periodic and/or event triggered. It also contains the events and what the [UE](#page-12-0) shall measure, e.g., RSRP, the number of cells, etc. One way to implement the proposed solution is to incorporate these settings in the measurement reporting configuration.

4.3 Channel Hardening in [SSBs](#page-11-0) and [CSI-RSs](#page-10-2) Measurements

Before evaluating the method proposed in the previous section, we analyze the fluctuations in both time and frequency domains. More specifically, this section evaluates the impact of the number of [SSBs](#page-11-0) on the fluctuations of [RSRP](#page-11-12) over the time. Besides, it is also evaluated the impact of the number of [CSI-RSs](#page-10-2) on the fluctuations of [CQI](#page-10-5) measurements along the subbands.

Regarding the [RSRP](#page-11-12) measurements, it was considered a L1 measurement periodicity equal to 20 ms and it was analyzed the standard deviation of the samples inside of a sliding window of 640 ms. Fig. [4.3a](#page-55-0) presents the [Cumulative Distribution Function \(CDF\)](#page-10-19) of the calculated standard deviation. Notice that the 64 [SSBs](#page-11-0) case presents lower values of standard deviation. For example, the percentage of standard deviation samples with value lower than or equal to 0.30 dBm increases from 15% to 34% when increasing the number of [SSBs](#page-11-0) from 4 to 64. This is due to the channel hardening.

Concerning the [CQI](#page-10-5) measurements along the [RBs,](#page-11-4) for each instant of time, it was estimated the power gain coefficient of variation of these measurements. Fig. [4.3b](#page-55-0) presents these statistics for 3 different numbers of [CSI-RSs.](#page-10-2) The higher the number of [CSI-RSs](#page-10-2) is (so, narrower beams) the higher the power gain is and the lower the coefficients of variation are.

[CH](#page-10-17) occurrence in the frequency domain could be exploited to reduce the size of [CQI](#page-10-5) reports. In this case, the [UE](#page-12-0) could report to the [BS](#page-10-3) the [CQI](#page-10-5) of a small set of subbands and inform the [BS](#page-10-3) that [CH](#page-10-17) is happening. Thus, the report size would be reduced without loss of information related to subband quality on the [BS](#page-10-3) side. Moreover, [RRA](#page-11-17) algorithms could also be simplified due to the reduced frequency selectivity. This idea is exploited in Chapter [6.](#page-79-0)

Regarding the [CH](#page-10-17) feasibility, it is important to highlight that [CH](#page-10-17) is more accentuated after coherent precoding has been applied and the [UE](#page-12-0) is aligned with a beam direction. Since [CSI-RSs](#page-10-2) can be [UE](#page-12-0) specific, it is possible to do this for each [UE.](#page-12-0) However, [SSBs](#page-11-0) are used for general broadcast. This is the reason why, in Fig. [4.3,](#page-55-0) we have lower levels of [CH](#page-10-17) in the measurements based on [SSB](#page-11-0) transmission, compared to the ones based on [CSI-RS](#page-10-2) transmission.

4.4 L1 Measurement Periodicity

This section analyzes the framework proposed in Section [4.2.](#page-53-1) The analyses are focused on [RSRP](#page-11-12) measurements based on [SSBs.](#page-11-0)

It was considered a sliding window of 640 ms. Important to remark that although we realize the importance of optimizing the size of the sliding window, this was not studied in this work. We just tried to make sure that its value was neither too low nor too high, since with a large window, e.g., 6 s, we would not be able to quickly react to a change in the channel and with a small one, e.g. 6 ms, we would not have enough samples.

The cell [RSRP](#page-11-12) was sampled using the measurement periodicities proposed in Table [4.2](#page-54-0) and according to their respective standard deviation value. The [RSRP](#page-11-12) samples generated

Figure 4.3 – Analyses of channel fluctuations in time and frequency domains.

Source: Created by the author.

(b) Subbands power gain coefficient of variation.

Figure 4.4 – Difference between RSRP measured with default periodicity, i.e., 20 ms, and higher periodicity.

with a higher measurement periodicity, i.e., 160 ms and 80 ms, were interpolated and we analyzed the difference between them and the samples obtained with the baseline measurement periodicity, i.e., 20 ms. Fig. [4.4](#page-56-0) presents the [CDF](#page-10-19) curves of these differences. The samples were split into 3 groups according to the standard deviation thresholds in Table [4.2.](#page-54-0) The brown curves are related to the case considering 80 ms as the measurement periodicity and the yellow ones are related to the case considering 160 ms as the measurement periodicity.

Considering 0.60 dB as the maximum acceptable difference, which in linear scale corresponds to a difference of 15%, in Fig. [4.4a](#page-56-0) we can see that both 80 ms and 160 ms can be used as a measurement periodicity if the samples standard deviation is lower than 0.30 dBm. Analogously, in Fig. [4.4b,](#page-56-0) we see that 160 ms should not be used as a measurement periodicity in case the standard deviation is lower than 0.80 dBm but greater than or equal to 0.30 dBm, while we can still use the value of 80 ms. Finally, Fig. [4.4c](#page-56-0) shows that neither the values of 80 ms nor 160 ms should be used as a measurement periodicity if the samples standard deviation is higher than or equal to 0.80 dBm.

Also, notice in Fig. [4.4](#page-56-0) that the proposed method is valid not only when we have a high number of [SSBs,](#page-11-0) e.g., 64, but also for the cases with low number of [SSBs,](#page-11-0) e.g., 4. As shown in Fig. [4.3a,](#page-55-0) the scenario with 4 [SSBs](#page-11-0) also presents cases with low [RSRP](#page-11-12) standard deviation, even if they are fewer than in the scenario with more [SSBs.](#page-11-0)

Figure 4.5 – Impact of mobility - 4 and 64 [SSBs](#page-11-0) - sliding window.

Figure 4.6 – Speed - Difference between [RSRP](#page-11-12) measured with default periodicity and higher periodicity.

Source: Created by the author.

4.5 Mobility Impact

The impact of [UE](#page-12-0) mobility on the proposed framework was also evaluated. A similar scenario to the one of the previous section was considered, the only difference is the [UE](#page-12-0) speed. As in Fig. [4.3a,](#page-55-0) Fig. [4.5](#page-57-0) presents the [CDF](#page-10-19) of standard deviation for the cases with

4 and 64 [SSBs,](#page-11-0) but considering 4 different [UE](#page-12-0) speeds. According to this figure, increasing the [UE](#page-12-0) speed increases the channel fluctuations in both cases, i.e., 4 and 64 [SSBs.](#page-11-0) Besides, remark that the mobility has a worse impact in the case with narrow beams, i.e., 64 [SSBs.](#page-11-0) This is due to the fact that spatial focusing of energy provided by a narrow beam translates to a larger spatial decorrelation [\[44\]](#page-93-0). Thus, in a scenario with narrow beams, when moving, a [UE](#page-12-0) will pass through more decorrelated beams. This result highlights the importance of beam tracking techniques in order to be able to quickly update the best beam direction to serve a [UE.](#page-12-0)

Although the number of [UEs](#page-12-0) subjected to channel hardening decreases when the [UE](#page-12-0) speed increases, the method proposed in Section [4.2](#page-53-1) still works as show in Fig. [4.6.](#page-57-1) Similar to Fig. [4.4,](#page-56-0) Fig. [4.6](#page-57-1) presents the [CDF](#page-10-19) of the difference between [RSRP](#page-11-12) samples with baseline measurement periodicity, i.e., 20 ms, and higher measurement periodicity. For group 1, even for higher speeds, both measurement periodicities presented differences lower than 0.60 dB, i.e., 15% in linear scale, in at least 90 % of the cases. For group 2, measurement periodicity equal to 80 ms still presented differences lower than 0.60 dB in more than 90 % of the cases. These results show that, as proposed in Table [4.2,](#page-54-0) measurement periodicity equal to 160 ms can be used for group 1, even when the [UEs](#page-12-0) are moving and that measurement periodicity equal to 80 ms can be used for groups 1 and 2.

4.6 Chapter Summary

The numerical results confirmed that when considering narrower [SSBs](#page-11-0) and [CSI-](#page-10-2)[RSs](#page-10-2) (which, in this chapter, is equivalent to increasing the number of [SSBs](#page-11-0) and [CSI-RSs\)](#page-10-2), the [CH](#page-10-17) becomes more noticeable. Furthermore, the numerical evaluation presented in this chapter validated the proposed framework for [CH](#page-10-17) detection and L1 measurement optimization, where the [CH](#page-10-17) is detected based on the standard deviation of [RSRP](#page-11-12) measurements in a sliding window and the measurement periodicity is dynamically adjusted according to the level of [CH.](#page-10-17) It was also concluded that the [UE](#page-12-0) mobility negatively impacts the [CH,](#page-10-17) i.e., increasing the [UE](#page-12-0) speed increases channel fluctuations for some [UEs.](#page-12-0) Despite of this, the proposed method still works for all [UEs.](#page-12-0)

5 DISTRIBUTED [RRM](#page-11-22) FOR [5G](#page-10-1) MULTI-RAT NETWORKS

In the two previous chapters we investigated general aspects related to multi[-RAT](#page-11-19) and [CH.](#page-10-17) Now, we will address these concepts from the point-of-view of [RRM.](#page-11-22) The present chapter focuses on managing radio resources in a multi[-RAT](#page-11-19) scenario while the next chapter will analyze how to improve, according to the adopted [RRA](#page-11-17) strategy and [KPIs,](#page-10-20) the performance of a multi[-RAT](#page-11-19) network in the presence of [CH.](#page-10-17)

More precisely, the present chapter formulates a [RRA](#page-11-17) optimization problem aiming at maximizing the minimum [UE](#page-12-0) throughput in the system subject to the constraint that for each [UE,](#page-12-0) its throughput must be higher than a requirement. The referred problem is non-linear and complex to solve. However, we get to transform it into a simpler form, a [MILP,](#page-10-21) that can be optimally solved using standard optimization methods. This solution is categorized as a centralized solution. Thus, we propose a distributed framework to overcome the drawbacks of centralized processing, e.g., processing costs and increased signaling overhead. This framework is divided into two parts: a [BS](#page-10-3) selection procedure (performed by the users) and a resource assignment algorithm (performed by the [BSs\)](#page-10-3). Besides, a performance evaluation is conducted, considering 4G [LTE](#page-10-9) and [5G](#page-10-1) [NR](#page-11-9) parameters.

5.1 Introduction

Considering the context of tight interworking between [5G](#page-10-1) [NR](#page-11-9) and [LTE,](#page-10-9) the traditional concept of resource can be extended from time, frequency, space and power to also include radio interfaces and access nodes. Thus, efficient [RRM](#page-11-22) techniques will be even more important than they were before.

[RRM](#page-11-22) techniques have already been broadly studied in the literature as it can be seen in [\[72\]](#page-96-0), where an extensive survey on these techniques is presented for multi-user [MIMO](#page-10-22) systems. However, the majority of them do not address some of the challenges presented in [HetNets,](#page-10-15) as the ones presented in Section [1.1.1.](#page-19-0)

In such heterogeneous networks, [UEs](#page-12-0) face different radio conditions (e.g., they may not be on the coverage area of the same [RATs\)](#page-11-19). Despite this, their tight requirements must be met by the operators. Satisfying all the [UEs](#page-12-0) despite of the network conditions is an important task in [5G](#page-10-1) and it is the main driver of this chapter.

In this context, we consider an optimization problem that maximizes the minimum [UE](#page-12-0) throughput in the system, while satisfying all the [UEs,](#page-12-0) i.e., keeping their throughput higher than their requirements. In other words, while keeping all the [UEs](#page-12-0) satisfied, we try to keep the throughput of the [UEs](#page-12-0) in bad radio conditions as high as possible, since this can avoid dissatisfaction in case their radio conditions get worse. When other objective functions are adopted, e.g., maximize system throughput, it is harder to keep all the [UEs](#page-12-0) satisfied over the time, since, usually, these functions allocate to the worst [UEs](#page-12-0) only the enough amount of resources to keep them in the limit of satisfaction. However, if their radio conditions get even worse, they might enter starvation due to lack of resources.

The remainder of this chapter is organized as follows. Sections [5.2](#page-60-0) and [5.3](#page-61-0) introduce the network model and the problem formulation, respectively. Sections [5.4](#page-62-0) and [5.5](#page-65-0) present the centralized solution and the proposed distributed framework, respectively. Section [5.6](#page-69-0) provides a practical view of our proposal, illustrating how it can be mapped into [3GPP](#page-10-0) network parameters and how they can be obtained. The proposed framework is evaluated via worst-case computational complexity analysis in Section [5.7](#page-70-0) and via computational simulations in Section [5.8.](#page-70-1) Finally, in Section [5.9,](#page-77-0) the main conclusions of this chapter are presented.

5.2 System Model

It is considered a system with U [UEs](#page-12-0) and N [RATs,](#page-11-19) where the UEs and [RATs](#page-11-19) are grouped in the sets [U](#page-13-3) and [N](#page-13-4), respectively. In [RAT](#page-11-19) *n* there are B_n B_n [BSs](#page-10-3) grouped in the set \mathcal{B}_n , where $B = \bigcup_{n \in \mathbb{N}} B_n$ $B = \bigcup_{n \in \mathbb{N}} B_n$ and $B = |\mathcal{B}|$.

As explained in Section [2.3,](#page-32-0) [LTE](#page-10-9) and [NR](#page-11-9) use different words to define the minimum allocable time-frequency chunk, however in this chapter we will use the term [RB](#page-11-4) for this purpose independently of the considered [RAT.](#page-11-19)

Each [RB](#page-11-4) is composed of a number of adjacent subcarriers in the frequency domain and of a number of [OFDM](#page-11-5) symbols spanning the duration of one [Transmission Time Interval](#page-11-23) [\(TTI\)](#page-11-23) in the time domain. Moreover, all the [BSs](#page-10-3) of [RAT](#page-11-19) *n* reuse K_n K_n [RBs](#page-11-4) arranged in the set K_n . The set containing all [RBs](#page-11-4) is defined as $\mathcal{K} = \bigcup_{n \in \mathbb{N}} \mathcal{K}_n$ $\mathcal{K} = \bigcup_{n \in \mathbb{N}} \mathcal{K}_n$ $\mathcal{K} = \bigcup_{n \in \mathbb{N}} \mathcal{K}_n$ and $K = |\mathcal{K}|$.

We also consider that the total transmit power available at each [BS](#page-10-3) of [RAT](#page-11-19) n is equal to P_n , which is equally distributed among all their [RBs.](#page-11-4) Thus, the power $p_{u,k,b}$ used by [BS](#page-10-3) b of [RAT](#page-11-19) *n* through [RB](#page-11-4) *k* to transmit to [UE](#page-12-0) *u* is $p_{u,k,b} = P_n/K_n$.

A joint optimization of [BS](#page-10-3) selection, resource assignment and power allocation would lead to a better performance. However, if an adaptive rate scheme is already implemented, the benefit of a joint optimization taking into account power allocation might be marginal when compared to the [Equal Power Allocation \(EPA\)](#page-10-23) case, which requires lower complexity [\[73\]](#page-96-1). Thus, in order to achieve a good trade-off between performance and complexity, [EPA](#page-10-23) with an adaptive rate scheme was adopted in the present work.

The channel coefficient $h_{u,k}$, [t] between [BS](#page-10-3) b and [UE](#page-12-0) u at [TTI](#page-11-23) t is approximated by the coefficient of the first symbol of the middle subcarrier that composes [RB](#page-11-4) k . Moreover, we assume that it remains constant during the period of one [TTI.](#page-11-23)

Therefore, the [SNR](#page-11-1) related to [UE](#page-12-0) u on [RB](#page-11-4) k available in [BS](#page-10-3) b is given by:

$$
\gamma_{u,k,b}[t] = \frac{p_{u,k,b}[t] |h_{u,k,b}[t]|^2}{\sigma^2},\tag{5.1}
$$

in which σ^2 denotes the thermal noise power.

We assume that the data transmission considers a link adaptation scheme which allows each [BS](#page-10-3) to transmit with a set of possible [MCSs](#page-10-8) with very low [BLER.](#page-10-12) The [MCS](#page-10-8) selected by a [BS](#page-10-3) is a function of the [SNR](#page-11-1) $\gamma_{u,k,b}[t]$.

Finally, let $x_{u,k,b}[t]$ be the assignment index indicating whether [RB](#page-11-4) k, reused by [BS](#page-10-3) b, is allocated to [UE](#page-12-0) u at [TTI](#page-11-23) t. Also, let $r_{u,k,b}[t]$ be the number of transmitted bits to UE u in [RB](#page-11-4) k of [BS](#page-10-3) *b* if this [RB](#page-11-4) is allocated to [UE](#page-12-0) *u* at [TTI](#page-11-23) *t*, where $r_{u,k,b}[t]$ is a function of $\gamma_{u,k,b}[t]$. The mean throughput $\theta_u[t]$ of [UE](#page-12-0) u between [TTIs](#page-11-23) 1 and t is then defined as

$$
\theta_u[t] = \frac{1}{t} \left[\sum_{j=1}^t \sum_{b=1}^B \sum_{k=1}^K x_{u,k,b}[j] r_{u,k,b}[j] \right].
$$
 (5.2)

The number of received bits $g_u[t]$ by [UE](#page-12-0) u until [TTI](#page-11-23) t, t included, is $g_u[t] = t\theta_u[t]$, therefore [\(5.2\)](#page-61-1) can be rewritten as

$$
\theta_u[t] = \frac{1}{t} \left[g_u[t-1] + \sum_{b=1}^{B} \sum_{k=1}^{K} x_{u,k,b}[t] r_{u,k,b}[t] \right].
$$
\n(5.3)\n
\nreceived bits\n
\nuncived bits\n
\nreceived bits at TTI *t*

5.3 Problem Formulation

In the following, the analyses are done [TTI](#page-11-23) per [TTI.](#page-11-23) Thus, in order to simplify the notation, we will replace $x_{u,k,b}[t]$ and $r_{u,k,b}[t]$ by $x_{u,k,b}$ and $r_{u,k,b}$, respectively. However, the reader should keep in mind that for different [TTIs](#page-11-23) these variables assume different values, as allocation is done per [TTI.](#page-11-23)

As previously mentioned, [RRM](#page-11-22) techniques will play an important role in [5G](#page-10-1) systems in order to efficiently manage radio resources across different [RATs.](#page-11-19) In this context, we aim at maximizing, at each [TTI](#page-11-23) t , the minimum rate experienced by all [UEs](#page-12-0) in the system subject to the constraint that for each [UE](#page-12-0) u in [U](#page-13-3), its throughput $\theta_u[t]$ at [TTI](#page-11-23) t must be at least ψ_u .

Furthermore, the considered problem has other constraints, e.g., each [BS](#page-10-3) can allocate a [RB](#page-11-4) to only one [UE](#page-12-0) at a time and UE u can only be connected to $l_{u,n}$ different [BSs](#page-10-3) of [RAT](#page-11-19) n at the same time. Moreover, consider $\omega_{k,n}$ as a binary parameter equal to one if [RB](#page-11-4) k can be used by the [BSs](#page-10-3) of [RAT](#page-11-19) *n*, i.e., $k \in \mathcal{K}_n$ $k \in \mathcal{K}_n$ $k \in \mathcal{K}_n$, and zero otherwise; and $\lambda_{b,n}$ as a binary parameter equal to one if the [BS](#page-10-3) *b* belongs to the [RAT](#page-11-19) *n*, i.e., $b \in \mathcal{B}_n$ $b \in \mathcal{B}_n$ $b \in \mathcal{B}_n$, and zero otherwise. It is important to highlight that, it does not make sense to consider $x_{u,k,b}$ and $r_{u,k,b}$ if $\lambda_{b,n} = 1$ and $\omega_{k,n} = 0$. For these cases, consider $x_{u,k,b} = r_{u,k,b} = 0$. Taking into account these constraints, the considered optimization

problem can be formulated as

$$
\max_{\overline{\mathbf{X}}} \min_{u \in \mathcal{U}} \left(\frac{1}{t} \left[g_u[t-1] + \sum_{b=1}^{B} \sum_{k=1}^{K} x_{u,k,b} r_{u,k,b} \right] \right), \tag{5.4a}
$$

$$
\text{s.t. } \frac{1}{t} \left[g_u[t-1] + \sum_{b=1}^{B} \sum_{k=1}^{K} x_{u,k,b} r_{u,k,b} \right] \ge \psi_u, \forall u \in \mathcal{U}, \tag{5.4b}
$$

$$
\sum_{u=1}^{U} x_{u,k,b} \le 1, \forall k \in \mathcal{K} \text{ and } b \in \mathcal{B},\tag{5.4c}
$$

$$
\sum_{b=1}^{B} H\left(\sum_{k=1}^{K} x_{u,k,b}, 1\right) \lambda_{b,n} \le l_{u,n}, \forall u \in \mathcal{U}, \forall n \in \mathcal{N},
$$
\n(5.4d)

$$
\sum_{u=1}^{U} \sum_{k=1}^{K} \sum_{b=1}^{B} x_{u,k,b} \left(1 - \sum_{n=1}^{N} \lambda_{b,n} \omega_{k,n} \right) = 0, \text{ and } (5.4e)
$$

$$
x_{u,k,b} \in \{0,1\},\tag{5.4f}
$$

where the elements $x_{u,k,b}$ are arranged in a multi-dimensional array $\mathbf{X} \in \{0,1\}^{\mathcal{U} \times \mathcal{K} \times \mathcal{B}}$ and $H(a,b)$ is the Heaviside function, which returns either one, if $a \ge b$, or zero, otherwise.

In [\(5.4a\)](#page-62-1) the objective function is the minimum rate in the system, i.e., $\min_{u \in \mathcal{U}} (\theta_u[t])$, where $\theta_{\nu}[t]$ is given in [\(5.3\)](#page-61-2). Constraint [\(5.4b\)](#page-62-2) states that all the [UEs](#page-12-0) must be satisfied, i.e., their throughput must be higher than their requirement ψ_u , while constraint [\(5.4c\)](#page-62-3) states that none [BS](#page-10-3) may allocate a [RB](#page-11-4) to more than one [UE](#page-12-0) at the same time.

In [\(5.4d\)](#page-62-4), H $(\sum_{k=1}^{K} x_{u,k,b}, 1)$ equals one only if [BS](#page-10-3) *b* allocates at least one [RB](#page-11-4) to [UE](#page-12-0) *u*, otherwise it is equal to zero. Thus, the left hand side of [\(5.4d\)](#page-62-4) represents the number of [BSs](#page-10-3) of [RAT](#page-11-19) *to which [UE](#page-12-0)* $*u*$ *is connected and the entire equation itself is related to the constraint on the* number of connections of each [UE.](#page-12-0) Also, $(5.4e)$ means that the [RB](#page-11-4) k can only be allocated by [BS](#page-10-3) *b*, if there is $n \in [1, N]$, such that $\lambda_{b,n} \omega_{k,n} = 1$, otherwise $(1 - \sum_{n=1}^{N} \lambda_{b,n} \omega_{k,n}) = 1$, then $x_{u,k,b}$ must be equal to zero.

Notice that [\(5.4d\)](#page-62-4) is neither a convex nor a concave function, thus in the next section we will rewrite this constraint in order to achieve a simpler instance of the problem and use it as a centralized benchmark solution.

5.4 Centralized Benchmark Solution

In this section, problem [\(5.4\)](#page-62-4) is reformulated as a [MILP,](#page-10-21) which can be solved by standard algorithms, such as the [Branch and Bound \(BB\)](#page-10-24) method [\[74\]](#page-96-2). Otherwise, it would be necessary to use the brute force or exhaustive search.

The non-linear objective function [\(5.4a\)](#page-62-1) can be linearized by introducing a slack variable μ and a new constraint, as in [\(5.5a\)](#page-63-0) and [\(5.5b\)](#page-63-1). We can also rewrite [\(5.4d\)](#page-62-4) as three new linear constraints, i.e., [\(5.5e\)](#page-63-2), [\(5.5f\)](#page-63-3) and [\(5.5g\)](#page-63-4), where the slack variable $\xi_{u,b} \in \{0,1\}$ is equal to one if the [UE](#page-12-0) u has any [RB](#page-11-4) allocated in the [BS](#page-10-3) b and zero, otherwise. These variables are arranged in the matrix $\Xi \in \{0, 1\}^{U \times B}$.

Therefore, applying these replacements in [\(5.4\)](#page-62-4) yields

$$
\max_{\mu,\overline{\mathbf{X}},\Xi} \mu,\tag{5.5a}
$$

s.t.
$$
\frac{1}{t} \left[g_u[t-1] + \sum_{b=1}^{B} \sum_{k=1}^{K} x_{u,k,b} r_{u,k,b} \right] \ge \mu, \forall u \in \mathcal{U},
$$
 (5.5b)

$$
\frac{1}{t}\left[g_u[t-1]+\sum_{b=1}^B\sum_{k=1}^K x_{u,k,b}r_{u,k,b}\right] \ge \psi_u, \forall u \in \mathcal{U},\tag{5.5c}
$$

$$
\sum_{u=1}^{U} x_{u,k,b} \le 1, \forall k \in \mathcal{K} \text{ and } b \in \mathcal{B},\tag{5.5d}
$$

$$
\sum_{k=1}^{K} x_{u,k,b} \le K \xi_{u,b}, \forall u \in \mathcal{U} \text{ and } \forall b \in \mathcal{B}, \tag{5.5e}
$$

$$
\sum_{k=1}^{K} x_{u,k,b} \ge \xi_{u,b}, \forall u \in \mathcal{U} \text{ and } \forall b \in \mathcal{B}, \tag{5.5f}
$$

$$
\sum_{b=1}^{B} \lambda_{b,n} \xi_{u,b} \le l_{u,n}, \forall u \in \mathcal{U} \text{ and } \forall n \in \mathcal{N}, \tag{5.5g}
$$

$$
\sum_{u=1}^{U} \sum_{k=1}^{K} \sum_{b=1}^{B} x_{u,k,b} \left(1 - \sum_{n=1}^{N} \lambda_{b,n} \omega_{k,n} \right) = 0, \qquad (5.5h)
$$

$$
x_{u,k,b} \in \{0,1\} \text{ and } \tag{5.5i}
$$

$$
\xi_{u,b} \in \{0,1\}.\tag{5.5j}
$$

If $\xi_{u,b} = 0$, [UE](#page-12-0) u is not connected to [BS](#page-10-3) b, and, according to [\(5.5e\)](#page-63-2) and [\(5.5f\)](#page-63-3), $x_{u,k,b}$ must be equal to zero $\forall k$, i.e., it can not be scheduled by this [BS.](#page-10-3)

The product $\lambda_{b,n} \xi_{u,b}$ in [\(5.5g\)](#page-63-4) is equal to one only if $\lambda_{b,n} = \xi_{u,b} = 1$, i.e., if [UE](#page-12-0) *u* is connected to [BS](#page-10-3) b and this BS belongs to [RAT](#page-11-19) n . So, the left hand side of [\(5.5g\)](#page-63-4) represents the number of [BSs](#page-10-3) of [RAT](#page-11-19) n to which [UE](#page-12-0) u is connected and the entire equation itself is related to the constraint on the number of connections of each [UE.](#page-12-0)

At this point, we introduce some concepts and definitions related to tensors. The first step is to arran[g](#page-14-15)e the elements $g_u[t-1]$ and ψ_u in the column vectors $g[t-1]$ and ψ , respectively; and the elements $\xi_{u,b}, \lambda_{b,n}, l_{u,n}$ and $\omega_{k,n}$, in the matrices Ξ , Λ Λ Λ , **L** and Ω , respectively. Now, we define the concept of unfolding. Considering that the elements $x_{u,k}$, are arranged in a multidimensional array $\overline{\mathbf{X}} \in \{0,1\}^{U \times K \times B}$ $\overline{\mathbf{X}} \in \{0,1\}^{U \times K \times B}$ $\overline{\mathbf{X}} \in \{0,1\}^{U \times K \times B}$, we denote $\mathbf{X}^{(2)} \in \{0,1\}^{K \times UB}$ as the mode-2 unfolding of $\overline{\mathbf{X}}$, where the elements $x^{(2)}$ of $X^{(2)}$ $X^{(2)}$ are defined in function of the elements of \overline{X} as $x^{(2)}_{k,n}$ $\sum_{k,u+(b-1)U}^{\infty} = x_{u,k,b}.$ Likewise, the elements $r_{u,k,b}$ form the multi-dimensional array $\overline{\mathbf{R}}$ $\overline{\mathbf{R}}$ $\overline{\mathbf{R}}$. The second concept is the [vec](#page-13-23) $\{\cdot\}$ operation. It is defined as vec $\{Z\} = \begin{bmatrix} \mathbf{Z} & \mathbf{Z} \\ \mathbf{Z} & \mathbf{Z} \end{bmatrix}$ $\mathbf{z}_1^{\mathrm{T}}$ $\mathbf{z}_1^{\mathrm{T}}$ $\mathbf{z}_1^{\mathrm{T}}$ $\mathbf{z}_2^{\mathrm{T}}$ $\mathbf{z}_2^{\mathrm{T}}$ $\mathbf{z}_2^{\mathrm{T}}$ **z**₂ $\mathbf{z}_2^{\mathrm{T}}$ $\mathbf{z}_2^{\mathrm{T}}$ $\mathbf{z}_2^{\mathrm{T}}$... $\mathbf{z}_J^{\mathrm{T}}$ 1^T 1^T 1^T , where z_j is the *j*-th column of matrix **Z** and $\{\cdot\}^T$ $\{\cdot\}^T$ is the transpose operation. To simplify the notation, we rename the following [vec](#page-13-23)tors: $\mathbf{x} = \text{vec}\left\{\mathbf{X}^{(2)^T}\right\}$ and $\mathbf{r} = \text{vec}\left\{\mathbf{R}^{(2)^T}\right\}$ $\mathbf{r} = \text{vec}\left\{\mathbf{R}^{(2)^T}\right\}$ $\mathbf{r} = \text{vec}\left\{\mathbf{R}^{(2)^T}\right\}$. We also consider **Z**⊙S as the Hadamard product and **Z**[⊗](#page-13-27)**Y** as the Kronecker product, where **S** and **Z** ∈ $\mathbb{R}^{I \times J}$ and **Y** ∈ $\mathbb{R}^{T \times R}$.

Finally, defining I_U I_U as an $U \times U$ identity matrix and I_U as a column vector with U

ones, we can reformulate [\(5.5\)](#page-63-2) using a tensorial notation as

$$
\max_{\mu, \mathbf{x}, \Xi} \quad \mu,\tag{5.6a}
$$

s.t.
$$
\mathbf{g}[t-1] + [(\mathbf{1}_{KB}^T \otimes \mathbf{I}_U) \odot (\mathbf{1}_U \otimes \mathbf{r}^T)] \mathbf{x} \ge t\mu \mathbf{1}_U,
$$
 (5.6b)

$$
\mathbf{g}[t-1] + \left[\left(\mathbf{1}_{KB}^{\mathrm{T}} \otimes \mathbf{I}_{U} \right) \odot \left(\mathbf{1}_{U} \otimes \mathbf{r}^{\mathrm{T}} \right) \right] \mathbf{x} \geq t \left[\left(\boldsymbol{\psi} \otimes \mathbf{1}_{U}^{\mathrm{T}} \right) \odot \mathbf{I}_{U} \right] \mathbf{1}_{U}, \tag{5.6c}
$$

$$
\left(\mathbf{I}_{KB} \otimes \mathbf{1}_U^T\right) \mathbf{x} \le \mathbf{1}_{KB},\tag{5.6d}
$$

$$
\left(\mathbf{1}_K^{\mathrm{T}} \otimes \mathbf{I}_{UB}\right) \mathbf{x} \leq K \text{vec} \left\{\Xi\right\},\tag{5.6e}
$$

$$
\left(\mathbf{1}_K^{\mathrm{T}} \otimes \mathbf{I}_{UB}\right) \mathbf{x} \ge \text{vec}\left\{\Xi\right\},\tag{5.6f}
$$

$$
\left(\Lambda^{T} \otimes I_{U}\right) \text{vec} \left\{ \Xi \right\} \leq \text{vec} \left\{ L \right\},\tag{5.6g}
$$

$$
\left\{-\mathbf{1}_N^{\rm T}\left[(\mathbf{1}_K{\otimes}\Lambda{\otimes}\mathbf{1}_U)\odot(\Omega{\otimes}\mathbf{1}_{UB})\right]^{\rm T}+\right.
$$

$$
\mathbf{1}_{UKB}^{\mathrm{T}} \mathbf{X} = 0,\tag{5.6h}
$$

$$
\mathbf{x} \in \{0, 1\}^{UKB \times 1} \text{ and } (5.6i)
$$

$$
\text{vec}\{\Xi\} \in \{0,1\}^{UB \times 1}.\tag{5.6j}
$$

The equations in [\(5.6\)](#page-63-3) are similar to their equivalents in [\(5.5\)](#page-63-2), e.g., [\(5.6c\)](#page-63-5) and [\(5.5c\)](#page-63-5), the only difference is that in [\(5.6\)](#page-63-3) we use vectors and matrices to replace the index notation. For example, [\(5.6c\)](#page-63-5) and [\(5.5c\)](#page-63-5) mean that all the [UEs](#page-12-0) must be satisfied, i.e., their throughput must be higher than their requirement ψ_u ; [\(5.5d\)](#page-63-6) and [\(5.6d\)](#page-63-6) mean that none [BS](#page-10-3) can allocate the same [RB](#page-11-4) to more than one [UE](#page-12-0) at the same time; [\(5.6e\)](#page-63-2), [\(5.6f\)](#page-63-3), [\(5.6g\)](#page-63-4), [\(5.5e\)](#page-63-2), [\(5.5f\)](#page-63-3) and [\(5.5g\)](#page-63-4) are related to the fact that none [UE](#page-12-0) can be connected to more than $l_{u,n}$ [BSs](#page-10-3) of [RAT](#page-11-19) *n*.

At this point, the variables of our problem are: μ , **x** and Ξ . To simplify even more the notation, they can be arranged into one single vector **w**, in which

$$
\mathbf{w} = \left[\mu \mid \mathbf{x}^{\mathrm{T}} \mid \text{vec}^{\mathrm{T}} \{ \Xi \} \right]^{\mathrm{T}}. \tag{5.7}
$$

Then, considering $\mathbf{0}_{UB}$ and $\mathbf{0}_{UB\times UKB}$ as a column vector with UB zeros and a $UB\times UKB$ matrix of zeros, respectively; and defining **m**, **A** and **B** as

$$
\mathbf{m} = \left[1 \left| \mathbf{0}_{UKB}^{T} \right| \mathbf{0}_{UB}^{T} \right]^{T} \Rightarrow \mathbf{m}^{T} \mathbf{w} = \mu,
$$
 (5.8a)

$$
\mathbf{A} = \left[\begin{array}{c} \mathbf{0}_{UKB} \end{array} \middle| \mathbf{I}_{UKB} \end{array} \middle| \mathbf{0}_{UKB \times UB} \right] \Rightarrow \mathbf{A}\mathbf{w} = \mathbf{x} \text{ and } (5.8b)
$$

$$
\mathbf{B} = \left[\begin{array}{c} \mathbf{0}_{UB} \end{array} \middle| \mathbf{0}_{UB\times UKB} \end{array} \middle| \mathbf{I}_{UB} \right] \Rightarrow \mathbf{B}\mathbf{w} = \text{vec} \left\{ \Xi \right\}, \tag{5.8c}
$$

we can finally rewrite the optimization problem [\(5.6\)](#page-63-3) as

$$
\max_{\mathbf{w}} \mathbf{m}^{\mathrm{T}} \mathbf{w}, \text{ s.t. } \mathbf{C} \cdot \mathbf{w} \le \mathbf{d} \text{ and } \mathbf{e} \cdot \mathbf{w} = 0,
$$
 (5.9)

where

$$
\mathbf{C} = \begin{bmatrix} t\mathbf{1}_U \mathbf{m}^{\mathrm{T}} - \left[(\mathbf{1}_{KB}^{\mathrm{T}} \otimes \mathbf{I}_U) \odot (\mathbf{1}_U \otimes \mathbf{r}^{\mathrm{T}}) \right] \mathbf{A} \\ - \left[(\mathbf{1}_{KB}^{\mathrm{T}} \otimes \mathbf{I}_U) \odot (\mathbf{1}_U \otimes \mathbf{r}^{\mathrm{T}}) \right] \mathbf{A} \\ (\mathbf{I}_{KB} \otimes \mathbf{1}_U^{\mathrm{T}}) \mathbf{A} \\ (\mathbf{1}_{KB}^{\mathrm{T}} \otimes \mathbf{I}_{UB}) \mathbf{A} - K \mathbf{B} \\ \mathbf{B} - (\mathbf{1}_{KB}^{\mathrm{T}} \otimes \mathbf{I}_{UB}) \mathbf{A} \\ (\Lambda^{\mathrm{T}} \otimes \mathbf{I}_U) \mathbf{B} \end{bmatrix}, \qquad (5.10)
$$

$$
\mathbf{d} = \begin{bmatrix} \mathbf{g}[t-1] \\ \mathbf{g}[t-1] - t \left\{ \left[(\mathbf{\psi} \otimes \mathbf{1}_U^{\mathrm{T}}) \odot \mathbf{I}_U \right] \mathbf{1}_U \right\} \\ \mathbf{1}_{KB} \\ \mathbf{0}_{UB} \\ \mathbf{0}_{UB} \\ \mathbf{0}_{UB} \\ \mathbf{vec} \left[\mathbf{L} \right] \end{bmatrix}
$$
 and (5.11)

$$
\mathbf{e} = \left\{ \mathbf{1}_{UKB}^{\mathrm{T}} - \mathbf{1}_{N}^{\mathrm{T}} \left[(\mathbf{1}_{K} \otimes \Lambda \otimes \mathbf{1}_{U}) \odot (\Lambda \otimes \mathbf{1}_{UB}) \right]^{\mathrm{T}} \right\} \mathbf{A}.
$$
 (5.12)

The solution of [\(5.9\)](#page-63-7) allocates [RBs](#page-11-4) in a way that maximizes the minimum throughput in the system and at the same time keeps all the [UEs](#page-12-0) satisfied. Indirectly, it also associates [UEs](#page-12-0) to [BSs.](#page-10-3) To do so, it requires the knowledge of $h_{u,k,b}[t]$, $\forall u \in \mathcal{U}$ $\forall u \in \mathcal{U}$ $\forall u \in \mathcal{U}$, $k \in \mathcal{K}$ $k \in \mathcal{K}$ $k \in \mathcal{K}$ and $b \in \mathcal{B}$ $b \in \mathcal{B}$ $b \in \mathcal{B}$ at each [TTI](#page-11-23) t. As already stated, this incurs in a huge signaling overhead and is computationally intensive. Thus in the next section, we present a distributed framework in order to reduce the required complexity to allocate resources in a ultra-dense heterogeneous scenario.

5.5 Proposed Distributed Framework

The proposed framework splits [\(5.4\)](#page-62-4) into two parts: a [BS](#page-10-3) selection procedure and a resource assignment. Sections [5.5.1](#page-65-1) and [5.5.2](#page-67-0) describe the [BS](#page-10-3) selection and the resource assignment procedures, respectively.

5.5.1 [BS](#page-10-3) Selection

The [BS](#page-10-3) selection procedure is sketched in the flowchart of Fig. [5.1](#page-66-0) and its pseudo code is presented in Alg. [5.1.](#page-67-1) Each [UE](#page-12-0) executes this method for each [RAT](#page-11-19) in order to choose the [BS](#page-10-3) that fits with its channel propagation conditions.

The first step, block (1) of Fig. [5.1](#page-66-0) and l. [1](#page-67-1) of Alg. [5.1,](#page-67-1) consists in selecting as candidate [BSs](#page-10-3) to a handover the ones with [RSRP](#page-11-12) greater than or equal to a threshold. If there is no [BS](#page-10-3) satisfying this requirement, the [UE](#page-12-0) will stay disconnected of this [RAT,](#page-11-19) block (3.a) and l. [3.](#page-67-1) On the other hand, if this set is not empty, the [UE](#page-12-0) will select as the best candidate [BS](#page-10-3) to connect to, block (4) and l. [17,](#page-67-1) the BS \hat{b} which maximizes the product $f_{h,1}^{\text{norm}}$ $\lim_{b,1} f_{b,2}$ $_{b,2}^{1,10}$, where $f_{h,i}^{\text{norm}}$ $\sum_{b,i}^{\text{norm}} = \frac{f_{b,i}}{\sum_{b \in \hat{\mathcal{B}}}}$ $J_{b,i}^{(j)}$, $\forall i \in \{1,2\}, f_{b,1} = RSRP_b$ $\forall i \in \{1,2\}, f_{b,1} = RSRP_b$ $\forall i \in \{1,2\}, f_{b,1} = RSRP_b$ and $f_{b,2} = \min(\theta_u[t-1])$, for all [UE](#page-12-0) u connected to [BS](#page-10-3)

b. The metric $f_{b,1}$ reflects the [BSs'](#page-10-3) signal strength, while $f_{b,2}$ is the lowest [UE](#page-12-0) throughput among all the [UEs](#page-12-0) connected to [BS](#page-10-3) b .

As presented in Chapter [3,](#page-45-0) if the [UEs](#page-12-0) consider only the [BSs'](#page-10-3) [RSRP](#page-11-12) as a criterion to connect to, the [BSs](#page-10-3) with better propagation conditions will be overloaded and a high signal strength will not result in higher transmission rates. This is the reason why a [UE](#page-12-0) should also take $f_{b,2}$ into account when selecting a [BS.](#page-10-3) For a given [BS](#page-10-3) b, if $f_{b,2}$ is low it means that at least

	1: $\hat{\mathcal{B}} \leftarrow \{b \mid b \in \mathcal{B}, \text{RSRP}_b \geq \text{threshold}\}\$	
	2: if $\hat{\mathcal{B}} = \emptyset$ then	\triangleright Test if $\hat{\mathcal{B}}$ is empty
3:	$\xi_{u,b} \leftarrow 0, \forall b \in \mathcal{B}$	► Stay disconnected
4: else		
5:	for $b \in \hat{\mathcal{B}}$ do	
6:	$f_{b,1} \leftarrow RSRP_b$	\triangleright $f_{b,1}$ reflects the BSs' signal strength
7:	$f_{b,2} \leftarrow \min_{\forall}$ UE u connected to $b(\theta_u[t-1])$	
8:	end for	
9:	$f_1^{\text{sum}} \leftarrow \sum_{b \in \hat{\mathcal{B}}} f_{b,1}$	
10:	$f_2^{\text{sum}} \leftarrow \sum_{b \in \hat{\mathcal{B}}} f_{b,2}$	
11:	for $b \in \hat{\mathcal{B}}$ do	
12:	for $i \in \{1, 2\}$ do	
13:	$f_{b,i}^{\text{norm}} \leftarrow \frac{f_{b,i}}{f^{\text{sum}}}$	\triangleright Normalization of $f_{b,i}$
14:	end for	
15:	$F_b = f_{b,1}^{norm} f_{b,2}^{norm}$	
16:	end for	
17:	$\hat{b} \leftarrow \arg \max \{F_b\}$	► Best candidate to a handover
	$b \in \hat{\mathcal{B}}$	
18:	if $RSRP_{h^*}$ < threshold then	► Verify the RSRP of the current BS
19:	$\xi_{u,\hat{b}} \leftarrow 1$	\triangleright Connect to \hat{b}
20:	else	
21:	if $(\xi_{u,b^*}[i] = 1, \forall i \in [t - T^*, t - 1])$ &	
	$\left(\hat{b}[i] = \hat{b}, \forall i \in [t - \hat{T} + 1, t - 1]\right)$ then	
22:	$\xi_{u,\hat{b}} \leftarrow 1$	\triangleright Connect to \hat{b}
23:	else	
24:	$\xi_{u,b^*} \leftarrow 1$	\triangleright Stay connected to the current BS, b^*
25:	end if	
26:	end if	

Algorithm 5.1 Pseudo code of proposed [BS](#page-10-3) selection procedure.

one [UE](#page-12-0) connected to [BS](#page-10-3) *b* has a low throughput. This may indicate for a UE looking for a BS to connect to that if it tries to handover to [BS](#page-10-3) b it may also experience a low throughput. On the other hand, if $f_{b,2}$ is high, it means that all the [UEs](#page-12-0) connected to it have high throughput. Thus, this [BS](#page-10-3) may be a good candidate in order to get a high throughput.

Before a handover, a [UE](#page-12-0) must stay connected to the current [BS](#page-10-3) b^* for at least T^* [TTIs,](#page-11-23) and the candidate [BS](#page-10-3) to the handover, \hat{b} , must have been selected as the best candidate for at least \hat{T} consecutive [TTIs,](#page-11-23) block (6) and l. [21.](#page-67-1) Otherwise, it must stay connected to b^* , block (7.b) and 1. [24.](#page-67-1) However, if the [RSRP](#page-11-12) of b^* is lower than a given threshold, block (5) and l. [18,](#page-67-1) an [UE](#page-12-0) is allowed to connect to \hat{b} even if the constraints in block (6) and l. [21](#page-67-1) are not satisfied.

5.5.2 Resource Assignment

27: end if

The proposed resource assignment is described in the flowchart of Fig. [5.2](#page-69-1) and its pseudo code is presented in Alg. [5.2.](#page-68-0) This algorithm should be executed independently by each [BS.](#page-10-3) Its main idea is first to keep all the [UEs](#page-12-0) satisfied and after, if there is still available [RBs,](#page-11-4) allocate them to the [UEs](#page-12-0) with lower throughput in order to increase the minimum throughput in the system. It is divided into three parts:

	μ algorithm $\sigma = 1$ scaled code of resource assignment procedure.	
	1: $\mathbf{X} \leftarrow \mathbf{0}_{\mathcal{U}_b \times K_n}$	\triangleright Initialize the allocation matrix
	2: $RB_{\text{free}} \leftarrow K_n$	\triangleright Initialize the number of unassigned RBs
	3: $\mathcal{U}_b \leftarrow \{u \mid u \in \mathcal{U}, \xi_{u,b} = 1\}$	
	4: for $u \in \mathcal{U}_b$ do	
	5: if $\theta_u[t] \ge \psi_u$ then	
	6: $\mathcal{U}_b \leftarrow \mathcal{U}_b \setminus \{u\}$	Remove UE u from \mathcal{U}_b
7:	end if	
	8: end for	
	9: while $(\mathcal{K}_n \neq \emptyset \& \mathcal{U}_b \neq \emptyset)$ do	
10:	$(\widehat{u}, k) \leftarrow \arg \max \{r_{u,k,b}\}\$	
	$u \in \mathcal{U}_b, k \in \mathcal{K}_n$	
11:	$x_{\widehat{u},\widehat{k},b} \leftarrow 1$	Assign RB \hat{k} to UE \hat{u}
12:	$\theta_{\widehat{u}}[t] \leftarrow \frac{t\theta_{\widehat{u}}[t] + r_{\widehat{u},\widehat{k},b}}{t}$	\triangleright Update the throughput of UE \widehat{u}
	13: $\mathcal{K}_n \leftarrow \mathcal{K}_n \setminus \{k\}$	Remove RB \vec{k} from the set of RBs, \mathcal{K}_n
14:	if $\theta_{\widehat{u}}[t] \geq \psi_{\widehat{u}}$ then	\triangleright Test if UE \widehat{u} is satisfied
15:	$\mathcal{U}_b \leftarrow \mathcal{U}_b \setminus \{u\}$	Remove UE \widehat{u} from \mathcal{U}_b
16:	end if	
	17: end while	
	18: if $K \neq \emptyset$ then	
19:	$\mathcal{U}_b \leftarrow \{u \mid u \in \mathcal{U}, \xi_{u,b} = 1\}$	\triangleright Reinitialize the set \mathcal{U}_b with all UEs connected to BS b
20:	while $\mathcal{K}_n \neq \emptyset$ do	
21:	$u^* \leftarrow \arg\min\{\theta_u[t]\}$	
	$u \in \mathcal{U}_h$	
22:	$k^* \leftarrow \underset{k \in \mathcal{K}_n}{\arg \max} \left\{ r_{u^*,k,b} \right\}$	
23:	$x_{u^*,k^*,b} \leftarrow 1$	\triangleright Assign RB k^* to UE u^*
24:	$\theta_{u^*}[t] \leftarrow \frac{t\theta_{u^*}[t]+r_{u^*,k^*,b}}{t}$	\triangleright Update the throughput of UE \widehat{u}
25:	$\mathcal{K}_n \leftarrow \mathcal{K}_n \setminus \{k^*\}$	Remove RB k^* from \mathcal{K}_n
26:	end while	
	$27:$ end if	

Algorithm 5.2 Pseudo code of resource assignment procedure.

- 1. Exclude satisfied [UEs,](#page-12-0) blocks (1)-(3) and ll. [4-8;](#page-68-0)
- 2. Satisfy [UEs,](#page-12-0) blocks (4)-(9) and ll. [9-17;](#page-68-0) and
- 3. Max. min. throughput, blocks (10)-(13) and ll. [18-27.](#page-68-0)

The first part consists in excluding the [UEs](#page-12-0) that are already satisfied, i.e., $\theta_u[t] \ge \psi_u$. For this, each [UE](#page-12-0) must inform the [BSs](#page-10-3) to which it is connected (it may be more than one, e.g., one per [RAT\)](#page-11-19), its current throughput. The [UE](#page-12-0) must take into account all the data that it has already received, no matter the [RAT](#page-11-19) from which it came from.

The second part tries to satisfy the [UEs](#page-12-0) not yet satisfied. It works in a loop, allocating [RBs](#page-11-4) to the [UEs](#page-12-0) with highest transmit rate on each [RB,](#page-11-4) blocks (4)-(5) and ll. [10-11.](#page-68-0) When a [UE](#page-12-0) gets satisfied, it is removed, block (7) and ll. [14-16.](#page-68-0) This loop continues until all the [RBs](#page-11-4) have been allocated, block (8), or all the [UEs](#page-12-0) are satisfied, block (9) and l. [9.](#page-68-0)

In the last part, the remaining [RBs](#page-11-4) are allocated to the [UEs](#page-12-0) with lowest throughput, block (11) and l. [21,](#page-68-0) aiming at maximizing the minimum throughput.

Figure 5.2 – Flowchart of proposed resource assignment procedure.

Source: Created by the author.

5.6 Practical Implementation Considerations

In order to provide to the readers a practical view of our proposal, we illustrate how our framework can be mapped into [3GPP](#page-10-0) network parameters and how they can be obtained. In order to execute a [BS](#page-10-3) selection, each [UE](#page-12-0) needs to know:

• [RSRP](#page-11-12) of candidate [BSs](#page-10-3) — The [UE](#page-12-0) can locally monitor the signal strength. This procedure is already standardized in [LTE](#page-10-9) and in [5G](#page-10-1) [NR;](#page-11-9)

• Lowest [UE](#page-12-0) throughput in each [BS](#page-10-3) — Each UE must periodically inform its throughput to the [BSs](#page-10-3) to which it is connected, and, after that, each [BS](#page-10-3) must broadcast the lowest throughput among the [UEs](#page-12-0) connected to it.

Regarding the resource allocation procedure, each [BS](#page-10-3) needs:

- Throughput requirement of [UEs](#page-12-0) connected to it From the network operators' point of view, usually the throughput requirement of a [UE](#page-12-0) is associated with the service it is using and/or its data plan, which can be available for the [BSs,](#page-10-3) since the operators have access to these information;
- Throughput of [UEs](#page-12-0) connected to it This information was already listed as a requirement in order to execute the [BS](#page-10-3) selection and must be informed by the [UEs](#page-12-0) to the [BSs](#page-10-3) to which they are connected;
- [CQI](#page-10-5) of [UE](#page-12-0) connected to it In [LTE,](#page-10-9) this information is already standardized. The [UEs](#page-12-0) monitor the received signal strength of the connected [BSs](#page-10-3) and report back the measured [CQI.](#page-10-5)

5.7 Complexity Analysis

In this section, we provide the worst-case computational complexity of the centralized benchmark and of the proposed framework. It gives an upper bound on the computational resources required by an algorithm and is represented by the asymptotic notation $O(\cdot)$ $O(\cdot)$. As in [\[75\]](#page-96-3), we consider summations, multiplications and comparisons as the most relevant and time-consuming operations.

The solution of [\(5.9\)](#page-63-7) can be obtained using the [Branch and Bound](#page-10-24) [\(BB\)](#page-10-24) algorithm. According to $[76]$, to solve a linear programming problem with c constraints and v integer variables, the number of required operations is $2(v+c)(2vc+v-3c)\sqrt{2^v}$. In [\(5.9\)](#page-63-7), $v = 1 + UKB + UB$ and $c = 2U + KB + 2UB + UN + 1$, thus its complexity is $O\left(\frac{U^2K^2B^2(UB + UN + 1)}{U^2K^2B^2(UB + UN + 1)}\right)$ $KB)+U^3KBN^2$ $\sqrt{2^{1+UB(K+1)}}$. On the other hand, the complexity of the proposed framework is $O(UK^2)$ $O(UK^2)$. The detailed analysis to obtain this value is presented in Appendix [A.](#page-98-0) Comparing both complexities, it can be concluded that the proposed framework can better handle large-scale scenarios, which is a key feature of [5G](#page-10-1) multi[-RAT](#page-11-19) multi-connectivity systems.

5.8 Performance Evaluation

In this section, the performance of the proposed distributed framework is evaluated via simulation. Subsection [5.8.1](#page-71-0) presents the considered scenario and the benchmark solutions. Subsection [5.8.2](#page-72-0) presents and discusses the results.

Figure 5.3 – Illustration of a [5G](#page-10-1) multi[-RAT](#page-11-19) multiconnectivity scenario, where the [LTE](#page-10-9) [BS](#page-10-3) acts as an umbrella cell and [NR](#page-11-9) [BSs](#page-10-3) act as hotspots. The [BSs](#page-10-3) are connected to a centralized processing unit, which is responsible for coordinating the resource usage by the [BSs.](#page-10-3) [UEs](#page-12-0) with [DC](#page-10-13) capability may simultaneously connect to [BSs](#page-10-3) of both [RATs](#page-11-19) when inside their coverage area.

Source: Created by the author.

5.8.1 Simulation Assumptions

The scenario considered in the performance evaluation was aligned with the [3GPP](#page-10-0) specifications. More specifically, we considered a downlink [5G](#page-10-1) multi[-RAT](#page-11-19) network based on the dense urban scenario proposed in [\[70\]](#page-95-11). It focused on macro [LTE](#page-10-9) [BSs](#page-10-3) with micro [NR](#page-11-9) [BSs.](#page-10-3) The [LTE](#page-10-9) [BSs](#page-10-3) were deployed in a hexagonal grid with 3 sectors per site, while the [NR](#page-11-9) [BSs](#page-10-3) were randomly deployed (one [NR](#page-11-9) [BS](#page-10-3) per [LTE](#page-10-9) sector). The [LTE](#page-10-9) [BSs](#page-10-3) acted as umbrella cells ensuring coverage to the system, while the [NR](#page-11-9) [BSs](#page-10-3) acted as hotspots ensuring high values of throughput, as illustrated in Fig. [5.3.](#page-71-1) For this purpose, the chosen [LTE](#page-10-9) carrier frequency was 3.50 GHz with 20 MHz of system bandwidth and 49 dBm of transmit power [\[77\]](#page-96-5). On the other hand, the chosen [NR](#page-11-9) carrier frequency was 28 GHz with 100 MHz of system bandwidth and 35 dBm of transmit power [\[71\]](#page-95-12).

Concerning the [NR](#page-11-9) physical layer, as in [LTE,](#page-10-9) the [NR](#page-11-9) [RB](#page-11-4) consisted of 12 subcarriers and 14 [OFDM](#page-11-5) symbols. However, the subcarrier spacing and the [TTI](#page-11-23) were different. In [LTE](#page-10-9) they were equal to 15 kHz and 1 ms, respectively, while in [NR,](#page-11-9) they were equal to 60 kHz and 0.25 ms, respectively [\[56\]](#page-94-0).

The [QUAsi Deterministic RadIo channel GenerAtor \(QuaDRiGa\)](#page-11-24) [\[78\]](#page-96-6) was used for the generation of channel samples. It generates 3D spatial and temporal consistent channel samples considering large and small-scale fading. The [LTE](#page-10-9) channel samples were generated according to the model standardized in [\[77\]](#page-96-5). Concerning the [NR](#page-11-9) channel model, it was adopted the one proposed by the [mmMAGIC](#page-11-25) project in [\[79\]](#page-96-7). As in [\[80\]](#page-96-8), for [NR,](#page-11-9) it was considered 3D antenna beamforming with high directive gain, 24.50 dB, and narrow beam width, 10.90° [Half Power Beamwidth \(HPBW\)](#page-10-25) in the azimuth plane. Ideal beam selection and beam tracking
procedures were assumed. Tables [5.1](#page-72-0) and [5.2](#page-73-0) present an extensive list of the adopted simulation parameters.

The solution of [\(5.9\)](#page-63-0) was used as an upper bound and was obtained with the IBM ILOG CPLEX Optimizer [\[83\]](#page-96-0). Only its feasible snapshots were considered.

The cross-carrier [Proportional Fairness \(PF\)](#page-11-1) [\[84\]](#page-96-1) was also used as benchmark. It tries to maximize the system throughput, while allowing all [UEs](#page-12-0) to have at least a minimal throughput. The scheduled [UE](#page-12-0) u^* on [RB](#page-11-2) k in [BS](#page-10-1) b at [TTI](#page-11-3) t is determined as:

$$
u^* = \underset{u \in \mathcal{U}_b}{\arg \max} \left\{ \frac{r_{u,k,b}[t]}{g_u[t-1]} \right\}.
$$
 (5.13)

5.8.2 Numerical Results

First of all, in order to analyze the coverage of [LTE](#page-10-2) and [NR](#page-11-4) [BSs,](#page-10-1) for each [UE](#page-12-0) and [RAT,](#page-11-5) we considered the strongest [SNR](#page-11-6) among all the possible [UE-](#page-12-0)[BS](#page-10-1) links. We highlight that, even the [UEs](#page-12-0) that were not connected to a [BS](#page-10-1) of a given [RAT,](#page-11-5) because even their best link to a [BS](#page-10-1) of this [RAT](#page-11-5) was lower than a given threshold, were considered in this analysis. Fig. [5.4](#page-73-1) presents the [CDF](#page-10-3) of these values. Considering −5 dB as the minimum [SNR](#page-11-6) allowing a [UE](#page-12-0) to connect to a [BS,](#page-10-1) according to the [MCSs](#page-10-4) curves in [\[67\]](#page-95-0), we can see that all the [UEs](#page-12-0) were covered by a [LTE](#page-10-2) [BS,](#page-10-1) since, for all [UEs,](#page-12-0) their best link was higher than −5 dB. On the other hand, for 20 % of the [UEs,](#page-12-0) even their best link to a [NR](#page-11-4) [BS](#page-10-1) was not enough to connect them to a [NR](#page-11-4) [BS,](#page-10-1) i.e., 20 % of the [UEs](#page-12-0) were not inside a [NR](#page-11-4) [BS](#page-10-1) coverage area. This validates the scenario as a macro layer, [LTE](#page-10-2) [RAT,](#page-11-5) acting as an umbrella and the micro layer, [NR](#page-11-4) [RAT,](#page-11-5) as hotspots.

Fig. [5.5](#page-74-0) presents the impact of the number of [UEs](#page-12-0) on the minimum throughput. For $U > 30$, there were no feasible solutions for the centralized benchmark, thus the presented results concern $U < 30$.

For $U \leq 20$, the proposed distributed framework performed nearly equal to the centralized solution requiring less computational effort and signaling overhead. By interpolation, we find that, for $U > 16$, [PF](#page-11-1) was not able to keep all the [UEs](#page-12-0) satisfied, i.e., with a throughput higher than 20 Mbps, while our proposal was able to keep at least 21 [UEs](#page-12-0) simultaneously satisfied.

Parameter	Value
UE distribution	Uniform in the macro layer
UE height	$1.50 \,\mathrm{m}$
UE speed	5 km/h
UE service profile	Full buffer
UE requirement (ψ_u)	20 Mbps
UE capabilities $(l_{u,n})$	1 LTE Rx and 1 NR Rx
Min. num. of snapshots	35
Confidence interval	95%

Table 5.1 – Common simulation parameters for both [RATs.](#page-11-5)

Source: Created by the author.

Parameter	LTE	NR	Ref.'s ^a
Layout	Macro layer: 1 hexagonal site	Micro layer: 1 randomly	$[70]$
Scenario	with 3 sectors 3GPP 3D Urban Macro	dropped NR BS per LTE sector mmMAGIC initial Urban Micro 10-80	$[77]$, $[79]$
Inter-site distance	500 m		$[77]$
BS height	$25 \,\mathrm{m}$	10 _m	[77], [71]
Carrier frequency	3.50 GHz	28 GHz	[77], [71]
System bandwidth	$20 \,\mathrm{MHz}$	$100 \,\mathrm{MHz}$	$[77]$, $[71]$
Subcarrier spacing	15 kHz	60 kHz	$[81]$, $[56]$
Num. of RBs (K_n)	100	125	$[82]$, $[56]$
TTI	1 ms	0.25 ms	$[81]$, $[56]$
Noise figure	9 dB	9dB	$[71]$
BS Tx power (P_n)	49 dBm	35 dBm	[77], [71]
Tx antenna type	3GPP 3D	Narrow beam (HPBW = 10.90°) and directivity gain $= 24.50$ dB)	$[77]$, $[80]$

Table 5.2 – Simulation parameters for [LTE](#page-10-2) and [NR.](#page-11-4)

^a Whenever two references appear, the first refers to [LTE](#page-10-2) and the second to [NR.](#page-11-4) Also, only one reference refers to both [RATs.](#page-11-5)

Source: Created by the author.

Figure 5.4 – [SNR](#page-11-6) of the [UEs'](#page-12-0) best link. For each [RAT,](#page-11-5) we considered the strongest [SNR](#page-11-6) among all the possible [UE](#page-12-0)[-BS](#page-10-1) links. Notice, in the [NR](#page-11-4) curve, that 20 % of the cases were lower than −5 dB meaning that for 20 % of the [UEs,](#page-12-0) even their best link was not enough to connect them to a [NR](#page-11-4) [BS,](#page-10-1) i.e., 20 % of the [UEs](#page-12-0) were not inside a [NR](#page-11-4) [BS](#page-10-1) coverage area.

Source: Created by the author.

Figure 5.5 – Minimum [UE](#page-12-0) throughput.

Source: Created by the author.

This means an increase of 31 % in the system's capacity. For $U = 16$, our proposal increased the minimum [UE](#page-12-0) throughput in 38 %, from 20.80 Mbps to 28.70 Mbps.

Note that, the proposed resource assignment, Fig. [5.2,](#page-69-0) tries to satisfy all the [UEs](#page-12-0) before maximizing the minimum throughput. Thus, when it can not satisfy all the [UEs,](#page-12-0) it prioritizes satisfying as much [UEs](#page-12-0) as possible rather than maximizing the minimum throughput. Therefore, for $U > 25$, our proposal has lower minimum throughput than the [PF.](#page-11-1) This is a trade-off that needs to be implemented in scenarios with high number of [UEs.](#page-12-0)

This trade-off can also be seen in Fig. [5.6.](#page-75-0) It presents the outage and the Jain's index in function of the number of [UEs,](#page-12-0) where the outage is the percentage of not satisfied [UEs](#page-12-0) and the Jain's fairness index measures the fairness among the [UEs](#page-12-0) throughput, i.e., $\Delta = \frac{\sum_{u=1}^{U} \theta_u^2}{\sum_{v=1}^{U} \theta_v^2}$ $\frac{(\sum_{u=1}^U c_u)}{U \sum_{u=1}^U (\theta_u)^2}$. The outage of [PF](#page-11-1) is always higher than the one of the proposed framework, even for $U > 25$ (when its minimum throughput is lower), this is due to the trade-off already explained.

Sometimes it is difficult to keep the throughput of [UEs](#page-12-0) only connected to [LTE](#page-10-2) [BSs](#page-10-1) as high as that of [UEs](#page-12-0) connected to both [RATs.](#page-11-5) When the number of [UEs](#page-12-0) increased from 5 to 20, the Jains' index of the proposed framework also raised, since this increased the competition for [NR](#page-11-4) [RBs,](#page-11-2) decreasing the throughput of [UEs](#page-12-0) in [DC](#page-10-6) and approximating it to the one achieved by the [UEs](#page-12-0) only connected to [LTE.](#page-10-2) For these loads, the Jains' index of the centralized benchmark was equal to 100 %. The Jains' index of the proposed framework was close to this value, but not equal, since not all [UEs](#page-12-0) were satisfied.

Concerning the Jains' index of the [PF,](#page-11-1) it was clearly lower than the one of our proposal. Ideally, it should exploit multi-user diversity while maintaining fairness. However, the fairness is not achieved. This problem is highlighted in Fig. [5.7,](#page-76-0) which presents the 50 %-ile

Figure 5.6 – Outage and Jain's index.

Source: Created by the author.

and 90 %-ile [UEs](#page-12-0) throughput. The unfair scheduling of [PF](#page-11-1) can be seen in the high difference between the throughput of these percentiles, even when the system is overloaded ($U = 30$).

[5G](#page-10-0) networks are expected to be deployed in high frequencies, where the propagation conditions are challenging, e.g., higher path loss and lower diffraction. Thus, the [UEs](#page-12-0) may experience channels with very different quality, as shown in Fig. [5.4,](#page-73-1) where the [NR](#page-11-4) [SNR](#page-11-6) varies from −20 dB to 30 dB (from a very poor to a very good quality). In such scenarios, since [PF](#page-11-1) is opportunistic, it may schedule [UEs](#page-12-0) with better channel quality even if they have high throughput, keeping [UEs](#page-12-0) with poor channel quality in starvation. In other words, for [PF,](#page-11-1) the good channel experienced by some [UEs](#page-12-0) compensates their high throughput in [\(5.13\)](#page-72-1), given to them priority to be scheduled. That is why, in Fig. [5.7,](#page-76-0) we have the large difference between the 50 %-ile and the 90 %-ile throughput.

The behavior of [PF](#page-11-1) not scheduling the [UEs](#page-12-0) with worst channel in [NR](#page-11-4) is illustrated in Fig. [5.8.](#page-76-1) This figure presents the [CDF](#page-10-3) of the [SNR](#page-11-6) related to the scheduled [UEs](#page-12-0) in each [RAT.](#page-11-5) In [NR,](#page-11-4) we can see that centralized benchmark and our proposal were able to schedule [UEs](#page-12-0) in a larger range of [SNR](#page-11-6) than [PF.](#page-11-1) Regarding [LTE,](#page-10-2) the behavior of [PF](#page-11-1) was similar to the one of the centralized benchmark and of our proposal, allocating all [UEs.](#page-12-0) This is due to the fact that, in [LTE,](#page-10-2) the difference of channel quality among the [UEs](#page-12-0) is not so large as it is in [NR,](#page-11-4) as it can be seen in Fig. [5.4.](#page-73-1)

In Chapter [3,](#page-45-0) it was concluded that it might be interesting to consider frameworks that could select between single connection and [DC](#page-10-6) according to the system load. When the load is high and the [UEs](#page-12-0) try to connect to more than one [BS](#page-10-1) at the same time, the network becomes highly interference-limited and the system performance decreases very fast. Thus, not all the

Figure 5.7 – 50 %-ile and 90 %-ile of [UEs'](#page-12-0) throughput.

Source: Created by the author.

Figure 5.8 – [SNR](#page-11-6) of scheduled [UEs](#page-12-0) per [RAT.](#page-11-5)

Source: Created by the author.

Source: Created by the author.

[UEs](#page-12-0) will benefit from the larger transmission bandwidth offered by [DC.](#page-10-6) A balance between load and number of [UEs](#page-12-0) in [DC](#page-10-6) needs to be found.

Our proposed framework already takes this balance into account, as it can be seen in Fig. [5.9.](#page-77-0) This figure presents the percentage of connected [UEs](#page-12-0) which were in [DC](#page-10-6) as a function of the number of [UEs](#page-12-0) in the system. The complementary of this percentage represents the [UEs](#page-12-0) in single connection. In low loads, the majority of the [UEs](#page-12-0) were in [DC](#page-10-6) mode. The single connection [UEs](#page-12-0) were mainly the ones which were not in the coverage area of a [NR](#page-11-4) [BS.](#page-10-1) When the load increased, in order to maintain the system's performance, the percentage of [UEs](#page-12-0) in [DC](#page-10-6) decreased for the three considered solutions. However, for [PF](#page-11-1) this reduction was higher than for the others. It decreased more than the necessary, if we consider the behavior of the centralized benchmark as the optimal one.

5.9 Chapter Summary

The present chapter focused on managing radio resources in a multi[-RAT](#page-11-5) scenario. More specifically, an optimization problem was formulated in order to maximize the minimum [UE](#page-12-0) throughput in the system subject to the constraint that all users must be satisfied. The referred problem is non-linear and hard to solve. However, we got to transform it into a simpler form, a [MILP,](#page-10-7) that can be optimally solved using standard numerical optimization methods. It was also proposed a distributed framework to overcome the drawbacks of centralized processing. It is divided into two parts: a [BS](#page-10-1) selection procedure (performed independently by each [UE\)](#page-12-0) and a resource assignment algorithm (performed independently by each [BS\)](#page-10-1). Besides, a performance evaluation was conducted, considering [Fourth Generation \(4G\)](#page-10-8) [LTE](#page-10-2) and [5G](#page-10-0) [NR](#page-11-4) system

parameters.

The proposed solution outperforms a cross-carrier [PF,](#page-11-1) as well as, it performs close to the benchmark solution. Compared to [PF,](#page-11-1) our proposal improves by 31 % the system's capacity and by up to 38 % the minimum throughput in the system. Regarding the benchmark solution, our proposal requires less computation effort and less signaling overhead. The analyses also showed that the proposed framework tries to avoid the system overload by decreasing the percentage of [UEs](#page-12-0) in [DC](#page-10-6) mode when the number of [UEs](#page-12-0) increases.

6 RESOURCE ALLOCATION IN [5G:](#page-10-0) COMPLEXITY AND RELIABILITY AS-**PECTS**

Continuing the study of [5G](#page-10-0) multi[-RAT](#page-11-5) scenarios and [CH](#page-10-9) occurrence, the present chapter focuses on the implications of these topics on the adopted [KPIs](#page-10-10) and [RRA](#page-11-8) algorithms.

More specifically, three different [RRAs](#page-11-8) and three different [KPIs](#page-10-10) were considered in the analyses. Regarding reliability, [DC](#page-10-6) and [FS](#page-10-11) performances were compared. Concerning complexity, it was evaluated a proposed method that optimizes [CQI](#page-10-12) measurements and reporting based on the occurrence of [CH.](#page-10-9)

Before addressing the evaluations themselves, next section presents the proposed method for [CQI](#page-10-12) measurement and reporting optimization.

6.1 [CQI](#page-10-12) Measurement and Reporting Optimization Based on [CH](#page-10-9) Occurrence

As already presented, due to the higher diversity of possible links (Tx-Rx beam pairs) over a wider bandwidth, the amount of [CQIs](#page-10-12) being reported by the [UEs](#page-12-0) might increase the complexity of [RRA.](#page-11-8) Thus, new approaches need to be adopted to avoid the increase in [RRA](#page-11-8) complexity as the number of antennas increases and the bandwidth enlarges.

Since [CH](#page-10-9) may reduce channel fluctuations, [CQI](#page-10-12) [RBs](#page-11-2) may have similar values. Thus, it will not be worth the effort to measure and report all of them. In this context, we propose a method in which is up to the [UE](#page-12-0) to identify when [CH](#page-10-9) is happening and inform this to its serving [BS,](#page-10-1) so it can take advantage of it.

The first step of the proposed method is illustrated in Fig. [6.1.](#page-80-0) A [UE](#page-12-0) performs measurements to derive the channel quality in all configured pairs of [RBs](#page-11-2) and beams (the colored squares in the figure). Then, the UE estimates the correlation of these pairs. If the correlation is high for a subset of beams and [RBs](#page-11-2) (squares with the same color in the figure), meaning that the channel has been hardened in this subset, the [UE](#page-12-0) will select a pair beam[-RB](#page-11-2) as representative of the subset and will report to the [BS](#page-10-1) only the [CQI](#page-10-12) of this pair. Besides, it needs to report a single bit indicating that there is [CH](#page-10-9) along with the bits informing the list of beams and [RBs](#page-11-2) to which this report corresponds.

As illustrated in Fig. [6.2,](#page-80-1) for each set of pairs beam[-RB](#page-11-2) in which the [UE](#page-12-0) detects the [CH,](#page-10-9) the [UE](#page-12-0) will still measure the [CQI](#page-10-12) of all pairs beam[-RB](#page-11-2) of these sets during the next X' ' measurement periods. If [CH](#page-10-9) is detected during these X' ' measurement periods, for the next measurement periods, the [UE](#page-12-0) is allowed to measure only the [CQI](#page-10-12) of the representative pair. The other pairs will still be measured, but with a longer periodicity to verify whether [CH](#page-10-9) is still happening or not.

Figure 6.1 – Proposed [CQI](#page-10-12) reporting optimization based on [CH](#page-10-9) occurence.

Source: Created by the author.

Figure 6.2 – Proposed [CQI](#page-10-12) measurement optimization based on [CH](#page-10-9) occurence.

Source: Created by the author.

Figure 6.3 – [5G](#page-10-0) multi[-RAT](#page-11-5) scenario.

6.2 Performance Evaluation

6.2.1 Simulation Assumptions

As illustrated in Fig. [6.3,](#page-81-0) this chapter considers co-sited [LTE](#page-10-2) and [NR](#page-11-4) [BSs.](#page-10-1) When not explicitly defined, the [LTE](#page-10-2) antennas cover areas of 120°, while six 8×8 [NR](#page-11-4) antenna arrays cover areas of 60° each. Besides, each [NR](#page-11-4) antenna array is connected to one analog beamformer. The [LTE](#page-10-2) and [NR](#page-11-4) [RATs](#page-11-5) are responsible for ensuring coverage and high throughput, respectively. To this purpose, the chosen [LTE](#page-10-2) carrier frequency is 2 GHz with 10 MHz of system bandwidth and 46 dBm of transmit power. On the other hand, the chosen [NR](#page-11-4) carrier frequency is 28 GHz with 20 MHz of system bandwidth and 28 dBm of transmit power.

Concerning the physical layer, the configuration presented in Section [2.3](#page-32-0) was adopted. In [LTE,](#page-10-2) the minimum scheduling unit is a subframe consisting of two [RBs,](#page-11-2) i.e., 14 [OFDM](#page-11-9) symbols spanning over 1 ms and 12 subcarriers with subcarrier spacing equal to 15 kHz. In [NR,](#page-11-4) the minimum scheduling unit is a slot, also consisting of 14 [OFDM](#page-11-9) symbols and 12 subcarriers, but spanning over 0.25 ms and with subcarrier spacing equal to 60 kHz. Tables [6.1](#page-82-0) and [6.2](#page-82-1) present an extensive list of the adopted simulation parameters.

As presented in [\[72\]](#page-96-7), different scheduling criteria have already been considered in the literature. They have pros and cons. Thus, three different scheduling criteria were chosen in order to analyze the possible impacts of the solutions used to address the challenges presented in the previous section. They are:

- *Max-rate*: maximizes the system throughput;
- *[PF](#page-11-1)*: schedules the [UE](#page-12-0) that maximizes the ratio between [CQI](#page-10-12) and the amount of already received bits;
- *Satisfaction oriented*: first maximizes the number of satisfied [UEs,](#page-12-0) and, after, allocates remaining unscheduled resources to the [UEs](#page-12-0) with minimum throughput.

Parameter	LTE	NR	$Ref.'s^b$
Layout	Macro layer: 1 site with 3 sec-	Micro layer: 1 site with 6 sec-	[70]
	tors	tors	
Scenario	3GPP 3D Urban Macro	mmMAGIC initial Urban Mi-	$[77]$, $[79]$
		$\text{cro } 10\text{-}80$	
Inter-site distance	$200 \,\mathrm{m}$		$[77]$
BS height	25 m	10 _m	[77], [71]
Carrier frequency	2 GHz	28 GHz	$[77]$, $[71]$
System bandwidth	$10\,\mathrm{MHz}$	20 MHz	$[77]$, $[71]$
Subcarrier spacing	15 kHz	60 kHz	$[81]$, $[56]$
Num. of RBs	50	25	$[82]$, $[85]$
Subframe (LTE) Slot	1 ms	0.25 ms	$[81]$, $[56]$
(NR) time duration			
Noise figure	9 dB	9dB	[71]
BS Tx power	$46\,\mathrm{dBm}$	$28\,\mathrm{dBm}$	[77], [71]
Tx antenna type	3GPP 3D	3GPP 3D	$[77]$

Table 6.1 – Simulation parameters for [LTE](#page-10-2) and [NR.](#page-11-4)

^b Whenever two references appear, the first refers to [LTE](#page-10-2) and the second to [NR.](#page-11-4) Also, only one reference refers to both [RATs.](#page-11-5)

Source: Created by the author.

Table 6.2 – Common simulation parameters for both [RATs.](#page-11-5)

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In this chapter, the joint beam-frequency multiuser scheduler framework proposed in [\[86\]](#page-97-1) was adopted. For each analog beamformer in the system, it finds the optimal beam direction in order to maximize the scheduling metric. Then, for each selected beam, the scheduler allocates the [RBs](#page-11-2) to the [UEs](#page-12-0) that maximizes the contribution to the target scheduling metric. Each [UE](#page-12-0) reports a set of preferred beams indices and a [CQI](#page-10-12) vector for all the [RBs](#page-11-2) over these beams.

This framework was adopted in two different ways:

- *Centralized*: a central unit is responsible for choosing which [BS,](#page-10-1) beam and frequency [RBs](#page-11-2) will be used to serve each [UE;](#page-12-0)
- *Decentralized*: each [BS](#page-10-1) individually allocates its own resource (without coordination among them), while the [UEs](#page-12-0) are responsible for choosing the best [BS](#page-10-1) for them.

Max-rate and [PF](#page-11-1) schedulers were implemented as centralized solutions while the satisfaction oriented scheduler was implemented as a decentralized solution. This way, we could also analyze

Figure 6.4 – [SNR](#page-11-6) of the [UEs'](#page-12-0) best link. For each [RAT,](#page-11-5) we considered the strongest [SNR](#page-11-6) among all the possible [UE](#page-12-0)[-BS](#page-10-1) links. Considering −5 dB as the minimum [SNR](#page-11-6) allowing a [UE](#page-12-0) to connect to a [BS,](#page-10-1) notice that all the [UEs](#page-12-0) were covered by a [LTE](#page-10-2) [BS.](#page-10-1) On the other hand, considering [NR](#page-11-4) 8×8 arrays, the [UE](#page-12-0)[-NR](#page-11-4) best links of 20 % of the [UEs](#page-12-0) were not good enough to connect them to a [NR](#page-11-4) [BS,](#page-10-1) i.e., 20 % of the [UEs](#page-12-0) were not inside a [NR](#page-11-4) [BS](#page-10-1) coverage area. This validates the scenario as a macro layer, [LTE,](#page-10-2) acting as an umbrella and a micro layer, [NR,](#page-11-4) as hotspots.

Source: Created by the author.

these two different implementation approaches.

6.2.2 Numerical Results

First, we analyzed the coverage of [LTE](#page-10-2) and [NR](#page-11-4) [BSs.](#page-10-1) As in the previous chapter, for each [UE](#page-12-0) and [RAT,](#page-11-5) we considered the link with the strongest [SNR](#page-11-6) among all possible [UE](#page-12-0)[-BS](#page-10-1) links. Fig. [6.4](#page-83-0) presents the [CDF](#page-10-3) of these values. Assuming −5 dB as the minimum [SNR](#page-11-6) allowing a [UE](#page-12-0) to connect to a [BS,](#page-10-1) notice that all the [UEs](#page-12-0) were covered by a [LTE](#page-10-2) [BS.](#page-10-1) On the other hand, considering [NR](#page-11-4) 8×8 arrays, the [UE](#page-12-0)[-NR](#page-11-4) best links of 20 % of the [UEs](#page-12-0) were not good enough to connect them to a [NR](#page-11-4) [BS,](#page-10-1) i.e., 20 % of the [UEs](#page-12-0) were not inside a [NR](#page-11-4) [BS](#page-10-1) coverage area. This validates the scenario as a macro layer, [LTE,](#page-10-2) acting as an umbrella and a micro layer, [NR,](#page-11-4) as hotspots. Also, notice the difference of 10 dB between the curves of 2×2 and 8×8 antenna arrays. Fig. [6.5](#page-84-0) complements Fig. [6.4](#page-83-0) by presenting the [SNR](#page-11-6) heat map. When deployed with smaller arrays, the coverage of [NR](#page-11-4) was even smaller.

6.2.2.1 Complexity

As aforementioned, the [CH](#page-10-9) effect may simplify [RRA](#page-11-8) in the frequency domain. Thus, in this section we investigate how to take advantage of this and we analyze its main impact on system's [KPIs.](#page-10-10)

Fig. [6.6](#page-84-1) presents the standard deviation of [RBs](#page-11-2) [SNR.](#page-11-6) The obtained result confirms the existence of [CH.](#page-10-9) That is, the fluctuations of [RBs](#page-11-2) [SNR](#page-11-6) around the mean [SNR](#page-11-6) decrease as the number of antennas increases. This suggests that choosing the central [RB](#page-11-2) as a representative

Figure 6.5 – [SNR](#page-11-6) heat map snapshot inside a circle of radius 133.33 m.

Source: Created by the author.

Figure 6.6 – [CDF](#page-10-3) of standard deviation of [RBs](#page-11-2) [SNR.](#page-11-6) Increasing the number of antennas, the standard deviation decreases, i.e., the fluctuations of [RBs](#page-11-2) [SNR](#page-11-6) around the mean [SNR](#page-11-6) decrease, which confirms the existence of [CH](#page-10-9) in the considered scenario.

Source: Created by the author.

[RB,](#page-11-2) reporting only its [CQI](#page-10-12) and considering the others [RBs](#page-11-2) [CQI](#page-10-12) equal to the reported value may not strongly harm the system's performance. Thus, we investigated the impact of this strategy on system's performance when using the previously presented schedulers (max rate, [PF](#page-11-1) and satisfaction oriented).

Fig. [6.7](#page-85-0) presents three system's [KPIs:](#page-10-10) the percentage of satisfied [UEs,](#page-12-0) the system throughput and the Jain's fairness index. Solid lines represent the case where the schedulers had knowledge of all [RBs](#page-11-2) [CQI,](#page-10-12) while dashed lines represent the case where the central [RB](#page-11-2) was used as representative and the schedulers considered the [RBs](#page-11-2) [CQIs](#page-10-12) equal to the central [RB](#page-11-2) [CQI.](#page-10-12) Notice that all the dashed lines are very close to their equivalent solid lines. Considering the confidence interval of 95 %, one could say that they are equal in many cases.

Source: Created by the author.

It is clear that the proposed strategy does not strongly harm the system's performance, while it reduces signaling overhead and [RRA](#page-11-8) complexity. Since frequency selective fading is

mitigated by the [CH,](#page-10-9) there is no need for performing complex frequency selective [RRA.](#page-11-8)

6.2.2.2 Reliability

As already mentioned, [LTE](#page-10-2) is expected to be used together with [5G](#page-10-0) as a reliable link. The [UE](#page-12-0) will be either simultaneously connected to both [RATs](#page-11-5) or it will be able to fast switch to [LTE](#page-10-2) when [NR](#page-11-4) quality decreases. The effects of these two approaches may differ according to the adopted scheduler, as we show in this section.

Fig. [6.8](#page-87-0) presents three system's [KPIs.](#page-10-10) Solid lines represent results considering the [DC](#page-10-6) approach, while dashed lines concerns the results of the [FS.](#page-10-11)

Regarding the max rate scheduler, when considering [FS,](#page-10-11) instead of [DC,](#page-10-6) the [UEs](#page-12-0) in poor coverage have higher chances to be scheduled, since [UEs](#page-12-0) with high channel gain are scheduled in only one [RAT.](#page-11-5) Therefore, for the max rate criterion, [FS](#page-10-11) has higher percentage of satisfied [UEs](#page-12-0) and higher Jain's fairness index, but [DC](#page-10-6) has higher system throughput.

The satisfaction oriented assumes no coordination between the [BSs.](#page-10-1) As a consequence, in [DC,](#page-10-6) both [RATs](#page-11-5) try to satisfy the same [UEs](#page-12-0) first (the easiest ones). Therefore, there are more [UEs](#page-12-0) with low throughput in [DC](#page-10-6) than in [FS,](#page-10-11) which means higher fairness but less satisfied [UEs.](#page-12-0)

On the other hand, [PF](#page-11-1) assumes coordination between the [BSs.](#page-10-1) Therefore, in [DC](#page-10-6) there is more diversity to schedule the [UEs](#page-12-0) than in [FS,](#page-10-11) so higher chances to increase the fairness and to satisfy more [UEs.](#page-12-0) However, there is a trade-off between satisfying [UEs](#page-12-0) with low channel gains and having high system throughput, so [DC](#page-10-6) has lower system throughput than [FS.](#page-10-11)

As one can see, it is important to take into account the scheduler being used in the [BSs](#page-10-1) and the [KPIs](#page-10-10) of interest when enabling [DC](#page-10-6) or [FS](#page-10-11) mode in the [UEs,](#page-12-0) since the selected mode may have a different impact on system performance according to the adopted scheduler.

6.3 Chapter Summary

Concerning the [RRA](#page-11-8) complexity, it was concluded that it can be reduced with almost no loss of performance by taken into account the [CH](#page-10-9) effect. Since [CH](#page-10-9) occurrence means that the channel fluctuations over the frequency become negligible, the [UEs](#page-12-0) could report the [CQI](#page-10-12) of just one [RB-](#page-11-2)beam pair that represent the set of pairs where [CH](#page-10-9) occurs. Thus, in this case, the [RRA](#page-11-8) may be simplified, since there is no frequency selectivity.

Regarding the [5G](#page-10-0) reliability, [DC](#page-10-6) and [FS](#page-10-11) can be used to improve it. However, despite of what one could expect, it was concluded that [DC](#page-10-6) is not always better than [FS.](#page-10-11) [DC](#page-10-6) and [FS](#page-10-11) performances are impacted by the adopted [RRA](#page-11-8) strategy. For example, while a max rate strategy with [DC](#page-10-6) satisfies less [UEs](#page-12-0) than with [FS,](#page-10-11) [PF](#page-11-1) presented an opposite behavior.

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7 CONCLUSIONS

As presented in Chapter [1,](#page-17-0) the main purposes of this thesis was to study solutions based on [DC](#page-10-6) and [CH](#page-10-9) occurrence to address the problems of reliability and complexity in [5G.](#page-10-0)

The literature review presented in Chapters [1](#page-17-0) and [2](#page-30-0) showed a better understanding of both concepts. Concerning [DC,](#page-10-6) we identified some challenges related to [HetNet](#page-10-13) scenarios, e.g., [RAT](#page-11-5) selection, and the standardized architectures, which gave us an idea of the degrees of freedom related to new proposals. For example, since a non-ideal backhaul interface is expected to connect [BSs](#page-10-1) of different [RAT,](#page-11-5) the new solutions can not rely on heavy communications between them. Furthermore, we also identified alternative solutions to [DC,](#page-10-6) e.g., [FS,](#page-10-11) since [DC](#page-10-6) is not expected to have the best performance in all scenarios. Regarding the [CH,](#page-10-9) the literature review helped us to identify possible causes of [CH,](#page-10-9) e.g., higher number of antennas and narrower beams. Besides, the technical background regarding measurement related tasks, e.g., mobility management, and [NR](#page-11-4) reference signals, such as [SSB](#page-11-10) and [CSI-RS,](#page-10-14) helped us to determine which upper layer functions could take advantage of [CH,](#page-10-9) e.g., [SSB](#page-11-10) is associated with cell [RSRP](#page-11-11) measurements (handover) and [CSI-RS](#page-10-14) is associated with [CQI](#page-10-12) measurements (scheduling).

With respect to the numerical results, on one hand, Chapters [3](#page-45-0) and [4](#page-52-0) presented general analyses related to [DC](#page-10-6) and [CH](#page-10-9) occurrence, respectively. On the other hand, Chapters [5](#page-59-0) and [6](#page-79-0) addressed these concepts from the perspective of [RRA.](#page-11-8)

In Chapter [3,](#page-45-0) it was concluded that, in multi[-RAT](#page-11-5) scenarios, metrics related to signal quality, e.g. [RSRQ,](#page-11-12) should be prioritized instead of metrics only related to the signal strength, e.g., [RSRP.](#page-11-11) Decision criteria only based on signal strength tend to overload the [RAT](#page-11-5) with better propagation conditions. It was also concluded that, in [5G,](#page-10-0) it should be considered shorter time between consecutive [RAT](#page-11-5) scheduling evaluations, which can vary according to the system conditions, e.g., the [UE](#page-12-0) speed. Finally, it was showed that while [DC](#page-10-6) performs better than [FS](#page-10-11) for low loads, [FS](#page-10-11) can present higher gains than [DC](#page-10-6) for high loads.

In Chapter [4,](#page-52-0) the numerical results confirmed that when deploying narrow beams (in that case, it was the same as increasing the number of [SSBs](#page-11-10) and [CSI-RSs\)](#page-10-14), the [CH](#page-10-9) becomes more noticeable. Furthermore a framework for [CH](#page-10-9) detection and L1 measurement optimization was proposed and validated. The proposed solution calculates the standard deviation of [RSRP](#page-11-11) measurements in a sliding window in order to measure the level of [CH](#page-10-9) and, based on this, the measurement periodicity is dynamically adjusted. It was also concluded that the [UE](#page-12-0) mobility negatively impacts the [CH,](#page-10-9) i.e., increasing the [UE](#page-12-0) speed increases channel fluctuations for some [UEs.](#page-12-0) Despite of this, the proposed method still works for all [UEs.](#page-12-0)

In Chapter [5,](#page-59-0) we took into account the conclusions of Chapter [3](#page-45-0) and we proposed a decentralized framework for radio resource managing. It is divided into two parts: a [BS](#page-10-1) selection procedure (performed independently by each [UE\)](#page-12-0) and a resource assignment algorithm (performed independently by each [BS\)](#page-10-1). As suggested in Chapter [3,](#page-45-0) the proposed [BS](#page-10-1) selection procedure takes into account not only the signal strength, but also the state of the [UEs](#page-12-0) already connected to the target [BS.](#page-10-1) Besides, as also suggested in Chapter [3,](#page-45-0) the balance between [UEs](#page-12-0) in [DC](#page-10-6) and single connection is also taken into account.

Finally, Chapter [6](#page-79-0) focused on the implications of [DC](#page-10-6) and [CH](#page-10-9) occurrence on the adopted [KPIs](#page-10-10) and [RRA](#page-11-8) algorithm. Concerning the [RRA](#page-11-8) complexity, it was concluded that it can be reduced with almost no loss of performance by taken into account the [CH](#page-10-9) effect. Since [CH](#page-10-9) occurrence means that the channel fluctuations over the frequency become negligible, the [UEs](#page-12-0) could report the [CQI](#page-10-12) of just one subband-beam pair that represent the set of pairs where [CH](#page-10-9) occurs. Thus, in this case, the [RRA](#page-11-8) may be simplified, since there is no frequency selectivity. Regarding multi[-RAT](#page-11-5) connectivity, it was concluded that [DC](#page-10-6) and [FS](#page-10-11) performances are impacted by the adopted [RRA](#page-11-8) strategy. For example, while a max rate strategy with [DC](#page-10-6) satisfies less [UEs](#page-12-0) than with [FS,](#page-10-11) [PF](#page-11-1) presented an opposite behavior.

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A COMPUTATIONAL COMPLEXITY OF PROPOSED DISTRIBUTED FRAME-WORK

A.1 [BS](#page-10-1) Selection

Each [UE](#page-12-0) executes Alg. [5.1](#page-67-0) for each [RAT.](#page-11-5) In this analysis, we consider U_b as the number of [UEs](#page-12-0) connected to [BS](#page-10-1) b .

In 1. [2,](#page-67-0) there is 1 comparison. In the worst case, the set $\hat{\mathcal{B}}$ is not empty, thus the algorithm continues to be executed.

The loop in Il. [5-8](#page-67-0) has B_n steps, one per [BS](#page-10-1) of [RAT](#page-11-5) *n*. Considering that to find the minimum element among *i* elements we need to do $i-1$ comparisons, in l. [7,](#page-67-0) for each [BS](#page-10-1) *b* there are $(U_b - 1)$ comparisons. Thus, in this loop there are $\sum_{b=1}^{B_n} (U_b - 1) = \mathbf{U_n} - \mathbf{B_n}$ comparisons.

Lines [9-10](#page-67-0) sum B_n terms, thus we have $2(B_n - 1)$ sums.

Loops between ll. [11-16](#page-67-0) and ll. [12-14](#page-67-0) have B_n and 2 steps, respectively. Thus, the division in 1. [13](#page-67-0) is repeated $2B_n$ times and the multiplication in 1. [15,](#page-67-0) B_n times.

Similar to 1. [7,](#page-67-0) in 1. [17](#page-67-0) there are $B_n - 1$ comparisons.

The comparison in l. [18](#page-67-0) is done **once**. In the worst case, this test is false and the next line is not executed. Finally, in l. [21](#page-67-0) there are $\mathbf{T}^* + \hat{\mathbf{T}} - \mathbf{1}$ comparisons.

Therefore, in the worst case, the number of operations in the [BS](#page-10-1) selection procedure is

$$
1 + U_n - B_n + 2(B_n - 1) + 2B_n + B_n + B_n - 1 + 1 + T^* + \hat{T} - 1 =
$$

$$
U_n + 5B_n + T^* + \hat{T} - 2.
$$
 (A.1)

In the worst case $U_n = U$ and $B_n = B$, thus the complexity of the [BS](#page-10-1) selection procedure is $O(U + B)$.

A.2 Resource Assignment

Each [BS](#page-10-1) executes Alg. [5.2](#page-68-0) independently. In this analysis, we will consider a BS $$ of [RAT](#page-11-5) n with U_h [UEs](#page-12-0) connected to it.

Alg. [5.2](#page-68-0) has 3 loops, ll. [4-8,](#page-68-0) [9-17](#page-68-0) and [20-26.](#page-68-0) As explained in Section [5.5.2,](#page-67-1) in the first loop, we check if the [UEs](#page-12-0) are already satisfied. In the second one, we allocate [RBs](#page-11-2) until all [RBs](#page-11-2) have been assigned or all the [UEs](#page-12-0) have achieved their throughput requirement, or even both events have happened. Finally, on the third one, we allocate the remaining [RBs.](#page-11-2)

We will analyze the possible cases for loop 2.

A.2.1 All [RBs](#page-11-2) are Assigned in Loop 2

Thus, loop 2 is repeated K_n times and loop 3 does not happen. The worst case is when none [UE](#page-12-0) gets satisfied, neither in loop 1 nor in loop 2.

Concerning loop 1, it is repeated U_b times, one per connected [UE.](#page-12-0) In l. [5,](#page-68-0) we have 1 comparison which will be repeated U_b times, so this line has U_b comparisons. The operation in l. [6](#page-68-0) is not executed, since none [UE](#page-12-0) is satisfied.

In l. [9,](#page-68-0) we have 2 comparisons which will be repeated $K_n + 1$ times, so l. [9](#page-68-0) has $2(K_n + 1)$ comparisons.

In l. [10,](#page-68-0) the set \mathcal{K}_n starts with K_n [RBs](#page-11-2) and decreases in one at each iteration of loop 2. So, after assigning *i* [RBs,](#page-11-2) K_n has $K_n - i$ [RBs.](#page-11-2) Similarly, each [UE](#page-12-0) that gets satisfied is removed from \mathcal{U}_b , l. [15.](#page-68-0) In this case, we do less comparisons in l. [10,](#page-68-0) since we do not consider the elements $r_{u,k}$, of the satisfied [UEs.](#page-12-0) In the worst case, no one gets satisfied and we need to do more operations. Considering that to find the maximum element among i elements we need to do $i-1$ comparisons, to find the maximum $r_{u,k,b}$ in l. [10,](#page-68-0) after *i* assignments, we need to do $[U_b(K_n-i)-1]$ comparisons, in the worst case. Thus, we have $\sum_{i=0}^{K_n-1} [U_b(K_n - i) - 1] = \frac{1}{2}$ $\frac{1}{2}$ (**U**_b**K**_n² – 2**K**_n + **U**_b**K**_n) comparisons in l. [10.](#page-68-0)

In order to update the [UE](#page-12-0) throughput in l. [12,](#page-68-0) 3 operations are done: one multiplication, one sum and one division. Since this update is repeated K_n times, we have $3K_n$ operations. The operation in l. [13](#page-68-0) and the comparison in l. [14](#page-68-0) are also repeated K_n times, so, in these lines, we have K_n subtractions and K_n comparisons, respectively. In the worst case, the operation in l. [15](#page-68-0) is not computed, since no one gets satisfied.

Thus, the number of operations is

$$
U_b + 2(K_n + 1) + \frac{1}{2} \left(U_b K_n^2 - 2K_n + U_b K_n \right) + 3K_n + K_n + K_n =
$$

$$
\frac{1}{2} \left(U_b K_n^2 + U_b K_n + 12K_n + 2U_b + 4 \right). \tag{A.2}
$$

Therefore, the complexity of the first case is $O(U_b K_n^2)$.

A.2.2 All [UEs](#page-12-0) Achieve Their Required Throughput in Loop 2

In this case, we consider that in loop 1, $U_b - L$ [UEs](#page-12-0) were already satisfied, thus L [UEs](#page-12-0) gets satisfied in loop 2. It is also considered that D [RBs](#page-11-2) are allocated on the second loop, where $L \leq D \lt K_n$, so, on the third one, $K_n - D$ [RBs](#page-11-2) are allocated. The case $D = K$ is included in previous case. That way, loop 2 is repeated D times and loop 3, $K_n - D$ times.

Similar to the first case, in 1. [5,](#page-68-0) one comparison is repeated U_b times, resulting in U_b comparisons. Since $U_b - L$ [UEs](#page-12-0) were already satisfied, the operation in l. [6](#page-68-0) is repeated $U_b - L$ times. In a similar analysis, 1. [9](#page-68-0) has $2(D+1)$ comparisons.

The worst case for l . [10](#page-68-0) is when the L [UEs](#page-12-0) are satisfied on the last L iterations, resulting in $\sum_{i=0}^{D-L-1} [L(K_n - i) - 1] + \sum_{i=D}^{D-1}$ $_{i=D-L}^{D-1}[(D-i)(K_n-i)-1]$ comparisons.

Analogous to the first case, the number of operations required to update the [UE](#page-12-0) throughput in ll. [12](#page-68-0) and [24](#page-68-0) is 3D and $3(K_n - D)$, respectively, resulting in $3K_n$ operations.

The subtraction in 1. [13](#page-68-0) and the comparison in 1. [14](#page-68-0) are repeated D times, so, in these lines, we have **D** subtractions and **D** comparisons, respectively. The operation in l. [15](#page-68-0) is computed **L** times.

The comparison in l. [18](#page-68-0) is computed once, while the comparison in l. [20](#page-68-0) is repeated **Kn** −**D** + **1** times. Ll. [21](#page-68-0) and [22](#page-68-0) correspond to (**Kn** −**D**)(**Ub** − **1**) and $\frac{(K_n - D)(K_n - D + 1)}{2}$ comparisons, respectively. Finally, l. [25](#page-68-0) corresponds to **Kⁿ** −**D** subtractions.

The total amount of operations in case 2, i.e., sum of the described operations, is presented in [\(A.3\)](#page-100-0).

$$
U_b + (U_b - L) + 2(D + 1) + \sum_{i=0}^{D-L-1} [L(K - i) - 1] + \sum_{i=D-L}^{D-1} [(D - i)(K_n - i) - 1] + 3K_n
$$

+2D + L + 1 + (K_n - D + 1) + (K_n - D)(U_b - 1) + \frac{(K_n - D)(K_n - D + 1)}{2}
+ (K_n - D) =

$$
\frac{1}{2} [(L - 1)D^2 + D(-2U_b + 4LK_n + 3)] + \frac{1}{2} (LK_n - 2L^2K_n + K_n^2 + 9K_n + 2U_bK_n)
$$

+
$$
\frac{1}{6} (-L^3 - 6L^2 + L) + 2U_b + 4.
$$
 (A.3)

Since $D \le K_n$ and $L \le \min(U_b, K_n)$, the complexity of this case is $O(U_b K_n^2)$.

Since the complexity of both cases is $O(U_b K_n^2)$ and, in the worst case, $U_b = U$ and $K_n = K$, thus, it is concluded that the resource assignment is $O(UK^2)$.

Finally, considering the complexity of the [BS](#page-10-1) selection and resource assignment procedures, we conclude that the complexity of the proposed framework is $O(UK^2)$.