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Potential assessment and kinetic modeling of carboxylic acids production using dairy wastewater as substrate



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HIGHLIGHTS

- Dairy wastewater (DW) is a potential substrate to produce carboxylic acids (CA).
- Kinetic modeling is a useful tool to elucidate acidogenic fermentation kinetics.
- High yield of CA (0.66 mgCA mgCOD_A⁻¹) was obtained from DW acidogenic fermentation.
- Models that describe an exponential phase are suitable to simulate CA production.
- Low concentrations of a medium-chain CA were achieved without e-donors addition.

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ABSTRACT

Carboxylic acids (CA) are high added-value compounds that can be produced via anaerobic fermentation by using agroindustrial residues as substrates. However, different compounds in wastewater impose uncontrolled metabolic pathways, in which the acidogenic fermentation kinetics need to be elucidated. This work aimed to assess the potential production of CA from dairy wastewater (DW) and to perform the kinetic modeling of the process. The experiments were conducted in quadruplicate batch reactors (250 mL of working volume) with inoculum from a brewery UASB at 0.61 \pm 0.04 gCOD gVSS⁻¹. To inhibit methanogenesis, 0.05 % (v/v) chloroform was added to the reactors. The tests showed that DW is a readily fermentable substrate to acidogenic microorganisms because it presents high rates of short-chain CA formation in the first two days of the experiment. The low concentrations of medium-chain CA found indicate that fats and proteins did not function as the main carbon source for DW fermentation. The yield obtained was 0.66 mgCOD_A⁻¹, which corresponds to 0.83 mgCOD_{CA} mgCOD_A⁻¹. Kinetic modeling studies have shown that mathematical models that can describe an exponential phase, such as First-order and Fitzhugh models, are suitable for simulating the production of carboxylic acids. Finally, DW seems to be a promising substrate to be investigated in the carboxylic platform.

1. Introduction

The recovery of high added-value products from agroindustrial wastes can be a sustainable and economically viable alternative to decrease the dependence on fossil fuels and implement environmentally friendly chemical processes. Carboxylic acids (CA) are among these added-value products, which can be prospected anaerobically from macromolecules fermentation by microbial consortium, usually requiring inhibition of methanogenesis and sulfetogenesis [1–3].

During acidogenic fermentation, the major CAs produced are shortchain carboxylic acids, which have up to five carbon atoms. These compounds can be used as carbon source for further processing or in the synthesis of building block chemicals, pharmaceuticals, cosmetics, materials, bioplastics, such as polyhydroxyalkanoates (PHA), and biofuels [4–6]. Compared to methane (CH₄), they are easier and safer to store and transport, besides having a higher market price [7].

In the context of agroindustry, dairy production is one of the most important components of the trade balance in developed and developing countries. World milk production reached 811 million tons in 2017 [8]. The dairy industry consumes high amounts of water and generates large volumes of wastewater, about 0.2-10 L of wastewater per liter of processed milk, with about 4–11 million tons of wastewater

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discharged annually worldwide [9,10]. Dairy wastewater (DW) is composed of suspended and dissolved solids, soluble organic components, lactose, nutrients, fats, detergent residues, and disinfectants [11,12].

Due to its high chemical oxygen demand (COD) and a high volume of wastewater generated, they may represent an interesting substrate to be investigated either on the biorefinery concept or on the carboxylic platform [11,13]. According to Atasoy et al. [14], it is estimated that, on a global scale, approximately 9.15 Mt acetic acid, 6.47 Mt propionic acid, and 5.39 Mt butyric acid could be recovered from DW, evidencing the potential of using this residue in the production of CA.

Mathematical modeling of fermentation processes is an attractive strategy for its scaling and optimization, as simulations can be applied to resource recovery treatment plants for engineering design, operation and prediction, where small process improvements can generate significant economic [15,16]. These tools are already widely studied for the complete anaerobic digestion [17–19], especially to optimize biogas production from organic wastes. However, as far as we are concerned, there are just a few studies of kinetic modeling assessing acidogenic fermentation of agroindustrial wastes, especially DW, in the perspective of the carboxylic platform.

Thus, the objective of this work was to assess the potential of CA production, perform mathematical modeling and estimate kinetic parameters that describe the hydrolysis of particulate organic matter, soluble substrate consumption and CA production under acidogenic anaerobic conditions using DW as substrate and microbial consortium as inoculum.

2. Materials and methods

2.1. Substrate and inoculum

DW was collected from a dairy industry located in the municipality of Maranguape, Ceará, Brazil. After collection, the wastewater was stored in a refrigerator at approximately 3 °C to avoid its degradation. The physicochemical characterization is shown in Table 1, whose values are in agreement with the literature [11,20].

The batch reactors used in the assays were inoculated with a sludge collected from an upflow anaerobic sludge blanket (UASB) reactor used in the treatment of brewery wastewater. Total solids (TS), total volatile solids (TVS) and total fixed solids (TFS) concentrations of the sludge were 81.0, 33.8, 47.2 g L⁻¹, respectively.

2.2. Batch tests

CA production assays were performed in quadruplicate batch reactors in borosilicate flasks with 300 mL total volume, 250 mL reaction volume and 50 mL headspace. Basal medium and pH 7.0 buffering, previously adjusted with 1 M HCl or NaOH, were performed according to the guidelines of Dams et al. [21]. The food/microorganism (F/M) ratio was 0.61 \pm 0.04 gCOD gVSS⁻¹. To inhibit methanogenesis and promote the accumulation of the products of interest, 0.05 % (v/v) chloroform was added to batch reactors [22].

The bioreactors were sealed with butyl rubber stoppers and purged with nitrogen (N₂) for approximately 1 min to establish an anaerobic atmosphere within the flasks. They were then kept in an incubator (MA-420, Marconi LTDA, Brazil) under orbital agitation of 150 rpm and a temperature of 35 \pm 0.3 °C for 7 days, which was the period required to observe the total conversion of COD added in the reactors.

Samples of 1 mL were collected from reactors on days 0, 2, 4 and 7 for COD analysis and quantification of CA in order to assess substrate conversion kinetics. At the end of the experiment, a gas sample was extracted from the headspace of the batch reactors to verify the efficiency of methanogenic inhibition and to determine the average concentrations of CH_4 , hydrogen (H_2) , carbon dioxide (CO_2) and hydrogen sulfide (H_2S) in the biogas.

Table 1

Pl	nysi	cocl	nemical	characteristics	of	the	dairy	wastewater	used	fo	r batc	h testir	ıg.
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Parameter	Representation	Average Values	Unit
Hydrogen potential	pН	5.40	-
Electric conductivity	EC	5.260	μ S cm ⁻¹
Color	Color	424	mgPt-Co L ⁻¹
Turbidity	TB	3,760	NTU
Alkalinity	Al	223.1	$mgCaCO_3 L^{-1}$
Acidity	Ac	861.6	$mgH_3COOH L^{-1}$
Total Nitrogen	TN	168.4	mg-N L^{-1}
Total Kjeldahl Nitrogen	TKN	168.0	mg-N L^{-1}
Organic Nitrogen	ON	160.5	mg-N L^{-1}
Ammoniacal Nitrogen	AmN	9.4	mg-N L^{-1}
Total Oxygen Chemical Demand	COD_{T}	17,629	$mgO_2 L^{-1}$
Soluble Chemical Oxygen Demand	COD _S	12,365	$mgO_2 L^{-1}$
Particulate Chemical Oxygen Demand	COD_{P}	5,264	$mgO_2 L^{-1}$
Total Biochemical Oxygen Demand	$BOD_{5T}^{20^{\circ}C}$	11,875	$mgO_2 L^{-1}$
Soluble Biochemical Oxygen Demand	BOD _{5S} ^{20°C}	10,000	$mgO_2 L^{-1}$
Particulate Biochemical Oxygen Demand	$BOD_{5P}^{20^{\circ}C}$	1,875	$mgO_2 L^{-1}$
Total Phosphorous	TP	105.4	mg-P L^{-1}
Orthophosphate	PO_4^{-3}	52.9	mg-P-PO4 ^{3 –} L ⁻¹
Sulfate	SO_4^{2-}	43.9	$mg L^{-1}$
Fluoride	F ⁻	36.3	mg L^{-1}
Chloride	Cl ⁻	2984.8	mg L^{-1}
Total Solids	TS	18,263	mg L^{-1}
Total Volatile Solids	TVS	12,292	mg L^{-1}
Total Fixed Solids	TFS	5,971	mg L^{-1}
Total Dissolved Solids	TDS	15,679	mg L^{-1}
Volatile Dissolved Solids	VDS	9,796	mg L^{-1}
Fixed Dissolved Solids	FDS	5,883	mg L^{-1}
Total Suspended Solids	TSS	2,584	mg L^{-1}
Volatile Suspended Solids	VSS	2,496	mg L^{-1}
Fixed Suspended Solids	FSS	88	mg L^{-1}
Hexane Soluble Substances	O.G	94.6	mg L^{-1}

2.3. Analytical methods

Physicochemical characterization analyses were performed according to Standard Methods for the Examination of Water and Wastewater [23].

Biogas composition was analyzed by gas chromatography with dielectric barrier ionization discharge (GC BID-2010 Plus, Shimadzu Corporation, Japan) equipped with a GS-GASPRO column (60 m x 0.32 mm) (Agilent Technologies Inc., USA). The oven, injector and detector temperatures were 250, 50 and 100 °C, respectively. Helium gas (White Martins LTDA, Brazil) was used as a carrier gas in a 2 mL min⁻¹ flow, and the run time of the method was 9 min. Biogas quantification was performed by recording the accumulated pressure in each batch reactor using a gauge pressure transmitter (Warme LTDA, Brazil).

Acetic (HAc), propionic (HPr), butyric (HBu), isovaleric (i-HVa), valeric (HVa) and caproic (HCa) acids concentrations were determined by high performance liquid chromatography (HPLC) using HPLC LC-20A chromatograph (Prominence, Shimadzu Corporation, Japan) equipped with Aminex HPX-87H (300 mm x 7.8 mm) column (Bio-Rad, USA) at 65 °C with sulfuric acid (H_2SO_4) 5 mM in deionized water as eluent (0.6 mL min⁻¹ isocratic flow) and refractive index detector (RID-10A, Shimadzu Corporation, Japan). For chromatographic and soluble COD analyses, the samples were filtered through a 0.45 µm pore glass fiber membrane (EMD Millipore, USA).

2.4. Mass balance and yields

A mass balance of the system was performed in terms of COD using Eq. (1-10) expressed in Table 2. The concentrations of CA were

Equations used for mass balance calculations.

Equation	Mass balance equation
1	$COD_P = COD_T - COD_S$
2	$COD_A = COD_T - COD_{CA(t0)}$
3	$COD_C = COD_A - COD_{Bio(tf)}$
4	$COD_{Bio} = COD_S - COD_{CA}$
5	$COD_{CA} = COD_{CA(tf)} - COD_{CA(t0)}$
6	$COD_{VSS} = COD_A - COD_{CA} - COD_{Bio(tf)} - COD_{BG}$
7	$Y_C = \frac{COD_C}{COD_A}$
8	$Y1_{CA} = \frac{COD_{CA}}{COD_A}$
9	$Y_{SSV} = \frac{COD_{VSS}}{COD_A}$
10	$Mass \ Balance = \frac{COD_S + COD_{BG} + COD_{VSS}}{COD_T}$

Legend: COD_P : particulate COD added in the batch reactor. COD_T : total COD added in the batch reactor. COD_S : soluble COD added in the batch reactor. COD_A : fraction of the total COD available to be bioconverted to CA or directed to cell growth and biogas formation, corresponds to the total COD fraction applied at the beginning of the experiment that is not in the form of CA. $COD_{CA(10)}$: fraction of soluble COD in the form of CA at the beginning of the batch. COD_c : COD directed to the production of CA, cell growth and biogas formation. $COD_{Bio(tf)}$: soluble COD fraction not related to CA at the end of the incubation period. COD_{Bio} : fraction of COD soluble not referring to CA. COD_{CA} : mass of CA formed during the incubation period. $COD_{CA(TD)}$: mass of CA at the end of the end of the incubation period. COD_{VSS} : COD directed to cell growth. COD_{BiG} : COD removed by biogas production (methane or hydrogen). Y_C : stoichiometric coefficient of COD yield converted to CA. Y_{VSS} : stoichiometric coefficient of cell growth yield. Units in mgCOD.

multiplied by the reaction volume in the bioreactor on the day of collection to obtain the mass of CA. The concentration of organic matter (COD in the form of acids) of each acid was obtained by the following conversion factors: 1 mgHAc = 1.07 mgCOD. 1 mgHPr = 1.51 mgCOD. 1 mgHBu = 1.82 mgCOD. 1 mgi-HVa = 2.04 mgCOD. 1 mgHVa = 2.04 mgCOD. 1 mgHCa = 2.21 mgCOD [24].

The yield, selectivity, and productivity of CA were calculated according to Eqs. (11), (12) and (13), respectively.

$$Y2_{CA} = \frac{M_{TCA}}{COD_A} \tag{11}$$

Selectivity=
$$\frac{M_{CA}}{M_{TCA}} \times 100$$
 (12)

$$Productivity = \frac{C_{CA1D} - C_{CAB}}{Time}$$
(13)

where: Y2_{CA}: CA production in relation to the available COD (mg_{CA} mgCOD_A⁻¹); M_{TCA}: total mass of CA formed during the incubation period (mg_{CA}); COD_A: total COD mass fraction available to be converted at the beginning of the batch (mgCOD); Selectivity: percentage of each CA formed in relation to the total acids produced (%); M_{CA}: mass of CA formed during the incubation period (mg_{CA}); Productivity: quantity of CA present per working volume and per time (mg_{CA} L⁻¹ d⁻¹); C_{CA1D}: CA concentration at one day of collection (mg_{CA} L⁻¹); C_{CAB}: CA concentration at the beginning of the batch (day zero) (mg_{CA} L⁻¹); and Time: unit of time (d).

2.5. Model fitting

The equations of the kinetic models selected to describe the hydrolysis process of particulate organic matter, soluble substrate consumption, and CA production in terms of COD and individual CA production are presented in Table 3.

A nonlinear least-squares regression analysis was performed using the Microsoft Office Excel 2019 Solver tool to estimate the parameters

Table 3

Selected models to describe the conversion of organic matter (hydrolysis, soluble substrate consumption and production of carboxylic acids – in terms of COD and individual acids).

Kinetic Model	Equation of the Kinetic Model
Hydrolysis	
First-order	$C_t = C_0 \exp(-kt)$
First-order with Residual	$C_t = C_r + (C_0 - C_r) \exp(-kt)$
Consumption of Soluble S	ubstrate (Biodegradable COD)
First-order	$C_t = C_0 exp(-kt)$
First-order with Residual	$C_t = C_r + (C_0 - C_r)exp(-kt)$
Logistic	$C_{t} = \frac{C_{0} + X_{0}}{1 + \left(\frac{X_{0}/C_{0}}{2}\right) exp\left[K_{L}(C_{0} + X_{0})t\right]}$
Monod with Growth	$C_{t} = exp\left(\frac{(C_{0} + X_{0} + K_{S})\ln\left(\frac{X}{X_{0}}\right) - (C_{0} + X_{0})\mu_{m\dot{\alpha}x}t + K_{S}\ln(C_{0})}{K_{S}}\right)$
Production of Carboxyli	c Acids
First-order	$CA_t = CA_f \left[1 - exp(-k_{CA}t) \right]$
Second-order	$CA_{t} = \frac{k_{CA''}(CA_{f})^{2}t}{1 + k_{CA''}(CA_{f})t}$
Fitzhugh	$CA_t = CA_f \left[1 - exp(-k_{CA}t)^n \right]$
Cone	$CA_t = \frac{CA_f}{1 + (k_{CA}t)^{-n}}$
ВРК	$CA_t = CA_f \left\{ 1 - exp \left[(m-1) \left(\frac{t}{t_0} \right)^{1/m} \right] \right\}$
	$\mu_m = \frac{CA_f exp(m)(1-m)}{e \cdot m \cdot t_0} \qquad \qquad k_{CA} = \frac{exp(m)(1-m)}{e \cdot m \cdot t_0}$
Monomolecular	$CA_t = CA_f \{1 - exp \left[-k_{CA}(t - \lambda)\right]\}$
Modified Gompertz	$CA_{t} = CA_{f} \exp\left\{-\exp\left\{-\exp\left[\frac{\mu_{m} e}{CA_{f}}(\lambda - t) + 1\right]\right\}$
Logistic	$CA_{t} = \frac{CA_{f}}{1 + exp\left[\frac{4\mu_{m}(\lambda - t)}{CA_{f}} + 2\right]}$

Legend: C_t: concentration of organic matter over time; C₀: initial organic matter concentration; k: velocity constant (k_H: hydrolysis rate constant/k_B: soluble substrate degradation rate constant); C_r: residual organic matter concentration; X₀: initial biomass concentration; X: final biomass concentration; k_L: Logistic model constant; K_S: saturation constant/Monod constant; μ_{max} : maximum microbial growth rate; CA_t: CA concentration over time; CA_f: final concentration of CA; k_{CA}: first-order CA production rate constant, k_{CA}": second-order CA production rate constant, t: digestion time, n: shape constant; m: constant of the BPK model; e: Euler number; λ : lag phase time; μ_m : maximum CA productivity.

of the selected kinetic models. This method adjusts the values of the model variables in order to minimize the sum of the squares of the differences between predicted and measured values. Data obtained from kinetic modeling were applied to plot the curves of each process using Origin software version 8.1 (OriginLab Corporation, Northampton, MA, USA).

2.6. Statistical analyses

The selection of the model that best describes each organic matter conversion process was performed using the determination coefficient (R^2) and the following error functions: root mean square error (RMSE); normalized root mean square error (NRMSE) and Akaike Information Criterion (AIC) [25,26].

$$RMSE = \sqrt{\frac{\sum_{i} (Y_{i,exp} - Y_{i,est})^{2}}{n}}$$
(14)

$$NRMSE = \left[\frac{RMSE}{(Y_{max} - Y_{min})}\right] x \ 100 \tag{15}$$

$$AIC = N. \ln\left(\frac{SS}{N}\right) + 2k \tag{16}$$

Table 4 Mass balance of fermentative assays using dairy wastewater as substrate.

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^a Time	^b COD _T	^b COD _P	^b COD _S	^b COD _{CA}	^b COD _{BIO}	^b COD _{BG}
0	700.7 ± 0.0	250.0 ± 0.0	450.7 ± 0.0	9.0 ± 0.0	441.7 ± 0.0	
2	660.6 ± 27.1	133.3 ± 38.3	527.3 ± 39.7	440.6 ± 35.2	86.6 ± 23.9	
4	657.6 ± 5.2	96.6 ± 14.3	561.0 ± 18.8	525.8 ± 5.9	35.2 ± 16.2	
7	654.4 ± 10.3	60.7 ± 11.3	593.7 ± 9.8	586.5 ± 6.4	7.2 ± 4.9	0.0 ± 0.0
^b COD _A	^b COD _{CA}	^b COD _C	^b COD _{VSS}	^c Y _C	^d Y1 _{CA}	eYvss
691.7 ± 0.0	577.5 ± 6.4	684.5 ± 4.9	107.0 ± 9.8	0.99 ± 0.01	0.83 ± 0.01	0.15 ± 0.01

Legend: a. Time in day (d); b. Mass in mgCOD; c. Y_{C} : Yield of converted COD (mgCOD_C mgCOD_A⁻¹); d. $Y1_{CA}$: COD yield converted to carboxylic acids (mgCOD_{CAf} mgCOD_A⁻¹); e. Y_{VSS} : yield of COD converted to biomass (mgCOD_{VSS} mgCOD_A⁻¹).

where: n is the number of experimental data points (observations); Y_{max} and Y_{min} are the observed maximum and minimum values for the evaluated response variable, respectively; AIC is the Akaike Information Criterion (dimensionless); N is the number of observations of experimental data; SS is the square sum of the residuals and k is the number of model parameters.

3. Results and discussions

3.1. Mass balance

The mass balance showed that most of the initial substrate COD that was available to the microorganisms (691.97 \pm 0.00 mgCOD - COD_A) was converted to CA (83 \pm 1 %), while the remaining COD was either directed to new cell formation (15 \pm 1 %) or remained available for microbial conversion or other non-detected products (1 \pm 1 %) (Table 4). Therefore, 99 \pm 1 % of the total applied COD was biologically transformed in CA and new cells, representing a mass of 684.5 \pm 4.9 mgCOD (COD_C), and demonstrating a high biodegradability of the DW, as reported by Silva et al. [27].

The yield of CA formation in relation to the available COD (Y1_{CA}), as well as the biomass formed in relation to the converted COD (Y_{VSS}), were $0.83 \pm 0.01 \text{ mgCOD}_{CA} \text{ mgCOD}_{A}^{-1}$ and $0.15 \pm 0.01 \text{ mgCOD}_{VSS}$ mgCOD_A⁻¹, respectively, resulting in a converted COD yield (Y_C) of $0.99 \pm 0.01 \text{ mgCOD}_{C} \text{ mgCOD}_{A}^{-1}$ (Table 4). These coefficients are essential to the design of biochemical reactors, to determine if the process would be economically viable and to help the process optimization in terms of efficiency and costs [28].

The biogas formed was mainly composed of CO₂ followed by traces of H₂. The concentrations of CH₄ and H₂S were below the quantification limit of the chromatographic method. Therefore, COD removal by biogas production was considered null (COD_{BG} = 0). Thus, it can be inferred that the inhibition of methanogenic archaea with 0.05 % (v/v) chloroform was efficient. Chloroform is a nonspecific inhibitor capable of inhibiting the methyl-coenzyme M reductase in methanogenic archaea, and may also interfere with the metabolism of homoacetogenic and sulfate-reducing bacteria (SRB) [29].

About 577.5 \pm 6.4 mg of COD was produced in terms of CA considering the available organic matter that was applied (COD_A), from which 305.3 \pm 7.4 mgCOD was directed to HAc production, 176.9 \pm 3.1 to HPr, 48.0 \pm 1.4 to HBu, 26.8 \pm 1.0 to i-HVa, 8.9 \pm 0.4 to HVa and 11.7 \pm 0.2 to HCa. Therefore, 53 \pm 1 % of the converted COD was directed to the formation of HAc; 31 \pm 1 % to HPr; 8 \pm 1 % to HBu; 5 \pm 1 % to i-HVa; 2 \pm 1 % to HVa and 2 \pm 1 % to HCa.

In this sense, 92 % of the converted COD was to the production of HAc, HPr, and HBu. The result obtained is consistent with the literature, as HAc, HPr and HBu are the main CA synthesized during acidogenic fermentation of organic waste using microbial consortium, and the distributions of the main soluble products reflect the predominant metabolic pathways in the bioreactor [30,7].

About 2 ± 1 % of the organic matter converted to CA was directed to the production of HCa, which differs from the others because it is a

medium-chain carboxylic acid (MCCA) and has a higher added-value in the industry. HCa can be biologically formed by an elongation process, which takes place via the reverse β -oxidation pathway, in the presence of an electron donor such as lactic acid (HLa), ethanol (EtOH) or H₂ [31,32].

At the beginning of the experiment, 124.5 and 13.1 mgCOD of HLa and EtOH were detected, respectively, which may have been directed to HAc and other acids production or even to elongation processes. Other short-chain acids such as HBu, i-HVa, and HVa can also be produced by chain elongation, as this is a process of sequentially adding two carbons to an even or odd chain CA [32]. After the beginning of the experiment, no concentrations of HLa and EtOH were detected, indicating that these compounds were consumed.

In literature, DW is commonly used in studies aimed at H_2 production, since lactose is a potential substrate [33]. On the other hand, reports of CA production from DW are scarce. Some studies have used cheese whey, a liquid by-product of the dairy industry – made up of lactose, protein, and lipids – to evaluate CA production.

For instance, Silva et al. [27] studied the acidification potential (i.e. the ratio between acid COD produced and the total applied COD) of a variety of organic residues, including cheese whey. They used batch reactors (working volume of 230 mL) with sewage sludge as inoculum, F/M ratio of 4 gCOD gVSS⁻¹, temperature of 37 °C and 2-bromoethanesulfonic acid (BES) to inhibit methanogenesis. The results indicated that cheese whey was a highly fermentable substrate, with an acidification degree of 39.8 ± 1.3 %, and 51.6 ± 3.8 % of the soluble COD was CA on the last day of the experiment (30th day).

On the other hand, in the current investigation, about 98 $\% \pm 0.81$ of the soluble COD corresponded to CA on the seventh day of the experiment, indicating that in Silva et al. [27] other metabolites, such as alcohols, may have been produced over the experimental time, contributing to the reduction of the CA formed in relation to the soluble COD available. Therefore, depending on the type of substrate and conditions applied, the COD available can be transformed into acids in the first days of testing as reported elsewhere [34,35].

3.2. Productivity, selectivity, and yield of carboxylic acids

The maximum productivity rate (μ_m) of CA occurred on the second day of the experiment for all acids (Table 5), and the highest values achieved were for HAc ($\mu_m = 420.4 \pm 34.5 \text{ mg L}^{-1} \text{ d}^{-1}$) and HPr ($\mu_m = 202.8 \pm 13.3 \text{ mg L}^{-1} \text{ d}^{-1}$). The average of μ_m was 999.65 \pm 597.35 mg L⁻¹ d⁻¹ and the total yield of CA (Y2_{CA}) was 0.66 mgCA mgCOD_A⁻¹, which corresponds to 0.83 mgCOD_{CA} mgCOD_A⁻¹ (Y1_{CA}).

The maximum productivity of HAc and HBu occurred on the second day (Table 5), suggesting that the addition of electron donors on this time of fermentation could favor the chain elongation process for HCa production in processes with similar kinetics, as HAc and HBu are the main electron acceptors to the chain elongation for HCa [31,32]. Since there was no addition of electron donors for HCa production, the results of using DW as a substrate for acidogenic fermentation and chain elongation studies are promising.

Maximum r	productivit	y rate,	selectivity	y and	yield o	of carbox	vlic acids	from th	e fermentative	assays	using c	dairy	wastewater a	s substrate.
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Parameter	HAc	HPr	HBu	i-HVa	HVa	HCa
^a Maximum productivity rate	420.4 ± 34.5	202.8 ± 13.3	31.8 ± 6.6	15.0 ± 1.3	$\begin{array}{l} 4.9 \pm 0.6 \\ 1 \pm 0.0 \\ 0.01 \pm 0.01 \end{array}$	4.4 ± 1.28
^b Selectivity	63 ± 0.8	26 ± 0.6	6 ± 0.2	3 ± 0.1		1 ± 0.0
^c Yield	0.4 ± 0.02	0.17 ± 0.01	0.04 ± 0.01	0.02 ± 0.01		0.01 ± 0.01

Legend: a. Maximum productivity rate (μ_m) of each acid produced (mg L⁻¹ d⁻¹); b. Percentage of each acid formed in relation to the total acids produced (%); c. Each acid yield in relation to the applied COD (mgCA mgCOD_A⁻¹).

In addition, the highest productivity and selectivity found for HAc are consistent with the studies of Chartrain and Zeikus [36], who reported that acetate corresponded to about 70 % of the intermediate metabolites produced from anaerobic lactose digestion. The substrate composition used in CA synthesis can influence both the amount produced and the distribution of acids and is one of the factors determining the choice of bioprocess operating parameters [37].

As the ranges are well-reported in the literature [38], it is known that DW is composed mainly of lactose $(250-930 \text{ mg L}^{-1})$, but fats $(35-500 \text{ mg L}^{-1})$ and proteins $(210-560 \text{ mg L}^{-1})$ are also part of its composition, likely being used as carbon sources during the fermentation process. Carbohydrates such as lactose are converted to glucose by enzymes, and most of the anaerobic bacteria use the Embden-Meyerhof-Parnas (EMP) glycolytic pathway to metabolize lactose [38].

Lactose hydrolysis involves sequential reactions with intermediate saccharides by β -galactosidase, which catalyzes lactose hydrolysis to galactose and glucose. Pyruvate produced from the EMP pathway is the main control point for fermentation, as it can be converted by acidogenic bacteria into a wide variety of metabolites such as HAc, HPr, HBu, alcohols (EtOH, propanol, and butanol), H₂ and CO₂. Subsequently, HPr, HBu, alcohols, and CO₂ are converted to HAc by proton reducing acetogenic pathways or by the homoacetogenic pathway [7,38,39].

In literature, it is already well established that HAc, HPr, and HBu are the acids mostly produced in carbohydrate fermentation [37]. Kisaalita et al. [40] studied the acidogenic fermentation of lactose in continuous flow reactor (1.5 L) using anaerobic sewage sludge at mesophilic temperature, pH 6.5 and stirring at 400 rpm. The authors concluded that HAc and HBu were the main products formed, and EtOH, HPr and HCa were formed in lower concentrations.

Although the carbohydrate fraction was not quantified in the physicochemical characterization of DW (Table 1), it is possible to infer from the CA profile generated that, carbohydrates, especially lactose, were the carbon source mostly used by the acidogenic microorganisms. In addition, lactose degradation provides the highest formation of HAc and HBu, according to the studies by Kisaalita et al. [38]. However, HPr was produced in larger proportions than HBu in DW fermentation, indicating that differences in individual CA depend on the complexity and heterogeneity of substrates (such as protein and lipid content) and the different operational parameters applied, which may activate or inactivate specific metabolic pathways [5,37].

Concentrations of oils and greases (94.6 mg L⁻¹) and total nitrogen (168.3 mg-N L⁻¹) in the DW physicochemical characterization (Table 1) indicate, respectively, the presence of lipids and proteins (such as casein) in milk. Lipids and proteins are considered less biodegradable than carbohydrates. In slow lipid metabolization, long-chain fatty acids (LCFA) are produced which can adhere to the bacterial cell wall and cause metabolic inhibition. Proteins, by presenting tertiary and quaternary three-dimensional structures, make proteases action more difficult. For these reasons, lipid and protein hydrolyses are usually considered the limiting step of acidogenic fermentation [37,41]. Because it is a wastewater from industrial processes that involve heat exchange [38], protein hydrolysis was not a limiting factor of acidogenic fermentation, since it is likely that proteins have gone through a denaturation process, which compromises its three-dimensional structure.

In addition, satisfactory i-HVa, HVa, and HCa production are related to protein fermentation, since the acidogenesis of non-proteinaceous substrates showed low yields of these CAs [42,43]. The low concentrations of these acids, as well as the short lag time in relation to CA production (section 3.4), indicate that in our case fats and proteins did not function as the main carbon source for DW fermentation, which is in agreement with other investigations [35,41].

Bengtsson et al. [44] studied the acidogenic fermentation of cheese whey in batch reactors (1.0 L) with acidogenic anaerobic sludge, mesophilic temperature (37 °C), pH 6.0 and reaction time of 17–57 days until CA stabilization production was achieved. The authors obtained higher selectivity of HAc (43 %), HPr (15 %) and HBu (42 %) and yield of 0.60 gCA $gCOD_A^{-1}$. The acids i-HVa, HVa and HCa acids were produced with low selectivity, and EtOH was not detected. The results were similar to the current experiments performed with DW since the yield obtained was 0.66 gCA $gCOD_A^{-1}$.

3.3. Kinetic modeling of hydrolysis and soluble substrate consumption

There was a continuous hydrolysis process of the particulate COD, as this fraction decreased in the system. Thus, soluble and biodegradable COD represented by carbohydrates, proteins and lipids and other soluble organic compounds, became available gradually. Simultaneously, the portion of biodegradable COD (available for conversion) decreased progressively and continuously, as shown in Fig. 1A, indicating that the consumption of this COD fraction occurred faster when compared to the COD fraction generated from the hydrolytic process. These results can be confirmed from the analysis of the estimated kinetic parameters from the mathematical COD conversion modeling (Table 6).

Soluble substrate degradation rate constant ($k_B = 0.86 \pm 0.31 d^{-1}$) was higher than the hydrolysis rate constant ($k_H = 0.47 \pm 0.50 d^{-1}$), according to First-order with residual model (Table 6). Since $k_B > k_H$, the biodegradable COD consumption rate was higher than the degradation rate of the particulate COD fraction (Figs. 1B and 1C). The soluble substrate decay is high, between the first and the second day (Fig. 1C), while the decay of particulate organic matter is slower considering the same period (Fig. 1B). The higher concentration of biodegradable COD available on the first day (1.77 gCOD L⁻¹) compared to particulate COD concentration (1.00 gCOD L⁻¹) may have contributed to this [45].

The First-order kinetic model with residual was the model that best fit not only the hydrolysis curve of particulate organic matter (Fig. 1B), with a high coefficient of determination ($R^2 = 0.995$) and lower AIC value (-29.062), but also the curve formed by the consumption of soluble substrate (Fig. 1C), with high R^2 (0.999) and lower AIC values (-25.950). This model, when considering the concentration of residual soluble organic matter (C_r) in its equation, may provide a better fit than the First-order model. Nevertheless, the First-order kinetic model (without residual) was also quite suitable for the mathematical simulation of both processes.

Logistic and Monod with growth models were also used to describe the consumption of soluble substrate and presented the least satisfactory adjustment performance (Table 6). The Logistic model is increasingly applied in the study of fermentative processes [18], being able to



Fig. 1. Organic matter concentration profiles (A), Kinetic modeling of hydrolysis of particulate COD (B) and Kinetic modeling of the biodegradable COD (C), during the fermentative tests using dairy wastewater as substrate.

Parameters estimated from hydrolysis kinetic modeling and soluble substrate consumption from fermentative assay using dairy wastewater as substrate.

Model	Parameter	Value	Model	Parameter	Value
Hydrolysis					
First-order	$k_{\rm H} (d^{-1})$	0.24 ± 0.14	First-order with	C_r (gCOD L ⁻¹)	0.25 ± 0.05
	R ²	0.962	Residual	$k_{\rm H} ({\rm d}^{-1})$	0.47 ± 0.50
	RMSE	0.055		R ²	0.995
	NRMSE	7.363		RMSE	0.021
	AIC	-21.215		NRMSE	2.761
				AIC	-29.062
Consumption of Soluble Sub	strate				
First-order	$k_{\rm B} ({\rm d}^{-1})$	0.77 ± 0.19	First-order with	C_r (gCOD L ⁻¹)	0.05 ± 0.03
	R^2	0.997	residual	$k_{\rm B} ({\rm d}^{-1})$	0.86 ± 0.17
	RMSE	0.037		R ²	0.999
	NRMSE	2.135		RMSE	0.024
	AIC	-24.359		NRMSE	1.363
				AIC	-25.950
Monod with growth	K_S (gCOD L ⁻¹)	5.86 ± 2.18	Logistic	k_{L} (L gCOD ⁻¹ d ⁻¹)	0.66 ± 0.11
	X (gSSV L^{-1})	4.70 ± 0.00		$k_{\rm B} ({\rm d}^{-1})$	0.14 ± 0.02
	$\mu_{máx} (d^{-1})$	0.70 ± 0.31		R ²	0.996
	k_{L} (L gCOD ⁻¹ d ⁻¹)	0.12 ± 0.02		RMSE	0.044
	$k_{\rm B} ({\rm d}^{-1})$	0.56 ± 0.09		NRMSE	2.549
	\mathbb{R}^2	0.997		AIC	- 22.940
	RMSE	0.037			
	NRMSE	2.133			
	AIC	-20.366			

Legend: k_H : hydrolysis rate constant; k_B : soluble substrate degradation rate constant; C_r : residual COD concentration; K_S : saturation constant/Monod constant; X: final biomass concentration; μ_{max} : maximum microbial growth rate; k_L : Logistic model constant; R^2 : coefficient of determination; RMSE: roof mean square error; NRMSE: normalized roof mean square error; AIC: Akaike Information Criteria.

Parameters estimated from the kinetic modeling of COD production for carboxylic acids from fermentative assay using dairy wastewater as substrate.

Model	Parameter	Value	Model	Parameter	Value
First-order	k _{CA} (d ⁻¹) R ² RMSE NRMSE AIC	0.60 ± 0.06 0.997 0.052 2.142 -21.683	Second-order	k _{CA} "(L gCOD ⁻¹ d ⁻¹) R ² RMSE NRMSE AIC	0.65 ± 0.11 0.985 0.117 4.819 -15.197
Fitzhugh	k _{CA} (d ⁻¹) n R ² RMSE NRMSE AIC	$\begin{array}{c} 0.47 \pm 0.09 \\ 0.69 \pm 0.33 \\ 0.998 \\ 0.041 \\ 1.699 \\ -21.539 \end{array}$	Cone	k _{CA} (d ⁻¹) n R ² RMSE NRMSE AIC	$\begin{array}{c} 0.81 \pm 0.17 \\ 1.91 \pm 0.30 \\ 0.996 \\ 0.057 \\ 2.343 \\ -18.967 \end{array}$
Monomolecular	k _{CA} (d ⁻¹) λ (d) R ² RMSE NRMSE AIC	$\begin{array}{l} 0.60 \pm 0.06 \\ 0.00 \pm 0.00 \\ 0.997 \\ 0.052 \\ 2.142 \\ -19.683 \end{array}$	Modified Gompertz	$\begin{array}{l} \mu_m \ (gCOD \ L^{-1} \ d^{-1}) \\ \lambda \ (d) \\ R^2 \\ RMSE \\ NRMSE \\ AIC \end{array}$	$\begin{array}{c} 0.98 \pm 0.11 \\ 0.16 \pm 0.02 \\ 0.987 \\ 0.109 \\ 4.491 \\ -13.762 \end{array}$
Logistic	μ_m (gCOD L ⁻¹ d ⁻¹) λ (d) R ² RMSE NRMSE AIC	$\begin{array}{c} 1.29 \pm 0.18 \\ 0.62 \pm 0.05 \\ 0.976 \\ 0.145 \\ 5.983 \\ -11.466 \end{array}$	ВРК	$\begin{array}{l} m \\ t_0 \ (d) \\ \mu_m \ (gCOD \ L^{-1} \ d^{-1}) \\ k_{CA} \ (d^{-1}) \\ R^2 \\ RMSE \\ NRMSE \\ AIC \end{array}$	$\begin{array}{c} 0.47 \pm 0.07 \\ 1.83 \pm 0.28 \\ 0.88 \pm 0.04 \\ 0.36 \pm 0.02 \\ 0.997 \\ 0.052 \\ 2.142 \\ -19.683 \end{array}$

Legend: k_{CA} : first-order CA production rate constant, k_{CA} ": second-order CA production rate constant; n: form constant; λ : lag phase time; μ_m : maximum CA productivity; m: constant of the BPK model; R^2 : coefficient of determination; RMSE: roof mean square error; NRMSE: normalized roof mean square error; AIC: Akaike Information Criteria.

estimate a constant k_L , defined as the ratio between the maximum growth rate (μ_{max}) and the Monod saturation constant (K_S), therefore k_L = μ_{max}/K_S . The higher μ_{max} , the higher the k_L and the higher the affinity of the microorganisms for the substrate. Through mathematical relationships, k_L (0.66 \pm 0.11 L gCOD $^{-1}$ d $^{-1}$) was obtained from the data estimated by the growing Monod model and, through it, k_B (0.14 \pm 0.02 d $^{-1}$).

Mathematical modeling using the growing Monod kinetic model presented the least satisfactory performance among the models tested for soluble substrate consumption. The Monod constant K_S obtained was 5.86 \pm 2.18 gCOD L⁻¹.

It is noteworthy that the final biomass concentration value estimated by the model (X = $4.70 \pm 0.00 \text{ gVSS L}^{-1}$) was the same as the initial biomass concentration (X₀) added in the assays, indicating that there was no cell growth. Nevertheless, 15 ± 1 % of the converted organic matter was directed to biomass production (Table 4, Section 3.1), which allows inferring low cell growth, as expected for anaerobic systems.

Some factors may have influenced the fit, given this inconsistency, as the Monod model is highly accurate for pure cultures and simple substrates, but fails to satisfactorily describe substrate consumption for heterogeneous cultures. In addition, its use is limited when cultivation conditions change rapidly or when there are low substrate concentrations [28,46].

3.4. Kinetic modeling of carboxylic acids production

Among the models tested to describe CA production in terms of COD, the First-order model presented the best fit to CA production data, with satisfactory R^2 (0.997) and lower AIC values (-21.683) compared to the other models, allowing to estimate the CA production rate constant (k_{CA}) of 0.60 \pm 0.06 d⁻¹. It is noticed that the production of CA in terms of COD from DW follows first-order kinetics [45], as evidenced by the lower values of the error functions of the First-order model in relation to that of Second-order model (Table 7).

The COD production curve in terms of COD (Fig. 2) resembles a

reverse L-shape, which characterizes a high COD productivity in the first days of incubation and an absence or short lag period relative to the production of acids [19]. At the end of the seven days of the experiment, 2.42 ± 0.03 gCOD L⁻¹ of CA were formed, and 64 % of this concentration was produced in the first 48 h. Probably, the kinetics of acid production from DW resembles the kinetics of microbial growth, conventionally described by the Monod model (1942), the enzymatic kinetics of Michaelis-Menten (1902) and the kinetics of CH₄ production in anaerobic reactors, whose curves are hyperbolic functions and have an exponential phase [19,47]. Therefore, the First-order, Fitzhugh, and Cone models may be suitable for this purpose.

Three models (Monomolecular, Modified Gompertz and Logistic) provided as output lag phases (λ) lower than one day, and one of them



Fig. 2. Kinetic modeling of COD production in the form of carboxylic acids (First-order model) from the fermentative assays using dairy wastewater as substrate.

Parameters estimated from the kinetic mode	ling of the product	ion of carboxylic acids fro	om the fermentative assa	iys using dairy waste	water as substrate.
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Firstorderkag. (a ⁻¹)0,610,6900,6900,6900,6900,6000,6	Model	Parameter	HAc	HPr	HBu	i-HVa		HVa	HCa
R ² 0.99 0.88 0.990 0.990 0.993 0.993 0.993 NRMSE 0.011 0.212 0.474 3.209 -5.22 -5.252 -5.438 Monomolecular 0.016 0.012 0.001 0.001 0.001 -5.252 -5.438 Monomolecular 0.024 -31.252 -3.9308 -4.27 -8.039 -5.252 -5.438 Monomolecular 0.001 0.000 0.002 0.001 0.001 0.001 0.001 0.001 0.001 0.001 0.001 0.001 0.001 0.001 0.001 0.001 0.001 0.001 0.001 0.001 0.001 0.001 0.	First-order	$k_{CA} (d^{-1})$	0.611	0.800	0.411	0.453		0.401	0.321
RMSE 0.011 0.021 0.004 0.020 0.01 0.01 HMSE 0.874 -2.8985 -41.908 -7.070 -5.752 -5.252 AC 0.587 0.2828 0.490 0.7470 -5.752 -5.252 R 0.993 0.397 0.397 3.074 0.931 RA 0.993 0.991		R ²	0.999	0.988	0.990	0.990		0.993	0.969
NRMSE 0.874 3.454 3.745 9.494 3.209 6.522 Firzhugh 0.674 -3.422 -2.805 -41.00 -7.522 -5.522 -5.522 kc, (a'-) 0.936 0.244 0.939 2.377 0.7522 -5.522 R ¹ 0.936 0.244 0.939 2.371 0.994 0.994 R ¹ 0.936 0.990 0.099 0.994 0.991 0.		RMSE	0.011	0.021	0.004	0.002		0.001	0.001
AIC -34.242 -28.965 -41.069 -47.070 -57.522 -6.255 Fizhugh 6,6(1 ⁻¹) 0.567 0.228 0.909 0.768 0.781 0.781 0.781 0.781 0.781 0.781 0.781 0.781 0.781 0.781 0.994 0.994 0.994 0.994 0.994 0.994 0.994 0.994 0.994 0.994 0.991 0.991 0.991 0.991 0.991 0.991 0.991 0.991 0.991 0.991 0.991 0.993 0.791 0.401		NRMSE	0.874	4.254	3.745	3.940		3.209	6.542
Fitzhughk _{ch} (1 ⁻¹)0.8770.2320.4090.7840.7840.7460.7470.7		AIC	-34.242	-28.985	-41.908	-47.070		-57.522	-50.255
n 0.363 0.244 0.993 2.397 1.07 2.161 RA 0.030 0.010 0.004 0.904 0.994 0.994 RMSE 0.101 0.012 0.040 0.901 0.904 0.931 Monomolecular Q 0.3240 -31.95 -39.090 -59.304 -56.52 -34.438 Monomolecular Q 0.001 0.001 0.021 0.405 0.405 0.224 Q 0.001 0.001 0.001 0.002 0.993 0.971 0.931 0.971 0.931 0.971 0.931 0.971 0.931 0.971 0.931 0.015 0.055 0.414 0.52 0.019 0.051 0.051 0.051 0.555 -48.454 Logistic M 0.354 0.975 0.937 0.351 0.414 0.528 0.351 0.414 0.528 0.351 0.414 0.528 0.351 0.414 0.528 0.351 0.415 0.015	Fitzhugh	$k_{CA} (d^{-1})$	0.587	0.292	0.409	0.748		0.478	0.544
Ri RMSE0.9990.9960.9900.9990.9940.993MomonolocularRMSE0.8002.3913.7440.6652.8073.020MonomolocularAC-32.44-3.908-5.903-5.64.38Monomolocularka, (d ⁻¹)0.6110.8000.4110.457-0.4050.328R0.0110.8000.0410.457-0.9320.9710.971RMSE0.9990.9880.9900.9900.9910.9120.911NMSE0.9744.2443.7453.899-35.526-48.434LogisticHm (g 1 ⁻¹ d ⁻¹)0.744-2.6985-39.908-45.153-35.52-48.434LogisticMMSE0.9540.9550.0230.5350.9120.0100.0010.01RMSE0.9580.9770.936-43.626-74.262-32.688-34.626-51.921.93RMSE1.865-32.422-32.688-34.626-48.476-51.021.931.931.931.931.931.931.931.931.931.931.94 </td <td></td> <td>n</td> <td>0.936</td> <td>0.244</td> <td>0.993</td> <td>2.397</td> <td></td> <td>1.307</td> <td>2.316</td>		n	0.936	0.244	0.993	2.397		1.307	2.316
MASE0.0100.0120.0040.0000.0010.001MomonolecularMRMSe0.32.464-31.595-39.304-35.304-56.592-54.38 $A_1(d^{-1})$ 0.6110.0000.0000.0240.0210.0210.0110.011 $A_1(d)$ 0.9990.9860.9900.9900.9020.9930.9910.9930.9910.9910.0110.0210.0120.0100.011 <td< td=""><td></td><td>R^2</td><td>0.999</td><td>0.996</td><td>0.990</td><td>0.999</td><td></td><td>0.994</td><td>0.993</td></td<>		R^2	0.999	0.996	0.990	0.999		0.994	0.993
NMMSE 0.850 2.991 3.744 0.665 2.807 3.024 Monomolecular ACC -3.244 -3.908 -5.934 -5.524 -5.524 Monomolecular A.(a) 0.601 0.000 0.411 0.475 -0.405 0.328 R 0.999 0.988 0.990 0.990 -993 0.971 NMSE 0.974 4.254 3.490 -9.010 0.010 Maspe 0.874 4.254 3.490 -45.153 -95.526 -48.434 Logistic Mage 0.972 0.010 0.012 0.010 0.014 0.014 0.014 0.016 0.014 0.014 0.016 0.015 0.016 0.017 0.016 0.01 0.016 0.017 0.016 0.017 0.016 0.017 0.016 0.017 0.016 0.017 0.016 0.017 0.016 0.017 0.016 0.017 0.016 0.017 0.016 0.017 0.016 0.017 0		RMSE	0.010	0.012	0.004	0.000		0.001	0.001
AIC -32,464 -31,895 -93,908 -53,302 -55,532 -54,438 Monomolecular λ (d) 0,000 0,000 0,024 0,034 0,032 R 0,000 0,000 0,000 0,024 0,035 0,035 0,035 0,937		NRMSE	0.850	2.391	3.744	0.665		2.807	3.020
Monomolecular k _c (d ⁻¹) 0.611 0.800 0.411 0.475 0.405 0.328 k 0.00 0.000 0.000 0.024 0.938 0.970 0.971 R ^A 0.991 0.988 0.900 0.900 0.901 0.933 0.971 MMSE 0.874 4.254 3.475 3.899 -55.526 -48.434 Logistic m.6 t ⁻¹ d ⁻¹ 0.74 -26.985 -39.908 -45.153 -55.526 -48.434 Logistic m.6 t ⁻¹ d ⁻¹ 0.838 0.957 0.937 0.985 0.977 0.985 0.976 0.998 0.997 0.985 0.917 0.985 0.917 0.916 -001 0.917 0.985 0.917 0.918 -011 0.012 0.917 0.918 -011 0.011 0.01 0.011 0.01 0.913 -011 0.913 -011 0.914 1.316 0.917 0.914 1.914 1.914 1.914 1.914 1.914 1.		AIC	-32.464	-31.595	- 39.908	-59.304		-56.592	-54.438
$\lambda_{ch}^{(1)}$ 0.0000.0000.0000.0240.0240.0290.973RMSE0.0110.0210.0900.9900.9930.9710.3076.397RMSE0.8744.2543.7453.899-45.153-55.526-48.434Logistic $\mu_m (g (1^{-1} d^{-1})$ 0.7640.4190.0270.190.0050.051 $\lambda_c(1)$ 0.7640.4190.0270.9550.55.52-98.9580.9770.9850.9570.9370.9510.9570.931 $\lambda_c(1)$ 0.9560.0230.0030.0010.011 <td>Monomolecular</td> <td>$k_{CA} (d^{-1})$</td> <td>0.611</td> <td>0.800</td> <td>0.411</td> <td>0.457</td> <td></td> <td>0.405</td> <td>0.328</td>	Monomolecular	$k_{CA} (d^{-1})$	0.611	0.800	0.411	0.457		0.405	0.328
R ² 0.9990.9880.9000.9000.9010.9100		λ (d)	0.000	0.000	0.000	0.024		0.024	0.079
RNSE 0.011 0.02 0.02 0.011 0.01 NEMSE 0.874 4.254 3.745 3.890 -5.526 -4.843 Logistic $\mu_{m} (g^{1-1} d^{-1})$ 0.764 0.491 0.274 0.191 -5.526 -8.843 Logistic $\mu_{m} (g^{1-1} d^{-1})$ 0.764 0.970 0.917 0.918 -0.154 0.005 R 0.985 0.629 0.010 0.003 0.017 0.985 0.971 0.985 0.971 0.916 0.016 0.016 NMSE 0.985 0.292 0.101 0.002 0.010 0.010 0.011 0.		R ²	0.999	0.988	0.990	0.990		0.993	0.971
INRME 0.874 4.254 3.499 .9.207 6.397 Logistic Ma -32.422 -39.908 -35.133 .9.55.26 .9.43 Logistic μ_{ee} (g l ⁻¹ d ⁻¹) 0.764 0.419 0.027 0.917 .0.95.35 .0.95.4 0.95.35		RMSE	0.011	0.021	0.004	0.002		0.001	0.001
AIC-32.20-20.805-90.908-45.133-55.26-48.43Logistic $\mu_m (g L^{-1} d^{-1})$ 0.7540.0270.0270.0130.0500.053 $\lambda (a)$ 0.8380.9550.0230.5350.1540.9500.981 R^2 0.9850.9970.9970.9850.9770.9850.9770.910NRMSE0.0590.0290.0100.0237.7425.193ARMSE-24.62-24.62-23.284.7197.7420.5012BPK16.65-24.620.2280.508-3.5250.5720.572 $\mu (g L^{-1} d^{-1})$ 0.4810.2150.2820.508-2.1290.508 $\mu_n (g L^{-1} d^{-1})$ 0.4810.2150.2180.0150.2160.216 R^2 0.9900.9880.9900.0270.2160.9010.901 R^2 0.9170.3550.4110.2560.2770.2110.214R0.0140.9900.9880.9020.9140.9140.9140.914R0.9170.2490.9410.010.9140.9140.9140.914R0.9170.9280.9300.4570.9141.9141.914R0.9240.9290.9570.9390.9470.9141.914R0.9240.9290.9570.9390.9470.9141.914R0.9240.9290.9570.939		NRMSE	0.874	4.254	3.745	3.899		3.207	6.397
Logisticµm (g 1^- 1^-).764.049.027.019.009.005.005A(d).0888.955.023.055.058.154.058R ² .0965.097.030.003.011.003.011.011RMSE.056.579.222.471.748.513.153.153AlC.18.65.579.222.471.748.76.513.153 <t< td=""><td></td><td>AIC</td><td>-32.242</td><td>-26.985</td><td>- 39.908</td><td>- 45.153</td><td></td><td>- 55.526</td><td>-48.434</td></t<>		AIC	-32.242	-26.985	- 39.908	- 45.153		- 55.526	-48.434
h A Rtime\begin{t	Logistic	$\mu_{\rm m} \ ({\rm g} \ {\rm L}^{-1} \ {\rm d}^{-1})$	0.764	0.419	0.027	0.019		0.005	0.005
R RMSE0.9570.9370.9480.9580.9570.951RMSE0.0590.0290.0100.0310.0110.0110.011NRMSE4.7685.799.2324.7197.7425.193ACC-18.650-24.262-32.688-43.626-48.4705.012ft (d)1.9481.8412.1712.1382.1932.272ft (d)1.9481.8412.1712.1382.1930.005ft (d)0.3550.4100.2620.0150.0010.021RASE0.9990.9800.9000.9010.9130.961RMSE0.1140.210.040.0210.010.010.01RMSE0.8744.2543.7453.940-5.522-48.255Ref0.9011.3225.0937.9141.80714.5716.542Ref0.9820.9140.953-4.9751-4.52760.934Ref0.9220.9140.9510.935-4.9751-4.5276Ref0.9240.9240.9500.9320.92-9.916Ref0.9240.914-3.062-3.93089.950-4.9751-4.5276Cone1.914-3.1600.9140.9250.921-4.5276-4.5276Ref0.9990.9240.9160.914-4.5276-3.914-4.5276-3.914-4.5276Ref0.9990.9240.9160.9140.914<		λ (d)	0.838	0.955	0.023	0.535		0.154	0.508
BPKNMSE0.0590.0290.0100.030.0100.011NMSE4.7685.9799.3224.7197.7425.133AIC-18.6655.9709.32.688-43.626-48.4765.0102BPKMa0.4570.4040.5290.508-48.4760.578h_a(g.1^-1d^-1)0.4380.2150.0280.1510.0050.0150.005h_a(g.1^-1d^-1)0.3550.4110.2560.2770.9310.9930.993R ² 0.9910.9910.9020.9930.9910.9930.916R ³ 0.9110.0210.0440.0210.9140.9930.916RMSE0.9140.2222.2083.940-45.070-9.55.224.825Second-order10.150.9210.9310.9143.940-55.524.825R0.9210.9320.9910.931-55.524.825R0.9210.9310.9141.8014.5712.9124.912R0.9210.9140.9570.9399.9141.9141.914R0.9210.9141.9021.9141.9141.9141.9141.914R0.9140.9140.9140.9140.9140.9141.9141.914R0.9140.9140.9140.9140.9140.9141.9141.914R0.9140.9140.9140.9140.9140.914 </td <td></td> <td>R²</td> <td>0.985</td> <td>0.977</td> <td>0.937</td> <td>0.985</td> <td></td> <td>0.957</td> <td>0.981</td>		R ²	0.985	0.977	0.937	0.985		0.957	0.981
NRMSE 1.768 5.979 9.232 4.719 7.742 5.133 BPK AIG -3.666 -24.262 -3.2688 -43.626 -48.767 -50.102 BPK man 0.457 0.4262 -3.268 6.3624 -0.48.76 0.503 A(d) 0.457 0.508 0.508 0.508 0.508 2.189 2.272 A(d) 1.948 1.841 2.171 2.138 2.189 2.123 k_{CA} (d ⁻¹) 0.352 0.414 0.256 0.277 0.51 0.501 k_{CA} (d ⁻¹) 0.359 0.998 0.990 0.990 0.991 0.993 0.991 R ² 0.991 0.874 2.521 0.475 3.901 5.912 4.825 Second-order MRSE 0.872 -5.928 -39.908 9.910 5.912 -48.255 Second-order MRSE 0.824 0.929 0.939 0.91 0.93 0.91 0.93 <td< td=""><td></td><td>RMSE</td><td>0.059</td><td>0.029</td><td>0.010</td><td>0.003</td><td></td><td>0.001</td><td>0.001</td></td<>		RMSE	0.059	0.029	0.010	0.003		0.001	0.001
AIC-18.665-24.262-32.688-43.626-48.476-50.102BPKm0.4570.4040.5290.5080.5220.5230.5210.5210.5210.5210.2720.5210.2720.0510		NRMSE	4.768	5.979	9.232	4.719		7.742	5.193
BPKm0.4570.4040.5290.5080.5320.572h0.(d)1.9481.8412.1712.1382.1902.720h(d)0.3550.2150.0280.0150.0510.0510.051k0.3550.4410.2560.2770.5100.2100.011RMS0.0110.0400.0210.9900.9010.0110.011NMSE0.170.2247.6933.9403.2096.5224.523Second-orderk0.8740.5037.9141.6015.2324.523RMSE0.0510.9940.9570.9390.9432.6124.523RMSE0.6520.9441.6079.9390.9432.6120.933RMSE0.6520.9540.9530.9539.4751.2189RMSE0.5270.9541.6040.6520.6321.2189RMSE0.9741.3201.6040.5700.5220.5280.917RMSE0.9940.9510.9630.9930.9171.9294.557RMSE0.9940.9510.9630.9910.9210.9670.9161.9210.967RMSE0.9940.9510.9630.9930.9210.9161.9210.9210.967RMSE0.9940.9510.9630.9930.9210.9210.9210.9210.916RMSE0.9940.9520.963<		AIC	-18.665	-24.262	-32.688	-43.626		-48.476	-50.102
h_0 (d)1.9481.8412.1712.1382.1892.272h_m (g 1^{-1} d^{-1})0.4380.2150.0280.0150.0500.005k_{c,a} (d^{-1})0.3550.4410.2560.2770.2510.210R ² 0.9900.9880.9000.9000.9010.9130.961NMSE0.0110.0210.0400.0220.0100.01NRMSE0.7222.6985-39.908-45.070-55.522-48.255AC-32.242-50.937.91418.07145.7012.6412RMSE0.9820.9940.9050.9320.020.933NMSE0.9820.9940.9050.9390.920.933AC-19.914-31.602-36.188-39.953-49.71-45.276ConeAC ₄ (⁻¹)0.2181.6045.7015.2240.9870.914AC-19.914-31.602-36.188-39.953-49.71-45.276ConeAC ₄ (⁻¹)0.7181.6045.7015.2520.9170.918MMSE0.9990.9950.9330.9990.920.9170.918Modified GompertzH ₁ (g 1 ⁻¹)0.1650.1610.7375.3491-5.4080.015Modified GompertzH ₁ (g 1 ⁻¹)0.5260.2710.0740.9340.910.050.910.95Modified GompertzH ₁ (g 1 ⁻¹)0.5260.2710.0160.310.15 <td>BPK</td> <td>m</td> <td>0.457</td> <td>0.404</td> <td>0.529</td> <td>0.508</td> <td></td> <td>0.532</td> <td>0.578</td>	BPK	m	0.457	0.404	0.529	0.508		0.532	0.578
μm μm (g L ⁻¹ d ⁻¹)0.4380.2150.0280.0150.0050.005kc _A (d ⁻¹)0.3550.4410.2660.2770.9930.996RMSE0.9990.9800.9900.9930.969RMSE0.0110.0210.0040.0020.0010.01NRMSE0.8744.2543.7453.940-555.22-48.255AlC-32.242-26.983-39.908-45.070-55.522-48.255Rk ₂ ," (Lg ⁻¹ d ⁻¹)1.3225.0937.91418.07145.7010.861R0.9620.9940.9570.9390.9480.8610.873RMSE0.0650.150.0080.0050.020.03NMSE0.6533.1602-36.148-39.953-49.75145.276ConeKc _A (d ⁻¹)0.7431.6040.5700.5320.5280.981R0.9990.9959.8930.9990.9890.9870.987NMMSE0.180.0140.050.0110.010.010.01NMSE0.9990.9959.830.9919.8930.9870.987Nodified GompertzMm (g L ⁻¹ d ⁻¹)0.5260.2710.280.0180.050.16Nodified GompertzMm (g L ⁻¹ d ⁻¹)0.5260.2710.280.9830.9910.9830.9910.9810.989Nodified GompertzRMm (g L ⁻¹ d ⁻¹)0.5260.		t ₀ (d)	1.948	1.841	2.171	2.138		2.189	2.272
k C Rk C A0.3550.4410.2560.2770.2510.210R0.9990.9800.9900.9900.9900.9930.9930.9930.9930.9930.9930.9930.9930.9930.9930.9930.9930.9930.9930.9930.9930.9140.0020.9030.9140.5522-48.255Second-orderAC C A C A-32.24-26.985-39.908-45.070-5.522-48.255-84.255-84.251-26.912-26.912-26.9120.9330.914-0.8930.814-26.912-26.912-26.9120.9330.914-0.893-8.912-26.912		$\mu_{\rm m} ({\rm g} {\rm L}^{-1} {\rm d}^{-1})$	0.438	0.215	0.028	0.015		0.005	0.005
R20.9990.9880.9900.9900.9900.9930.969RMSE0.0110.0210.0040.0210.0100.01NRMSE0.8744.2403.7453.940-5.522-48.255Second-order $k_{CA}^{\prime}(1g^{-1}d^{-1})$ 1.3225.0937.91418.0715.522-48.251R20.9820.9940.9570.9390.9420.9320.9430.933RMSE0.5233.0677.6939.5908.47612.189AIC-19.914-31.602-36.148-39.953-49.75145.27Cone $k_{CA}^{(1^-)}$ 0.7431.6040.5700.5220.5280.411n2.2181.6040.5700.5320.5280.9140.914n0.9990.9950.9830.9910.9810.9810.9910.914Modified Gompertz $\mu_{n}^{c1}(1^{-1})$ 0.5260.7140.0280.9140.0510.0110.010.011AG0.9240.9260.9300.9700.9180.9150.9150.9180.9150.9180.9150.918Modified Gompertz $\mu_{n}^{c1}(1^{-1}(1^{-1})$ 0.5260.2710.0280.9180.9150.9180.9150.9180.9150.9180.9180.9150.9180.9150.9180.9150.9180.9150.9180.9180.9150.9180.9150.9180.9150.9180.918 <td< td=""><td></td><td>$k_{CA} (d^{-1})$</td><td>0.355</td><td>0.441</td><td>0.256</td><td>0.277</td><td></td><td>0.251</td><td>0.210</td></td<>		$k_{CA} (d^{-1})$	0.355	0.441	0.256	0.277		0.251	0.210
RMSE0.0110.0210.0040.0020.0010.001NRMSE0.8744.2543.7453.9403.2096.542AlC-32.242-26.985-39.908-45.070-55.526.742Second-order $k_{\alpha}^{\prime}(r, g^{-1} d^{-1})$ 1.3225.0937.91418.07145.7016.612R ² 0.9820.9940.9570.9390.9480.8930.9480.893RMSE0.0650.0150.0080.0050.020.031ARMS2.3773.602-36.148-39.953-49.751-45.276ConeAIC-19.914-31.602-36.148-39.953-49.751-45.276RMSE0.9940.9570.5320.5280.9110.912RMSE0.9141.8061.8402.7872.0782.455R ² 0.9990.9950.9830.9990.9010.9110.011RMSE0.0180.0280.0180.0010.0110.0110.011Modified Gompertz $\mu_{m} g L^{-1} d^{-1}$ 0.5260.2710.77.949-53.491-54.085-51.699RMSE0.9920.9800.9950.0150.0150.0150.0150.1150.115RMSE0.9240.9800.9700.9830.9830.9830.9830.9830.9810.989RMSE0.9240.9260.0260.0160.3730.1150.1150.1150.115 <tr< td=""><td></td><td>R²</td><td>0.999</td><td>0.988</td><td>0.990</td><td>0.990</td><td></td><td>0.993</td><td>0.969</td></tr<>		R ²	0.999	0.988	0.990	0.990		0.993	0.969
NRMSE0.8744.2543.7453.9403.2096.542AC-32.242-26.955-39.908-45.070-55.522-48.255Second-order $k_{CA}^{-1}(Lg^{-1}d^{-1})$ 1.3225.0337.91418.0706.70126.12RASE0.9820.9940.9570.9390.9480.823RMSE0.0650.1550.0080.0050.020.031ARSE-19.914-31.602-36.148-39.9534.761-45.276ConeAC-19.914-31.602-36.148-39.9530.9210.411AR-19.914-31.602-36.148-39.9530.9210.9214.576ConeAC-19.914-31.602-36.148-39.9530.9210.411AR-19.914-31.6020.5700.5220.9210.981AR0.9990.9950.9830.9990.9210.916RAG0.1411.0641.8402.7872.0782.455RASE0.1860.0140.0550.0140.0110.011Ndiffed GompertzHag L ⁻¹ d ⁻¹ 0.5260.2740.2760.1630.3730.1150.051AG0.9240.9920.9800.9700.9810.9830.9810.9810.981Modified GompertzHag L ⁻¹ d ⁻¹ 0.5260.9800.0700.9160.9160.9160.916AG0.9240.9820.9800.9700.9		RMSE	0.011	0.021	0.004	0.002		0.001	0.001
AIC -32.242 -26.985 -39.908 -45.070 -55.522 -48.253 Second-order $k_{CA}^{\prime}(1g^{-1}d^{-1})$ 1.322 5.093 7.914 18.071 45.701 26.412 R^2 0.982 0.994 0.957 0.939 0.948 0.803 0.02 0.933 RMSE 0.652 0.015 0.008 0.02 0.02 0.933 0.946 0.933 AIC -19.914 -31.602 -36.148 -39.953 -49.751 -45.276 Cone $k_{CA}(d^{-1})$ 0.743 1.604 0.570 0.532 0.528 0.411 n 2.218 1.306 1.840 2.787 2.078 2.455 R^2 0.999 0.995 0.983 0.999 0.989 0.981 0.971 NMMSE 1.465 2.841 4.783 1.375 3.877 4.253 Modified Gompertz $\mu_m (g L^{-1} d^{-1})$ 0.526 0.271 0.028 0.018 0.051 0.051 $A(d)$ 0.274 0.276 0.164 0.373 0.115 0.115 0.115 R^2 0.992 0.980 0.970 0.91 0.01 0.01 0.01 $RMSE$ 0.422 0.274 0.276 0.016 0.373 0.115 0.01 RAC 0.992 0.980 0.970 0.91 0.01 0.01 0.01 $RMSE$ 0.422 0.274 0.276 0.07 0.01 0.0		NRMSE	0.874	4.254	3.745	3.940		3.209	6.542
Second-order $k_{CA}" (l. g^{-1} d^{-1})$ 1.3225.0937.91418.07145.70126.412 R^2 0.9820.9940.9570.9390.9480.893RMSE0.0650.0150.0080.0050.0020.003NRMSE5.2373.0677.6939.5908.47612.189AIC-19.914-31.602-36.148-39.953-49.751-45.276Cone $k_{CA} (d^{-1})$ 0.7431.6040.5700.5320.5280.411n2.2181.3061.8402.7872.0782.455R^20.9990.9950.9830.9990.9890.987MSE0.180.0140.0050.0110.0140.011NRMSE1.4652.8414.7831.3753.8774.253AIC-28.106-30.215-37.949-53.491-54.008-51.699Modified Gompertz $\mu_m (g l^{-1} d^{-1})$ 0.5260.2710.0280.0180.0050.095A(d)0.2740.2760.0160.3730.1150.1150.156RMSE0.9920.9800.9970.9980.9830.9830.9830.983Modified Gompertz $\mu_m (g l^{-1} d^{-1})$ 0.5260.2710.0260.160.3730.1150.115RMSE0.9920.9800.9700.9980.9830.9830.9830.9830.9830.9830.983RMSE0.922<		AIC	-32.242	-26.985	- 39.908	-45.070		- 55.522	-48.255
R²0.9820.9940.9570.9390.9480.893RMSE0.0650.0150.0080.0050.0020.003NRMSE5.2373.0677.6939.5908.47612.189AIC-19.914-31.602-36.148-39.953-49.751-45.276k _{CA} (d ⁻¹)0.7431.6040.5700.5320.9780.411R2.2181.3061.8402.7872.0782.455R ² 0.9990.9950.9830.9990.9890.987RMSE0.0180.0140.0050.0110.0010.001NRMSE1.4652.8414.7831.3753.8774.253AIC-28.106-30.215-37.949-53.491-54.008-51.699Modified Gompertzµm (g L ⁻¹ d ⁻¹)0.5260.2710.0280.0180.0050.015R0.9920.9800.9700.9980.9830.9890.9890.989RMSE0.0420.270.0070.0110.0110.0110.011RMSE0.4220.9800.9700.9980.9810.9830.983RMSE0.0420.270.0070.0110.0010.0110.011RMSE0.420.270.070.0110.0110.0110.011RMSE0.420.5876.4391.6874.8483.887R0.9990.5876.4391.6874.92.21-5	Second-order	k_{CA} " (L g ⁻¹ d ⁻¹)	1.322	5.093	7.914	18.071	45.701		26.412
RMSE0.0650.0150.0080.0050.0020.003NRMSE5.2373.0677.6939.5908.47612.189AlC-19.914-31.602-36.148-39.953-49.751-45.276 k_{CA} (d ⁻¹)0.7431.6040.5700.5320.5280.411n2.2181.3061.8402.7872.0782.455R ² 0.9900.9950.9830.9990.9870.987NMSE0.0180.0140.0050.0010.0010.001NRMSE1.4652.8414.7831.3753.8774.253AIC-28.106-30.215-37.949-53.491-54.008-51.699Modified Gompertz μ_m (g L ⁻¹ d ⁻¹)0.5260.2710.0280.0180.0050.005 λ (d)0.2740.2760.0160.3730.1150.1150.115 R^2 0.9920.8020.9800.9920.9800.9830.989Nodified Gompertz μ_m (g L ⁻¹ d ⁻¹)0.5260.2710.0280.1830.1050.115 R^2 0.9920.8020.9800.9920.9800.9830.9920.9830.989Nodified Gompertz μ_m (g L ⁻¹ d ⁻¹)0.5260.2710.0160.0110.0110.015 R^2 0.9920.8020.9800.9920.9800.9810.9160.9160.9160.916 R^2 0.9920.981		R ²	0.982	0.994	0.957	0.939	0.948		0.893
NRMSE5.2373.0677.6939.5908.47612.189AIC -19.914 -31.602 -36.148 -39.953 -49.751 -45.276 Cone k_{CA} (d^{-1}) 0.743 1.604 0.570 0.522 0.528 0.411 n 2.218 1.306 1.840 2.787 2.078 2.455 R^2 0.990 0.995 0.983 0.999 0.996 0.987 MSE 0.118 0.014 0.001 0.001 0.001 NRMSE 1.465 2.841 4.783 1.375 3.877 4.253 AIC -28.106 -30.215 -37.949 -53.491 -54.008 -51.699 Modified Gompertz μ_m (g $L^{-1} d^{-1}$) 0.526 0.271 0.028 0.018 0.005 0.005 R^2 0.992 0.802 0.970 0.983 0.983 0.989 0.983 R_4 0.974 0.276 0.070 0.011 0.011 0.011 R^2 0.992 0.802 0.970 0.981 0.981 0.981 R_4 0.920 0.970 0.910 0.001 0.001 0.001 R_4 0.920 0.920 0.970 0.910 0.011 0.011 R_4 0.920 0.920 0.970 0.910 0.011 0.011 R_4 0.920 0.920 0.970 0.910 0.011 0.011 R_4 0.920 0.920 $0.$		RMSE	0.065	0.015	0.008	0.005	0.002		0.003
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$		NRMSE	5.237	3.067	7.693	9.590	8.476		12.189
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$		AIC	-19.914	-31.602	-36.148	- 39.953	- 49.751		-45.276
$ \begin{array}{llllllllllllllllllllllllllllllllllll$	Cone	$k_{CA} (d^{-1})$	0.743	1.604	0.570	0.532	0.528		0.411
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$		n	2.218	1.306	1.840	2.787	2.078		2.455
RMSE 0.018 0.014 0.005 0.001 0.001 0.001 NRMSE 1.465 2.841 4.783 1.375 3.877 4.253 AIC -28.106 -30.215 -37.949 -53.491 -54.008 -51.699 Modified Gompertz μm (g L ⁻¹ d ⁻¹) 0.526 0.271 0.028 0.018 0.005 0.005 λ (d) 0.274 0.276 0.016 0.373 0.115 0.115 R ² 0.992 0.980 0.970 0.998 0.983 0.989 RMSE 0.42 0.27 0.007 0.011 0.001 0.001 NMMSE 3.390 5.587 6.439 1.687 4.848 3.887 AIC -21.394 -24.805 -35.571 -51.854 -52.221 -52.420		R ²	0.999	0.995	0.983	0.999	0.989		0.987
NRMSE 1.465 2.841 4.783 1.375 3.877 4.253 AIC -28.106 -30.215 -37.949 -53.491 -54.008 -51.699 Modified Gompertz μ_m (g L ⁻¹ d ⁻¹) 0.526 0.271 0.028 0.018 0.005 0.005 λ (d) 0.274 0.276 0.016 0.373 0.115 0.115 R ² 0.992 0.980 0.970 0.9983 0.989 0.989 MSE 0.042 0.27 0.007 0.01 0.001 0.001 NRMSE 3.390 5.587 6.439 1.687 4.848 3.887 AIC -21.394 -24.805 -35.571 -51.854 -52.221 -52.420		RMSE	0.018	0.014	0.005	0.001	0.001		0.001
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$		NRMSE	1.465	2.841	4.783	1.375	3.877		4.253
$ \begin{array}{llllllllllllllllllllllllllllllllllll$		AIC	-28.106	-30.215	- 37.949	-53.491	-54.008		-51.699
Å. (d) 0.274 0.276 0.016 0.373 0.115 0.115 R ² 0.992 0.980 0.970 0.998 0.983 0.989 RMSE 0.042 .027 0.007 0.001 0.001 0.001 NRMSE 3.390 5.587 6.439 1.687 4.848 3.887 AIC -21.394 -24.805 -35.571 -51.854 -52.221 -52.420	Modified Gompertz	$\mu_{\rm m}$ (g L ⁻¹ d ⁻¹)	0.526	0.271	0.028	0.018	0.005		0.005
R ² 0.992 0.980 0.970 0.998 0.983 0.989 RMSE 0.042 .027 0.007 0.001 0.001 0.001 NRMSE 3.390 5.587 6.439 1.687 4.848 3.887 AIC -21.394 -24.805 -35.571 -51.854 -52.221 -52.420	-	λ (d)	0.274	0.276	0.016	0.373	0.115		0.115
RMSE0.042.0270.0070.0010.0010.001NRMSE3.3905.5876.4391.6874.8483.887AIC-21.394-24.805-35.571-51.854-52.221-52.420		R ²	0.992	0.980	0.970	0.998	0.983		0.989
NRMSE 3.390 5.587 6.439 1.687 4.848 3.887 AIC -21.394 -24.805 -35.571 -51.854 -52.221 -52.420		RMSE	0.042	.027	0.007	0.001	0.001		0.001
AIC -21.394 -24.805 -35.571 -51.854 -52.221 -52.420		NRMSE	3.390	5.587	6.439	1.687	4.848		3.887
		AIC	-21.394	-24.805	-35.571	-51.854	-52.221		-52.420

Legend: k_{CA} : first-order CA production rate constant, k_{CA} ": second-order CA production rate constant; n: form constant; λ : lag phase time; μ_m : maximum CA productivity; m: constant of the BPK model; R^2 : coefficient of determination; RMSE: roof mean square error; NRMSE: normalized roof mean square error; AIC: Akaike Information Criteria.

(Monomolecular) estimated $\lambda = 0.00$ d. The form factor n of the Fitzhugh (n = 0.69 ± 0.33) and Cone (n = 1.91 ± 0.30) model indicates that there was a lag period related to CA production, although short (Table 7). Nevertheless, it can be concluded that the lag phase in relation to acid COD production from DW is quite short, which is desirable in biotechnological processes since the start-up time treating DW for product recovery would be small. Discrepancies between values may be related to the parameters used in each mathematical equation.

Another important parameter that has been estimated by the three models (Modified Gompertz, Logistic and BPK) is the maximum productivity rate (μ_m). The highest production rate was estimated by the BPK model ($\mu_m = 1.83 \pm 0.28$ gCOD L⁻¹ d⁻¹), while the lowest was found by the Modified Gompertz model ($\mu_m = 0.98 \pm 0.11$ gCOD L⁻¹ d⁻¹). The Logistic model provided intermediate productivity between the values estimated by the other two previous models ($\mu_m = 1.29 \pm 0.18$ gCOD L⁻¹ d⁻¹).

The best models to simulate individual CA production from DW were: First-order model for HAc, HBu, and HVa; Second-order model

for HPr; and Fitzhugh model for i-HVa and HCa (Table 8). There was a satisfactory visual adjustment of all models to the CA progression curve over time (Fig. 3), with an emphasis on the HAc curve (Fig. 3A), described optimally by the First-order model ($R^2 = 0.999$ and AIC = -34.242), and for the i-HVa curve (Fig. 3D), which was perfectly described by the Fitzhugh model ($R^2 = 0.999$ and AIC = -59.304).

Considering the models that best fit the experimental data, the first order product formation rate constant (k_{CA}), which could be estimated from both First-order and Fitzhugh models, was higher for i-HVa ($k_{CA} = 0.748 \text{ d}^{-1}$, Fitzhugh model) and smaller for HVa ($k_{CA} = 0.401 \text{ d}^{-1}$, First-order model). HAc, HBu, and HCa presented intermediate values, with k_{CA} equal to 0.611; 0.411 and 0.544 d^{-1} , respectively. Although CA production was characterized by first-order kinetics, the Second-order model was better adjusted to HPr production, and the second-order rate constant (k_{CA} ") was 5.093 L g⁻¹ d⁻¹. Such value cannot be directly compared with k_{CA} of the other acids because it has a different unit.

Maximum productivity rate (µm) could be estimated by three



Fig. 3. Kinetic modeling of the individual production of carboxylic acids from the fermentative assays using dairy wastewater as substrate. A. HAc. B. HPr. C. HBu. D. i-HVa, E. HVa. F. HCa.

models (Modified Gompertz, Logistic and BPK). The values that most closely approximated to the real maximum productivity calculated from the concentration data obtained on the collection days (Table 5, Section 3.2) were, in mg L⁻¹ d⁻¹, 438 (BPK model); 215 (BPK model); 28 (Modified Gompertz model); 15 (BPK model); 5 (BPK model) and 5 (BPK model), for HAc, HPr, HBu, i-HVa, HVa and HCa, respectively, and the BPK model estimated this parameter more satisfactorily. Lag phase lower than one day to start the production of all acids indicated that the microorganisms quickly used the substrate for CA production, as discussed for the production curve of acid in terms of COD (Fig. 2).

4. Conclusions

The tests showed that DW is a readily fermentable substrate to acidogenic microorganisms because it presents high rates of short-chain CA formation in the first two days of the experiment. The low concentrations of medium-chain CA found indicate that fats and proteins did not function as the main carbon source for DW fermentation. However, HCa was produced without the external addition of electron donors. The yield obtained was 0.66 mgCA mgCOD_A⁻¹, which corresponds to 0.83 mgCOD_{CA} mgCOD_A⁻¹. Models that describe an exponential phase are the most suitable for the simulation of CA

production. Therefore, DW appears to be a high potential substrate for producing added-value products such as short-chain and medium-chain carboxylic acids.

Declaration of Competing Interests

The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.

Author contribution statement

Milena Maciel Holanda Coelho: helped the experiments during the undergraduate studies on the Biotechnology Major at Federal University of Ceará.

Naassom Wagner Sales Morais: performed the experiments during his master's study at the Civil Enginnering Program at the Federal University of Ceará.

Erlon Lopes Pereira: Assistant professor Federal University of Ceará and co-supervisor of the students.

Renato Carrhá Leitão: part of the analysis was performed at Embrapa and he helped in the experiment planning and discussion of the results.

André Bezerra dos Santos: was the supervisor of the students and leader of the Environmental Technology group at the Federal University of Ceará.

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