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Phase quantification in nanobainite via magnetic measurements and X-ray diffraction

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Abstract

Accurate phase quantification of nanostructured bainitic steel is of importance because of the nature of its percolating structure that controls many of its mechanical properties. X-ray diffraction is the technique of choice for such analysis, but magnetic methods can be more rapid and less sensitive to defect structures. In this study, the phase volume fractions measured using both of these techniques for the specific mixtures associated with nanostructured bainite have been compared and contrasted. An expression which relates the volume fraction and the saturation magnetisation is obtained and its form is found to be consistent with previous work done on duplex stainless steels and TRIP steels. The fitting constants used in many of such analyses vary significantly so an attempt is made to rationalise the differences by considering the factors that determine the intrinsic saturation magnetisation of ferrite.

Keywords: nanostructured bainite, phase quantification, saturation magnetisation, X-ray diffraction

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1. Introduction

Nanostructured bainite contains an extremely fine mixture of ferrite and austenite. The ability of the austenite to percolate the steel dictates amongst other factors, the ductility [1] and its resistance to the diffusion of hydrogen through the two-phase mixture [2]. Given the specific austenite morphology characteristic of nanostructured bainite, there is a critical threshold of austenite fraction below which the material fractures during tensile loading [3], and the austenite also ceases to be effective as a barrier to hydrogen ingress [2].

There are many methods to determine the retained austenite content [4–8], each of which has limitations that have been discussed extensively [9, 10]. Diffraction using X-rays or neutrons has the advantage of rigour in the analysis of data and remains the method of choice for phase fraction analysis. However, magnetic methods to determine volume fractions can be rapid to implement even though they may require calibration. One difficulty is that the calibration constants seem to vary widely as a function of the alloy composition and microstructure [11–16]. In the present work we investigate X-ray diffraction and magnetic detection of retained austenite in nanostructured bainitic steel, and attempt to clarify the nature of the calibration function required for the magnetic technique. Given that there are now several commercial applications and numerous research programmes associated with this structure, it would be useful to have an easy method to characterise the retained austenite content with confidence.

2. Experimental Methods

2.1. Material

All alloys used were cast as 25-50 kg ingots, which were then reduced 50% via hot forging. The chemical compositions are presented in table 1.

2.2. Heat treatments

The heat treatment of small samples cut via electrical-discharge machining included homogenisation at 1200°C for 2 days and furnace cooling,

Table 1: Chemical composition, wt%, of the alloys used.

Alloy	C	Si	Mn	Cr	Mo	Ni	V	Co	P	S	Al
A	0.79	1.59	1.94	1.33	0.30	0.02	0.11	-	<0.005	-	-
B	0.80	1.59	2.01	1.00	0.24	-	-	1.51	0.002	0.002	-
C	0.79	1.56	1.98	1.01	0.24	-	-	1.51	0.002	0.002	1.01
D	0.78	1.60	2.02	1.01	0.24	-	-	3.87	0.002	0.002	1.37

austenitisation in the γ region (900-1000 °C) for 15 min and air cooling, bainitic transformation at different temperatures and times (table 2) before being quenched in water at room temperature, and in some cases tempering also for different times and temperatures. For the two heat treatments prior to the bainitic transformation, samples were sealed in quartz tubes back-filled with argon or in a vacuum furnace. Cooling slowly through the 700-550 °C range, following homogenisation, was used to ensure pearlite formation and avoid martensite, which would induce quench cracks [17]. Extensive characterisation by X-ray diffraction and microscopy in these and similar conditions has been reported previously [18–22].

The main three parameters that determine the quantity of the ferromagnetic ferrite present are the mass, chemical composition, and the heat treatment of the samples. Therefore, the magnetisation was studied by altering only one of these three parameters at a time in order to separate out their individual contributions. For example, samples 6 and 7 have different compositions but constant heat treatment and approximately constant mass; samples 8, 9 and 10 have different mass but constant composition and heat treatment; samples 3 and 4 have different heat treatment but constant composition and approximately constant mass; and finally samples 1 and 2 have no variation, meaning constant heat treatment, composition, and very similar mass.

2.3. X-ray diffraction

Samples were polished to a 1 μm finish, etched with 2% Nital and analysed with X-ray diffraction (XRD) to measure the volume fractions of bainitic ferrite and retained austenite using a *Philips* PW1830 vertical diffractometer with unfiltered CuK_α radiation. Scans were performed with an acceleration voltage and current of 40 kV and 40 mA from 40 to 125 °, with a step size of

Table 2: Heat treatments performed on different samples. The weight column corresponds to the final sample geometry of thin discs used for TEM and magnetic measurements.

Sample	Alloy	Weight / g	Isothermal transformation		Tempering	
			Temperature / °C	Time	Temperature / °C	Time
1	A	0.01135	200	10 days	-	-
2	A	0.01065	200	10 days	-	-
3	A	0.00965	200	10 days	400	1 h
4	A	0.0089	200	10 days	500	1 h
5	B	0.00405	150	1 year	-	-
6	B	0.00395	200	4 days	-	-
7	C	0.0036	200	4 days	-	-
8	D	0.0099	200	4 days	-	-
9	D	0.0064	200	4 days	-	-
10	D	0.01235	200	4 days	-	-

0.05° and a dwell time of 26 s. A divergence slit of 0.5°, an anti-scatter slit of 0.5°, and a receiving slit of 0.2 mm were used to restrict the beam size and the counts obtained. The volume fractions of ferrite and austenite were derived using *HighScore Plus* and the Rietveld refinement method.

2.4. Transmission electron microscopy

Samples were cut into thin slices 250 µm thick using a silicon carbide cutting wheel and ground down to 40-100 µm using 1200 silicon carbide grinding paper. These thin discs of 0.3 mm in diameter were then electropolished using a twin jet polishing machine and a solution of 80% ethanol, 15% glycerol, and 5% perchloric acid with voltages between 20-40 V. Samples were observed in a JEOL 200 CX with an accelerating voltage of 200 kV.

2.5. Vibrating sample magnetometer

The magnetisation and coercive field of the different samples were measured at room temperature using the TEM discs prior to electropolishing with a VSM EGG-PAR model 4500 with a maximum applied field of 600 kA m⁻¹ and total measuring time of 25 min. These conditions were chosen in order to be able to compare the results to XRD volume fractions and to other magnetic measurements in the literature, which were mostly performed at room temperature. This study concentrates only on dual phase systems, but

it should be noted that for the tempered samples additional measurements could be performed above the Curie temperature of cementite (480 K) without affecting the structure in order to obtain information about the carbide phase fractions.

3. Results and discussion

Given the similarity in heat treatments and expected nanostructure, only some representative samples were studied using TEM. The images obtained are presented in fig. 1. For the sake of brevity, samples from here onwards are referred to as X-T^{isotrans}-t^{isotrans}-T^{temper}-t^{temper}-Y, where X is the alloy type, T stands for the temperature in [°C], t is the time in hours [h], days [d], or years [y], and Y is the sample number in case of there being more than one with the same composition and heat treatment.

The stereologically corrected bainitic plate size of some untempered samples was determined using the mean width in the direction normal to the plate length. For sample 1 (A-200C-10d-1) and 2 (A-200C-10d-2) the mean thickness is 39 ± 1 nm and for sample 5 (B-150C-1y) it is 51 ± 4 nm [18].

The volume fraction of retained austenite obtained via Rietveld analysis of the complete XRD spectra (including overlapping peaks) is presented in table 3 along with the values of saturation magnetisation per unit mass obtained at the maximum applied field and the effective field corrected by the demagnetisation factor corresponding to shape (thickness) of each sample [23]. The magnetisation curves are presented in fig. 2.

It can be seen from table 3 that tempering at 500 °C for 1 h decomposed all the retained austenite and left behind a completely ferritic structure, as confirmed by the TEM image of fig. 1b. It is therefore not surprising that this sample displayed the highest specific saturation magnetisation. By plotting the measured volume fraction of bainitic ferrite V_{α_b} against the specific saturation magnetisation m_s (fig. 3), it was possible to perform a linear fit which yields the following equation

$$V_{\alpha_b} = 0.0054 m_s - 0.015 \quad (1)$$

The small value of the y-intercept confirms the fact that the magnetisation of a completely austenitic sample should be approximately zero [14], so the

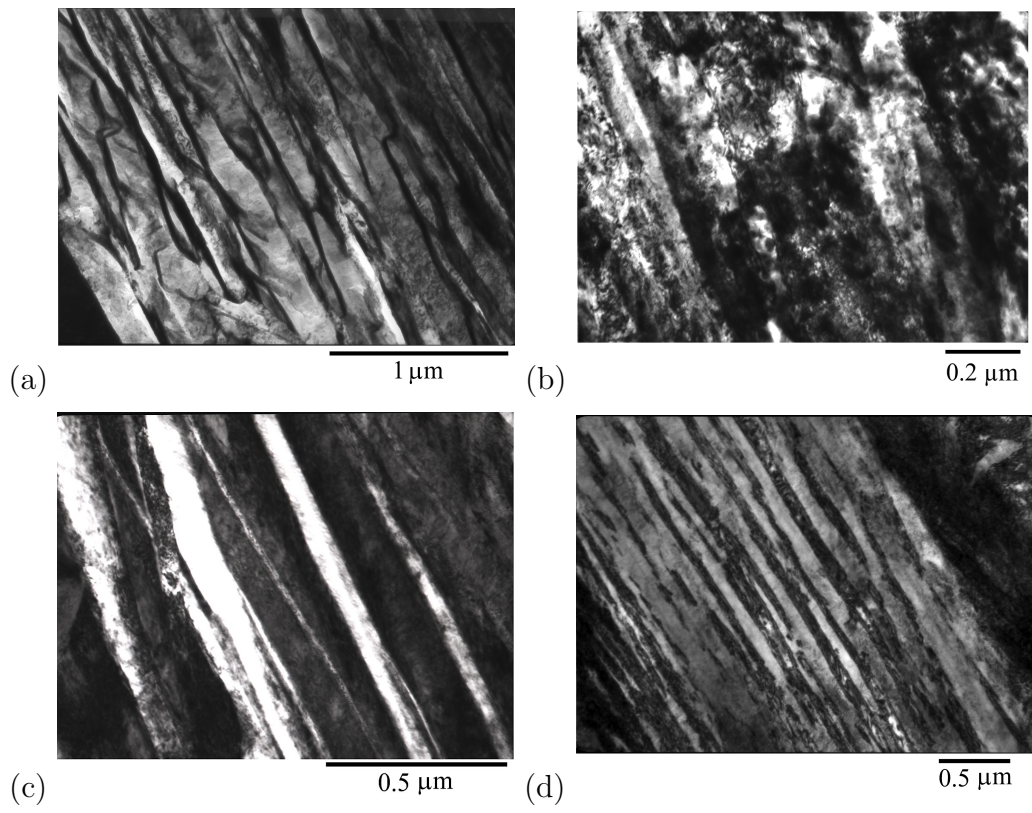


Figure 1: TEM micrographs of samples: a) 3 (A-200C-10d-400C-1h), b) 4 (A-200C-10d-500C-1h), c) 5 (B-150C-1y), and d) 8 (D-200C-4d-1).

Table 3: Volume fraction of retained austenite V_γ , saturation magnetisation m_s , and effective field H_{eff} for each sample. The error to all volume fractions is ± 0.01 and for all magnetisation measurements, ± 1 . For the analysis, only bainitic ferrite and austenite were considered, although the structure will contain carbides after tempering.

Sample	V_γ	$m_s / \text{A m}^2 \text{kg}^{-1}$	$H_{\text{eff}} / \text{kA m}^{-1}$
1 A-200C-10d-1	0.215	149.4	167.6
2 A-200C-10d-2	0.215	149.2	168
3 A-200C-10d-400C-1h	0.161	152.7	168.5
4 A-200C-10d-500C-1h	0	184.9	167.6
5 B-150C-1y	0.204	154.3	172.1
6 B-200C-4d	0.192	145.5	172.3
7 C-200C-4d	0.171	163.1	172.3
8 D-200C-4d-1	0.233	147.7	168.5
9 D-200C-4d-2	0.233	150.1	170.7
10 D-200C-4d-3	0.233	143.0	167.3

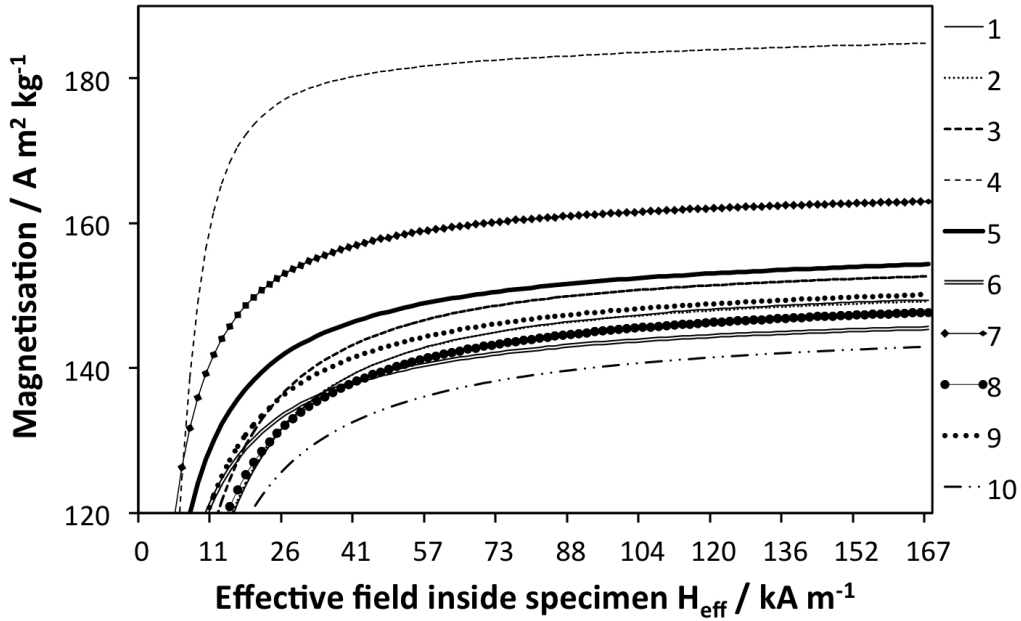


Figure 2: Magnetisation curves for each sample.

equation can be rewritten as

$$V_{\alpha_b} = \frac{m_s}{185.2} \quad (2)$$

The value $185.2 \text{ A m}^2 \text{ kg}^{-1}$ represents the intrinsic saturation magnetisation of ferrite (M_s) with an average of the compositions in table 1, which is in close agreement with the measured magnetisation of $184.9 \text{ A m}^2 \text{ kg}^{-1}$ for sample 4 (A-200C-10d-500C-1h).

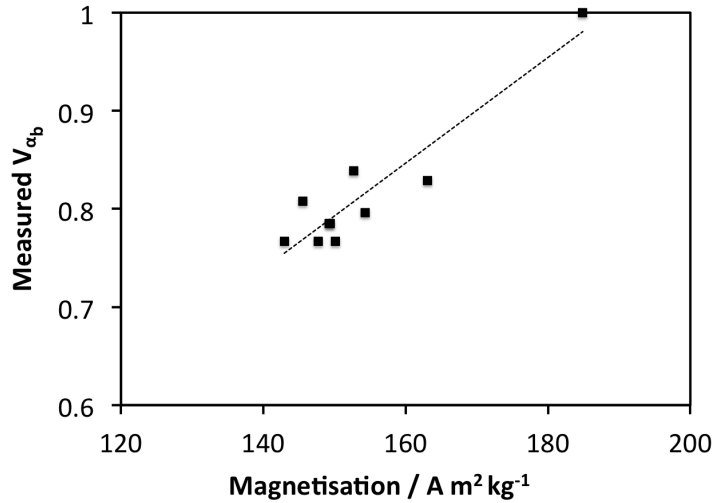


Figure 3: Measured volume fraction of bainitic ferrite and saturation magnetisation.

By using equation 2, it is possible to plot the expected volume fraction of bainitic ferrite for all samples against the measured value. As seen in fig. 4, 70% of the measured values lie within the error bars of the calculated value despite slight compositional variations. The error bars of the measured values all correspond to 0.01 given by the generally achieved accuracy of the Rietveld refinement method using *High Score Plus*, whilst the error bars of the calculated values were determined by

$$\delta V_{\alpha_b} = 0.005423 \delta m_s + 0.000137 m_s \quad (3)$$

where 0.005423 is the average of the V_{α_b}/m_s ratio of all samples and 0.000137 is its standard error, as described in [14].

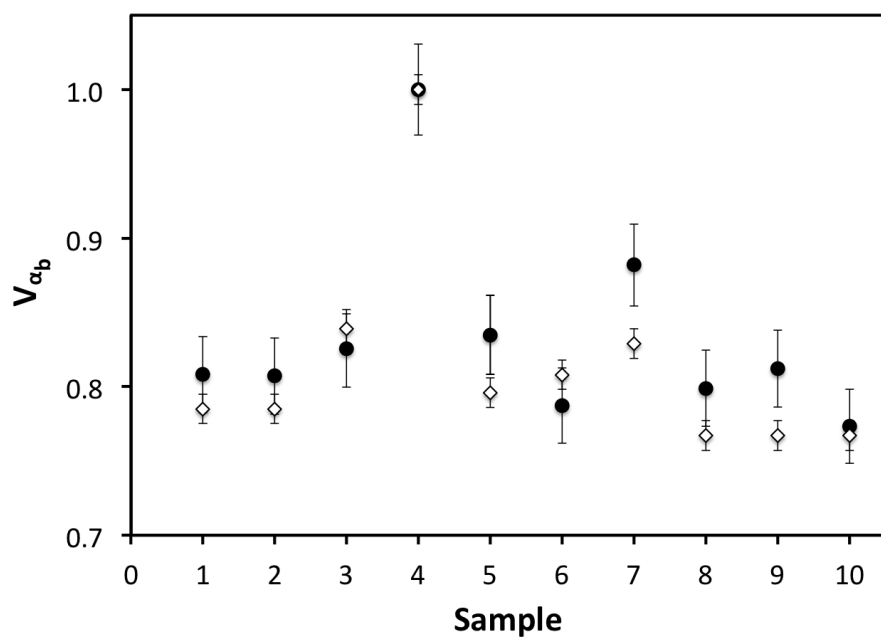


Figure 4: Measured volume fraction of ferrite via diffraction (black dots) compared with the calculated value (white diamond) using the proposed equation.

The fact that the ferrite volume fraction of sample 5 (B-150C-1y), 7 (C-200C-4d) and 9 (D-200C-4d-2) cannot be accurately predicted is not clear as it could not be attributed to either the mass of the sample, the chemical composition, or the heat treatment. It is possible nevertheless that since magnetic measurements were performed on TEM samples, the nanostructure was not homogenous for such sample size or there was stress induced transformation of the retained austenite to martensite. Recent research has shown that even after significant cycling stressing, the austenite films of nanostructured bainite in the regions of maximum subsurface shear stress do not stress transform to martensite [24]. Nevertheless, less stable blocky austenite regions could in principle transform to martensite during thin disc sample preparation distorting volume fraction measurements. Ion milling of the samples would reduce this effect, but given the cost and time associated with it, standard TEM sample preparation was chosen knowing that the affected region caused by the final grinding step with 1200 grit is $\sim 26 \mu\text{m}$ for both sides, which corresponds to $\sim 10\text{-}40\%$ of the sample volume depending on the different specimen thickness. Analysis of samples 8, 9, and 10 that have the same composition and heat treatment but different thickness (178, 155, and 222 μm respectively) confirms that the thinnest sample has the highest magnetisation and thus the highest ferrite content ($150.1 \text{ A m}^2 \text{ kg}^{-1}$) and the thickest one, the lowest ($143.0 \text{ A m}^2 \text{ kg}^{-1}$) that could in part be because the region of possible stress transformation of austenite to martensite is a larger percentage of the whole sample. Although sample preparation is a variable that could lead to further improvement of the accuracy of magnetic phase quantification, the different magnetisation values for samples 8-10 still lie within the error estimated.

A variety of values have been found for the intrinsic saturation magnetisation of ferrite in different steels (saturation magnetisation of samples containing virtually no austenite), but no quantitative explanations of such difference have been presented in the literature to date. Here, a simple calculation was performed to estimate this quantity based solely on the chemical composition of the alloy

$$M_s^{\text{calc}} = k \frac{\sum m_s^i x_i}{\sum x_i} \quad (4)$$

Since only iron ($m_s^{\text{Fe}}=218 \text{ A m}^2 \text{ kg}^{-1}$), cobalt ($m_s^{\text{Co}}=159 \text{ A m}^2 \text{ kg}^{-1}$), and nickel ($m_s^{\text{Ni}}=54.4 \text{ A m}^2 \text{ kg}^{-1}$) are ferromagnetic at room temperature, m_s for all

other elements was taken as $0 \text{ A m}^2 \text{ kg}^{-1}$ [25]. x is the weight percent of each element and k is a correction factor that will be discussed later. The results of this calculation for different alloys in contrast with the measured values are presented in table 4.

Table 4: Measured (M_s^{exp}) and calculated (M_s^{calc}) intrinsic saturation magnetisation of ferrite for different alloys, except for the ones marked with † which are martensitic. Magnetic measurements were performed at room temperature (temperature not stated in those marked with *). The chemical composition of each alloy is shown in wt%.

Name	$M_s^{\text{exp}} / \text{A m}^2 \text{ kg}^{-1}$	$M_s^{\text{calc}} / \text{A m}^2 \text{ kg}^{-1}$	Fe	C	Si	Mn	Cr	Mo	Ni	V	Co	P	S	N	Nb	Ti	Al
Superduplex stainless UNS S32750 [14]	128	142.1	63.523	0.02	0.34	0.83	24.57	3.75	6.68	-	-	0.026	0.001	0.26	-	-	-
Duplex stainless UNS S39205 [13]	133*	154.5	69.575	0.032	-	-	22.38	2.55	5.32	-	-	0.028	0.003	0.1123	-	-	-
304 stainless [26]	160.4*†	160.2	71.299	0.07	0.72	1.32	18.03	-	8.46	-	0.08	0.015	0.006	-	-	-	-
Superbainite (Alloy A)	184.9	204.7	93.915	0.79	1.59	1.94	1.33	0.30	0.02	0.11	-	0.005	-	-	-	-	-
300 maraging steel [16]	188	170.4	66.93	0.01	-	-	-	4.96	17.86	-	9.31	-	-	-	-	0.79	0.14
TRIP (A11.4P) [12]	189.5	211.2	96.87	0.18	0.02	1.52	-	-	-	-	-	0.005	-	0.004	-	-	1.4
TRIP (A11.8) [12]	197.5	210.1	96.36	0.2	0.02	1.53	-	-	-	-	-	0.081	-	0.0055	-	-	1.8
Cr- High carbon [15]	206.4†	212.1	97.3	0.93	0.21	0.69	0.68	0.14	-	-	-	0.013	0.004	-	0.032	-	-

In fig. 5, the calculated values of intrinsic saturation magnetisation for each of the alloys in table 4 are plotted against the measured experimental values. A linear regression was applied which yielded the following equation if solved for M_s^{exp}

$$M_s^{\text{exp}} = 1.13M_s^{\text{calc}} - 33.35 \quad (5)$$

In previous work it is assumed that the chemical composition dominates the intrinsic saturation magnetisation of the ferrite, while it is acknowledged that microstructure also plays a role [12, 15, 27]. From our analysis it is possible to quantify how dominant the chemical composition actually is. Given the significant grain size difference between samples such as nanostructured bainite with a mean ferritic plate size of $\sim 40\text{-}60 \text{ nm}$ and the superduplex stainless steel with grains up to $\sim 350 \mu\text{m}$, it can be speculated that there must be a contribution of the ferritic grain size (domain size), shape/size of the sample², and crystal structure of the ferritic phase (cubic or tetragonal) that can be incorporated to equation 4 by a constant k , which has a value of 1.052 for this study if the linear regression is performed with an intercept of zero. By providing data such as the grain and sample size in future studies, a more complete equation to predict the intrinsic saturation magnetisation

²Zhao et al. measured a 3% difference in the saturation magnetisation between small and large samples [12].

of ferrite, M_s , and hence the volume fraction of ferrite/austenite could, in principle, be determined using magnetic measurements alone.

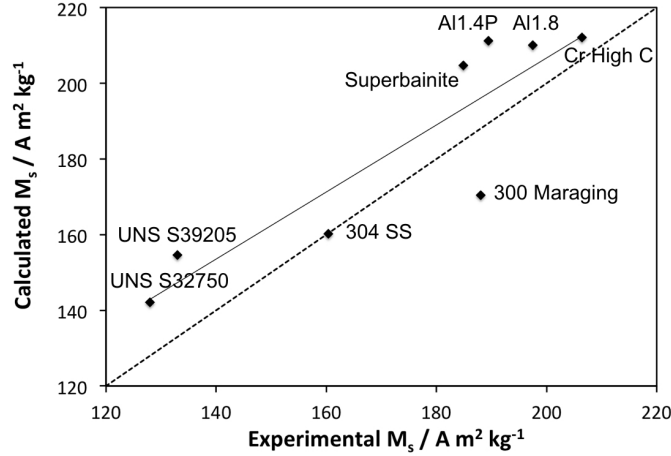


Figure 5: Calculated intrinsic saturation magnetisation against experimental values for different alloys. The continuous line is the applied linear regression and the dashed line represents perfect correspondence to the experimental data.

4. Conclusion

By performing a short magnetisation measurement at room temperature it is possible to confidently determine the amount of austenite/ferrite volume fraction of a nanostructured bainitic alloy irrespective of small compositional variations by using $V_{\alpha_b} = m_s/185.2$. Similar expressions have been derived for stainless steels with substantial compositional, grain size, and phase volume fraction differences confirming the applicability of magnetisation measurements as a reliable tool for phase quantification in steels.

A simple calculation has been performed to determine the intrinsic saturation magnetisation of ferrite based solely on the chemical composition of the ferromagnetic elements present in the alloy. The results indicate that chemical composition does not predict this property entirely and that additional parameters such as the grain size (domain size), sample size/shape, or crystal structure of the ferrite may need to be considered in the development of a generally applicable model.

5. Acknowledgements

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